


First Observation of Quantum Correlations in $e^+e^- \rightarrow X D \bar{D}$ and C -Even Constrained $D \bar{D}$ Pairs

M. Ablikim *et al.**
(BESIII Collaboration)

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The study of meson pairs produced with quantum correlations gives direct access to parameters that are challenging to measure in other systems. In this Letter, the existence of quantum correlations due to charge-conjugation symmetry C are demonstrated in $D \bar{D}$ pairs produced through the processes $e^+e^- \rightarrow D \bar{D}$, $e^+e^- \rightarrow D^* \bar{D}$, and $e^+e^- \rightarrow D^* \bar{D}^*$, where the lack of charge superscripts refers to an admixture of neutral-charm-meson particle and antiparticle states, using 7.13 fb^{-1} of e^+e^- collision data collected by the BESIII experiment between center-of-mass energies of 4.13–4.23 GeV. Processes with either C -even or C -odd constraints are identified and separated. A procedure is presented that harnesses the entangled production process to enable measurements of D^0 -meson hadronic parameters. This Letter provides the first confirmation of quantum correlations in $e^+e^- \rightarrow X D \bar{D}$ processes and the first observation of a C -even constrained $D \bar{D}$ system. The procedure is applied to measure $\delta_{K\pi}^D$, the strong phase between the $D^0 \rightarrow K^- \pi^+$ and $\bar{D}^0 \rightarrow K^- \pi^+$ decay amplitudes, which results in the determination of $\delta_{K\pi}^D = (192.8^{+11.0+1.9}_{-12.4-2.4})^\circ$. The potential for measurements of other hadronic decay parameters and charm mixing with these and future datasets is also discussed.

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Quantum correlations induced by charge-conjugation symmetry C in the production of pairs of neutral D mesons from electron-positron collisions have been well-demonstrated with data collected near energy threshold by the CLEO and BESIII Collaborations [1–4]. The production through a virtual photon and the intermediate vector $\psi(3770)$ resonance both enforce the $D \bar{D}$ final state to be C -odd, where the lack of charge superscripts on the D mesons refers to an admixture of the neutral-charm-meson particle and antiparticle states. This constraint induces interference between the mass and charge-parity (CP) eigenstates of the $c\bar{u}$ system. The interference has been harnessed to determine hadronic parameters such as the strong-phase difference between decays of D^0 and \bar{D}^0 mesons to the same final state. These hadronic parameters are critical inputs to the interpretation of mixing and CP -violation measurements in the decays of charm and beauty quarks [5,6].

The presence of such correlations for $D \bar{D}$ pairs produced in higher energy e^+e^- collisions, where additional particles may be produced, has been previously proposed [7–12] but never examined experimentally. In these collisions, the $D \bar{D}$

system can be produced as flavor-definite, or with either C -odd or C -even constraints, depending on the additional particles produced during the collision. When the accompanying particle system X is composed of only a combination of photons and π^0 mesons, the expected C eigenvalue of the $D \bar{D}$ pair is simply $(-1)^{n+1}$, where n is the number of additional photons produced in the collision. Final states that are suppressed in a C -odd initial state are enhanced in the C -even case and vice versa. Additionally, the interference of $D \bar{D}$ final states depends on the D^0 – \bar{D}^0 mixing parameters [5] x and y at first order for a C -even constrained system, where x and y are enhanced relative to a flavor-definite state [8,10]. In comparison, the dependence is quadratic in the C -odd case. This dependence introduces the opportunity for measurements of charm mixing from e^+e^- collision data using a time-integrated method.

This Letter presents the study of quantum correlations in $D \bar{D}$ pairs produced in the processes $e^+e^- \rightarrow D \bar{D}$, $e^+e^- \rightarrow D^* \bar{D}$ [13], and $e^+e^- \rightarrow D^* \bar{D}^*$, and the first observation of C -even constrained $D \bar{D}$ pairs with 7.13 fb^{-1} of e^+e^- collision data collected by the BESIII experiment between center-of-mass energies of 4.13–4.23 GeV. The correlations are exploited to measure the strong phase $\delta_{K\pi}^D$ between $D^0 \rightarrow K^- \pi^+$ and $\bar{D}^0 \rightarrow K^- \pi^+$ decays, which is described in detail in Ref. [14]. The potential for future measurements is also discussed.

The BESIII detector [15] records the data from symmetric e^+e^- collisions provided by the BEPCII storage ring

*Full author list given at the end of the Letter.

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[16]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber, a plastic scintillator time-of-flight system, and a CsI(Tl) electromagnetic calorimeter. All these detectors are enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon-identification modules interleaved with steel. The end-cap time-of-flight system was upgraded in 2015 using multigap resistive plate chamber technology. This upgrade occurred after the 1.1 fb^{-1} of data was collected at the center-of-mass energy of 4.16 GeV, but benefits all other data samples in this analysis.

Simulated samples produced with a Geant4-based [17] (MC) package, which includes the geometric description of the BESIII detector and the detector response, are used to determine detection efficiencies and estimate backgrounds. The simulation models the beam-energy spread and initial-state radiation in the e^+e^- annihilations with the generator KKMC [18]. The production of open-charm pairs, radiative production of charmonia, and continuum processes are also generated with KKMC. All particle decays are modeled with EvtGen [19,20], using branching fractions either taken from the Particle Data Group [21] when available, or otherwise estimated with Lundcharm [22,23]. Final-state radiation from charged final-state particles is incorporated using the PHOTOS package [24]. The simulation is produced without quantum correlations, allowing for a null-test comparison to the data. Simulation samples for the $e^+e^- \rightarrow D^0\bar{D}^0$, $e^+e^- \rightarrow D^{*0}\bar{D}^0$, and $e^+e^- \rightarrow D^{*0}\bar{D}^{*0}$ processes are produced with 40 times the luminosity of the data sample and scaled down for comparison.

The presence of quantum correlations is studied in five $e^+e^- \rightarrow XD\bar{D}$ production mechanisms expected to be C -definite: $D\bar{D}[C = -1]$, $D^*\bar{D} \rightarrow \gamma D\bar{D}[C = +1]$, $D^*\bar{D} \rightarrow \pi^0 D\bar{D}[C = -1]$, $D^*\bar{D}^* \rightarrow \gamma \pi^0 D\bar{D}[C = +1]$, and $D^*\bar{D}^* \rightarrow \gamma\gamma/\pi^0\pi^0 D\bar{D}[C = -1]$. Quantum correlations are demonstrated in the production mechanisms of interest through the examination of the rates of $D\bar{D}$ pairs decaying to final states expected to be forbidden or enhanced under C constraints with negligible dependence on poorly known external parameters. The examined final states are either composed of two individual CP -eigenstate D decays [25], or subject to exchange symmetries of the two D mesons imposed on the overall $D\bar{D}$ wave function. These rates are measured relative to the $D\bar{D} \rightarrow K^+\pi^-$ vs $K^-\pi^+$ final state, which has a rate that is affected negligibly by C correlations. The measured rates of both forbidden and enhanced processes are interpreted together to confirm the presence of correlations in each production mechanism with expected eigenvalue C_{exp} . The presence of the correlations is quantified through a coherence factor κ , defined by

$$\hat{C}|D\bar{D}\rangle = \kappa C_{\text{exp}}|D\bar{D}\rangle - (1 - \kappa)C_{\text{exp}}|D\bar{D}\rangle. \quad (1)$$

A sample that is completely coherent will have $\kappa = 1$, and 0.5 if exactly incoherent.

The $D\bar{D}$ pairs decaying to the final states listed in Table I are reconstructed and assigned production-mechanism hypotheses using kinematic variables. Three kinematic variables of the reconstructed $D\bar{D}$ pair are used to isolate $D\bar{D}$ and $D^*\bar{D}$ events,

$$E_{\text{miss}} \equiv E_{\text{c.m.}} - E_{D\bar{D}}, \quad c^4 M_{\text{miss},D\bar{D}}^2 \equiv E_{\text{miss}}^2 - c^2 \mathbf{p}_{D\bar{D}}^2, \\ \text{and } \Delta M_{\text{rec},D} \equiv \min(|M_{\text{rec},D} - m_{D^{*0}}|, |M_{\text{rec},\bar{D}} - m_{D^{*0}}|), \quad (2)$$

where $E_{\text{c.m.}}$ is the e^+e^- collision energy in the center-of-mass frame, $\mathbf{p}_{D\bar{D}}$ ($E_{D\bar{D}}$) is the three-momentum (energy) of the $D\bar{D}$ pair calculated under kinematic constraints to optimize resolution, $m_{D^{*0}}$ corresponds to the known D^{*0} mass [21], and the recoil mass $M_{\text{rec},D}$ is defined as

$$c^2 M_{\text{rec},D} \equiv \left[\left(E_{\text{c.m.}}^2 - \sqrt{c^2 \mathbf{p}_D^2 + c^4 m_{D^0}^2} \right)^2 - c^2 \mathbf{p}_D^2 \right]^{\frac{1}{2}}. \quad (3)$$

E_{miss} is used to isolate $e^+e^- \rightarrow D\bar{D}$ events, $\Delta M_{\text{rec},D}$ separates $e^+e^- \rightarrow D^*\bar{D}$ from $e^+e^- \rightarrow D^*\bar{D}^*$ events, and $M_{\text{miss},D\bar{D}}^2$ distinguishes between $D^*\bar{D} \rightarrow \gamma D\bar{D}$ and $D^*\bar{D} \rightarrow \pi^0 D\bar{D}$ hypotheses. For events that are not categorized as $e^+e^- \rightarrow D\bar{D}$ or $e^+e^- \rightarrow D^*\bar{D}$, a $D^* \rightarrow \gamma D$ candidate is searched for from the combination of each D candidate and additional photon candidates. Selections are applied on the reconstructed invariant mass and the recoil mass of the D^* candidate, defined similarly to Eq. (3), to suppress backgrounds. $D^*\bar{D}^* \rightarrow \gamma \pi^0 D\bar{D}$ events are isolated from the other $D^*\bar{D}^*$ decay hypotheses with the variable $M_{\text{miss},\gamma D\bar{D}}^2$, defined similarly to the variable in Eq. (2). Flavor-definite $D^0\bar{D}^0$ pairs produced from $D^{*+}D^{*-} \rightarrow \pi^+\pi^- D^0\bar{D}^0$ are suppressed with vetoes on low-momentum charged pions. It should be noted that the isolation selection requirements rely only on partial reconstruction of the final state to maximize selection efficiencies: $D^*\bar{D}$ events are identified by only reconstructing the $D\bar{D}$ pair, and only a single $D^* \rightarrow \gamma D$ candidate is reconstructed to identify $D^*\bar{D}^*$ events. Because of the low efficiency and resolution with which the slow neutral pions from $D^* \rightarrow \pi^0 D$ decays are reconstructed, this decay mode is not pursued and $D^*\bar{D}^* \rightarrow \pi^0\pi^0 D\bar{D}$ events are incorporated with low efficiency. Further details of the selection criteria are presented in Ref. [14].

The discriminating power of the selection procedure and evidence of quantum correlations are exemplified in Fig. 1 for $D\bar{D} \rightarrow K_S^0\pi^0$ vs $K_S^0\pi^0$ decays identified with $e^+e^- \rightarrow D^*\bar{D}^*$ production, where an enhancement in the data is apparent in the $D^*\bar{D}^* \rightarrow \gamma\pi^0 D\bar{D}$ [$C = +1$] region of the distribution and a suppression is seen in the

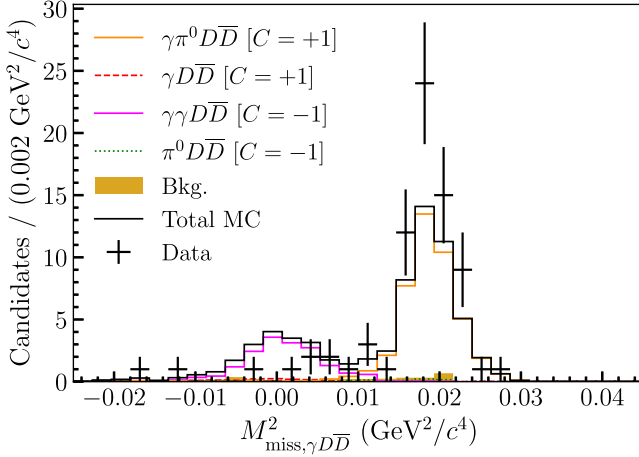


FIG. 1. $M^2_{\text{miss}, \gamma D\bar{D}}$ distribution of the $D\bar{D} \rightarrow K_S^0 \pi^0$ vs $K_S^0 \pi^0$ candidates identified with an $e^+e^- \rightarrow D^*\bar{D}^*$ hypothesis in data, compared to histograms from simulation samples produced without quantum correlations.

$D^*\bar{D}^* \rightarrow \gamma\gamma D\bar{D}[C = -1]$ region of the distribution, relative to the correlation-free simulation.

The isolation selection requirements sort correctly reconstructed $D\bar{D}$ pairs into production-mechanism hypotheses with high efficiency and purity, but still introduce non-negligible rates of production-mechanism misidentification. This means that the observed yield from a given production-mechanism hypothesis may contain contributions from $D\bar{D}$ pairs constrained to a C eigenvalue opposite to what is assumed. Production mechanism cross feed of this sort and selection and reconstruction efficiencies are simultaneously accounted for through an unfolding equation,

$$\vec{n} = A^{-1} \times \vec{N}, \quad (4)$$

where, for a given $D\bar{D}$ final state, \vec{n} gives the efficiency-corrected number of events from each production mechanism, \vec{N} contains the observed yields from each production-mechanism hypothesis, and the entries of the matrix A_{ij} give the probabilities of an event produced from production mechanism i being identified with production-mechanism hypothesis j .

Table I lists the six examined $D\bar{D}$ final states whose rates are expected to be maximally affected by the C constraints. Additional combinations of the examined CP -eigenstate decays are not considered due to limited sample sizes or large backgrounds. The six final states, the $D\bar{D} \rightarrow K^-\pi^+$ vs $K^+\pi^-$ final state considered for normalization, and the five production-mechanism hypotheses for each final state leave 35 observed yields that must be determined. This is achieved with fits to the two-dimensional distribution of the reconstructed invariant mass of the D candidates, which determines the observed yields of correctly reconstructed

TABLE I. List of examined $D\bar{D}$ final states and their expected CP eigenvalues. The rates of the first six listed final states are expected to be significantly affected by quantum correlations.

$D\bar{D} \rightarrow$		CP eigenvalue ^a	
$\pi^+\pi^-\pi^0$	vs	$K_S^0\pi^0$	-1
$\pi^+\pi^-\pi^0$	vs	K^+K^-	+1
$K_S^0\pi^0$	vs	$K_S^0\pi^0$	+1
$K_S^0\pi^0$	vs	K^+K^-	-1
$K_S^0\pi^0$	vs	$\pi^+\pi^-$	-1
$K^\pm\pi^\mp$	vs	$K^\pm\pi^\mp$	Not applicable
$K^-\pi^+$	vs	$K^+\pi^-$	Not applicable

^aThe decay $D \rightarrow \pi^+\pi^-\pi^0$ is not exactly CP -definite, but is treated as such with a correction factor based on the measured CP -even fraction [26].

$D\bar{D}$ pairs and subtracts the small contributions from backgrounds that mimic the $D\bar{D}$ final state.

The efficiency and cross-feed corrected yields for each of the six final states in Table I are determined based on Eq. (4) and expected to be significantly affected by the C constraints. The impact of the quantum correlations in each of these final states is studied as a ratio to the number of observed $D\bar{D} \rightarrow K^-\pi^+$ vs $K^+\pi^-$ decays, which has a rate expected to be modified by less than 1% from the C constraints. For simplicity of comparison, the ratios are additionally scaled by measured branching fractions and efficiencies such that the expected ratios in the absence of C correlations and mixing effects are exactly unity. For a production mechanism constrained to an eigenvalue C , the ratios for CP -eigenstate $D\bar{D}$ pairs are expected to be 0 if $C \neq CP$ and 2 otherwise [27], to linear order in mixing terms. While the $D \rightarrow K^\pm\pi^\mp$ decay is not CP -definite, the decay $D\bar{D} \rightarrow K^\pm\pi^\mp$ vs $K^\pm\pi^\mp$ is forbidden due to the requirement of antisymmetric exchange of the D and \bar{D} mesons in a C -odd constrained system, while the C -even ratio is predicted to be 2.2 due to additional enhancement from mixing effects. The measured ratios are compared to the quantum-correlated predictions in Fig. 2, which clearly demonstrate the presence of quantum correlations in all examined production mechanisms.

The information on the correlations from both enhanced and forbidden final states is combined by introducing independent coherence factors for each production mechanism, as defined in Eq. (1). The quantum-correlated predictions are reformulated to incorporate the coherence factors, and the coherence factors are then determined by a simultaneous χ^2 fit to the 30 observed yields expected to be forbidden or enhanced. Systematic uncertainties due to imperfect knowledge of reconstruction efficiencies and input branching fractions are accounted for through Gaussian constraints in the fit, but contribute very little to the determined uncertainties. The fit is of good quality, with a χ^2 per degree of freedom of 19.9/25. The fitted

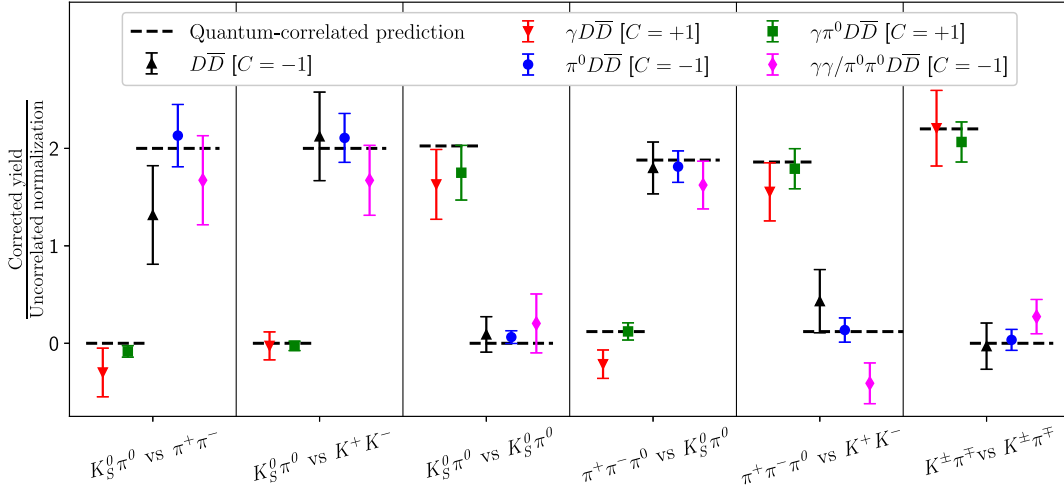


FIG. 2. The ratios of efficiency-corrected yields observed in data to those expected in the absence of correlations and mixing for each $D\bar{D}$ final state originating from each production mechanism. The displayed errors include systematic uncertainties.

coherence factors and their uncertainties are shown in Table II. The results all show good agreement with the assumption of exact coherence in each of the studied production mechanisms and are all incompatible with the absence of quantum correlations, which validates the procedure for analyzing the interference effects in $e^+e^- \rightarrow X D\bar{D}$ processes.

Given the demonstrated coherence, these samples can be leveraged to measure hadronic parameters. The procedure and results of Ref. [14] are summarized here, which employs the mixture of C -even and C -odd correlations in a novel measurement technique of $\delta_{K\pi}^D$, the strong-phase difference between $D^0 \rightarrow K^-\pi^+$ and $\bar{D}^0 \rightarrow K^-\pi^+$ decay amplitudes.

The measurement of $\delta_{K\pi}^D$ with these data proceeds similarly to what is presented in the demonstration of the correlations. Decays of $D\bar{D} \rightarrow K^\mp \pi^\pm$ vs Y are reconstructed, where Y is one of the following recoil D decay modes: $\{\pi^+\pi^-\pi^0, K^+K^-, \pi^+\pi^-, K_S^0\pi^0, K_S^0\pi^+\pi^-\}$. The $D\bar{D}$ pairs are then sorted into production-mechanism hypotheses using the same selection requirements described in the demonstration of quantum correlations, and observed yields are determined through fits to the reconstructed invariant masses of the two D candidates.

The examined CP -eigenstate recoil D decays are analyzed to measure $r_{K\pi}^D \cos \delta_{K\pi}^D$, where $r_{K\pi}^D$ is the magnitude

of the ratio of the $D^0 \rightarrow K^-\pi^+$ and $\bar{D}^0 \rightarrow K^-\pi^+$ decay amplitudes. For each of the $D\bar{D} \rightarrow K^\mp \pi^\pm$ vs CP -eigenstate samples, a χ^2 fit is performed to the ratio of observed yields from the two C -even production mechanisms to the observed yields in the three C -odd production mechanisms. The production-mechanism cross-feed corrections are parametrized in the fit, and the corrected yields relate to $r_{K\pi}^D \cos \delta_{K\pi}^D$ through the expected ratio,

$$R_{CP} = \frac{(1 - 2\lambda y)(1 + (r_{K\pi}^D)^2 + 2\lambda r_{K\pi}^D \cos \delta_{K\pi}^D)}{(1 + (r_{K\pi}^D)^2 - 2\lambda r_{K\pi}^D \cos \delta_{K\pi}^D)}, \quad (5)$$

where $\lambda = \pm 1$ corresponds to the CP eigenvalue [28] of the recoil D decay. The parameters y and $(r_{K\pi}^D)^2$ are fixed to the values from Ref. [29] in the fit, and contribute negligible uncertainty. Averaging the results of the four CP -eigenstate decays determines $r_{K\pi}^D \cos \delta_{K\pi}^D = -0.070 \pm 0.008$, where the reported uncertainty is statistical.

Samples of $D\bar{D} \rightarrow K^\mp \pi^\pm$ vs $K_S^0 \pi^+ \pi^-$ decays allow an additional determination of $r_{K\pi}^D \cos \delta_{K\pi}^D$, and are also sensitive to $r_{K\pi}^D \sin \delta_{K\pi}^D$ due to the nontrivial strong phases of the $D \rightarrow K_S^0 \pi^+ \pi^-$ decay amplitude. This sample is analyzed in bins of the $D \rightarrow K_S^0 \pi^+ \pi^-$ phase space defined by the “equal- $\Delta\delta_D$ ” binning scheme from Ref. [3]. The parameters $r_{K\pi}^D \cos \delta_{K\pi}^D$ and $r_{K\pi}^D \sin \delta_{K\pi}^D$ are determined by a simultaneous fit to the reconstructed invariant-mass distributions in each phase-space bin from each production-mechanism hypothesis, which partitions the total sample into 80 subsamples. Cross feed between phase-space bins and production mechanisms is accounted for in the fit. The $D \rightarrow K_S^0 \pi^+ \pi^-$ parameters are fixed to the values determined in Refs. [2,3], and the charm-mixing parameters x and y to the values determined in Ref. [29]. The fit determines $r_{K\pi}^D \cos \delta_{K\pi}^D = -0.044 \pm 0.014$ and $r_{K\pi}^D \sin \delta_{K\pi}^D = -0.022 \pm 0.017$, where both

TABLE II. The coherence factors determined by fit to the observed yields of the processes in Table I.

Production mechanism	κ
$D\bar{D}$	1.015 ± 0.066
$D^* \bar{D} \rightarrow \gamma D\bar{D}$	1.044 ± 0.044
$D^* \bar{D} \rightarrow \pi^0 D\bar{D}$	1.028 ± 0.024
$D^* \bar{D}^* \rightarrow \gamma \pi^0 D\bar{D}$	1.027 ± 0.017
$D^* \bar{D}^* \rightarrow \gamma \gamma / \pi^0 \pi^0 D\bar{D}$	0.963 ± 0.060

uncertainties are only statistical, with a χ^2 per degree of freedom of 85.1/73.

The results of the CP -eigenstate and $K_S^0\pi^+\pi^-$ recoil decays in this Letter are combined accounting for correlated systematic uncertainties [30] to determine $\delta_{K\pi} = (192.8^{+11.0+1.9}_{-12.4-2.4})^\circ$, with the value of $r_{K\pi}^D$ taken from Ref. [29]. The result agrees well with the most precise measurement from BESIII, performed at the $\psi(3770)$ resonance, $\delta_{K\pi}^D = (187.6^{+8.9+5.4}_{-9.7-6.4})^\circ$ [31], and a recent indirect determination from the LHCb experiment $\delta_{K\pi}^D = (190.2 \pm 2.8)^\circ$ from Ref. [29].

The presence of both C -even and C -odd correlated samples allows for robust control of systematic uncertainties. This is highlighted in comparison to Refs. [31,32], which determined $\delta_{K\pi}^D$ from $e^+e^- \rightarrow D\bar{D}$ events collected near the production threshold. The examination of the ratios of CP -eigenstate yields between C -even and C -odd correlated samples provides cancellation in all systematic uncertainties associated with reconstructing the $D\bar{D}$ final state. For reference, such systematics contributed an uncertainty roughly two-thirds of the statistical component on the determination of $r_{K\pi}^D \cos \delta_{K\pi}^D$ from CP -eigenstate decays in Ref. [31]. The mixed C constraints also benefit the analysis of $D\bar{D} \rightarrow K^\mp\pi^\pm$ vs $K_S^0\pi^+\pi^-$ decays, where the leading uncertainties arise from the measurements of hadronic parameters of the $D \rightarrow K_S^0\pi^+\pi^-$ decay determined in Ref. [3]. The total systematic uncertainty on the determination of $\delta_{K\pi}^D$ in this Letter is reduced by roughly a factor of 3 compared to Ref. [31], and arises from production-mechanism cross-feed corrections and modeling small background contributions.

The total precision of this measurement with 7.13 fb^{-1} of data collected between $E_{\text{c.m.}} = 4.13\text{--}4.23 \text{ GeV}$ is roughly equivalent to the previous measurement with 2.93 fb^{-1} of BESIII data collected at $E_{\text{c.m.}} = 3.77 \text{ GeV}$ presented in Ref. [31]. The analysis presented in this Letter determines $\delta_{K\pi}^D$ with a larger statistical uncertainty despite a larger integrated luminosity and comparable inclusive cross section of $e^+e^- \rightarrow D\bar{D}$. The larger statistical uncertainty arises from the challenge of D decays with missing particles in the final state, such as $D^0 \rightarrow K_L^0\pi^+\pi^-$, as the production mechanisms are partially reconstructed to optimize the yields of fully reconstructed $D\bar{D}$ final states, and from the low efficiency with which $D^*\bar{D}^* \rightarrow \pi^0\pi^0D\bar{D}$ decays are reconstructed. Despite this, the analysis presented in this Letter demonstrates that D meson strong-phase measurements with e^+e^- data collected at higher energy ranges would complement the established approach of studying D strong phases with data collected near the $\psi(3770)$ energy threshold.

Given the similar sensitivities, the result from this measurement is combined with the result from Ref. [31] accounting for correlated uncertainties due to the assumed hadronic parameters of the $D \rightarrow K_S^0\pi^+\pi^-$ decay. The combined analysis gives $\delta_{K\pi}^D = (189.2^{+6.9+3.4}_{-7.4-3.8})^\circ$.

Measurements of C -even constrained $D\bar{D}$ pairs similar to those presented in this Letter with future datasets of e^+e^- collisions collected by BESIII and the proposed super τ -charm facility (STCF) [33] could also constrain the values of parameters related to charm-mixing and indirect CP violation, as discussed in Refs. [7–9,11,34]. Based on the procedure presented in this Letter, the sensitivity of STCF to the charm-mixing parameters x and y and the parameters corresponding to CP violation in mixing [5], $|q/p|$ and ϕ , is examined. The sensitivities at several center-of-mass energies primarily proposed for other physics goals are analyzed: $E_{\text{c.m.}} = 4.01 \text{ GeV}$, $E_{\text{c.m.}} = 4.18 \text{ GeV}$, and $E_{\text{c.m.}} = 4.26 \text{ GeV}$. However, center-of-mass energies near the $\psi(4040)$ resonance are expected to be optimal for collection of quantum-correlated $D\bar{D}$ pairs due to large cross sections of both the $e^+e^- \rightarrow D^*\bar{D}$ and $e^+e^- \rightarrow D^*\bar{D}^*$ processes, so the sensitivity from data collected at $E_{\text{c.m.}} = 4.03 \text{ GeV}$ is also considered. Assumed cross sections are taken from the measurements in Ref. [35], and reconstruction efficiencies are estimated based on current BESIII results. All combinations of the decay modes considered in this Letter, the $D \rightarrow K^\mp\pi^\pm\pi^0$ decay, and the $D \rightarrow K^\mp\pi^\pm\pi^+\pi^-$ decay using the binned results from Ref. [4] are included in the sensitivity studies. The best known values for branching fractions [21] and hadronic parameters [3,4,29] are assumed, and the uncertainty on these parameters is neglected as sufficient future precision can be achieved with the C -odd samples produced from the same data. The possibility of direct CP violation is neglected, although it should be noted that the correlated C -odd production mechanisms could be used to probe such effects due to their quadratic dependence on mixing parameters [8,36]. The precision with the considered decays modes assuming 1 ab^{-1} at each energy point is shown in Table III, which allows for comparison in sensitivity at these energy points. The final distribution of luminosity at STCF should be informed by more detailed studies of the $e^+e^- \rightarrow D^*\bar{D}$ and $D^*\bar{D}^*$ production cross sections near the $\psi(4040)$ resonance and will need to be optimized against competing physics goals. It should be

TABLE III. Projected statistical sensitivity to charm-mixing parameters with 1 ab^{-1} at various e^+e^- collision energies using the D decay modes considered in this Letter and the $D \rightarrow K^\mp\pi^\pm\pi^0$ and $D \rightarrow K^\mp\pi^\pm\pi^+\pi^-$ decays. The combined sensitivity with 1 ab^{-1} samples at each energy is also shown.

$E_{\text{c.m.}}$ (GeV)	x (10^{-4})	y (10^{-4})	$ q/p $ (%)	ϕ ($^\circ$)
4.01	8.3	2.4	4.4	3.2
4.03	6.9	2.0	3.4	2.5
4.18	7.9	2.3	4.1	3.0
4.26	11.4	3.2	6.7	4.8
Combined (4 ab^{-1})	5.6	1.5	2.1	1.6

noted that the stated sensitivities depend strongly on the assumed hadronic parameters of the included modes.

The results of the sensitivity studies suggest that measurement techniques similar to those presented in this Letter at a high-intensity charm factory such as STCF would provide roughly equivalent sensitivity to the current global averages [29,37] dominated by results from the LHCb Collaboration: 4.4×10^{-4} on x , 2.1×10^{-4} on y , 1.8% on $|q/p|$, and 1.2° on ϕ . This would provide the first confirmation of a nonzero mass difference between neutral- D -meson mass eigenstates outside of the LHCb Collaboration and independent confirmation of other parameters to current precision from a vastly different measurement technique. The inclusion of additional decay modes such as $D \rightarrow K^\mp e^\pm \nu_e$, considered in Ref. [10], and $D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$, whose strong phases are not currently well-known, would additionally improve the expected precision on charm-mixing parameters.

In this Letter, the first demonstration of quantum correlations of $D\bar{D}$ pairs produced in $e^+e^- \rightarrow X D\bar{D}$ decays has been presented, including the first observation of C -even correlated $D\bar{D}$ pairs. These processes have been employed to measure the strong phase between $D^0 \rightarrow K^- \pi^+$ and $\bar{D}^0 \rightarrow K^- \pi^+$ decays, finding $\delta_{K\pi} = (192.8_{-12.4-2.4}^{+11.0+1.9})^\circ$. This opens up new prospects for the measurement of D -meson hadronic parameters and paves the way toward time-integrated measurements of D^0 - \bar{D}^0 mixing from e^+e^- colliders.

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Data availability—The data that support the findings of this article are not publicly available upon publication because it is not technically feasible and/or the cost of preparing, depositing, and hosting the data would be prohibitive within the terms of this research project. The data are available from the authors upon reasonable request.

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 T. Ma,^{73,59} X. T. Ma,^{1,65} X. Y. Ma,^{1,59} Y. M. Ma,³² F. E. Maas,¹⁹ I. MacKay,⁷¹ M. Maggiora,^{76a,76c} S. Malde,⁷¹ Q. A. Malik,⁷⁵
 H. X. Mao,^{39,k,l} Y. J. Mao,^{47,h} Z. P. Mao,¹ S. Marcello,^{76a,76c} A. Marshall,⁶⁴ F. M. Melendi,^{30a,30b} Y. H. Meng,⁶⁵ Z. X. Meng,⁶⁸
 G. Mezzadri,^{30a} H. Miao,^{1,65} T. J. Min,⁴³ R. E. Mitchell,²⁸ X. H. Mo,^{1,59,65} B. Moses,²⁸ N. Yu. Muchnoi,^{4,c} J. Muskalla,³⁶
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 G. B. Sun,⁷⁸ G. X. Sun,¹ H. Sun,⁶⁵ H. K. Sun,¹ J. F. Sun,²⁰ K. Sun,⁶² L. Sun,⁷⁸ S. S. Sun,^{1,65} T. Sun,^{52,f} Y. C. Sun,⁷⁸
 Y. H. Sun,³¹ Y. J. Sun,^{73,59} Y. Z. Sun,¹ Z. Q. Sun,^{1,65} Z. T. Sun,⁵¹ C. J. Tang,⁵⁵ G. Y. Tang,¹ J. Tang,⁶⁰ J. J. Tang,^{73,59}
 L. F. Tang,⁴⁰ Y. A. Tang,⁷⁸ L. Y. Tao,⁷⁴ M. Tat,⁷¹ J. X. Teng,^{73,59} J. Y. Tian,^{73,59} W. H. Tian,⁶⁰ Y. Tian,³² Z. F. Tian,⁷⁸
 I. Uman,^{63b} B. Wang,⁶⁰ B. Wang,¹ Bo Wang,^{73,59} C. Wang,^{39,k,l} C. Wang,²⁰ Cong Wang,²³ D. Y. Wang,^{47,h} H. J. Wang,^{39,k,l}
 J. J. Wang,⁷⁸ K. Wang,^{1,59} L. L. Wang,¹ L. W. Wang,³⁵ M. Wang,^{73,59} M. Wang,⁵¹ N. Y. Wang,⁶⁵ S. Wang,^{12,g} T. Wang,^{12,g}
 T. J. Wang,⁴⁴ W. Wang,⁶⁰ W. Wang,⁷⁴ W. P. Wang,^{36,59,73,o} X. Wang,^{47,h} X. F. Wang,^{39,k,l} X. J. Wang,⁴⁰ X. L. Wang,^{12,g}
 X. N. Wang,^{1,65} Y. Wang,⁶² Y. D. Wang,⁴⁶ Y. F. Wang,^{1,8,65} Y. H. Wang,^{39,k,l} Y. J. Wang,^{73,59} Y. L. Wang,²⁰ Y. N. Wang,⁷⁸
 Y. Q. Wang,¹ Yaqian Wang,¹⁸ Yi Wang,⁶² Yuan Wang,^{18,32} Z. Wang,^{1,59} Z. L. Wang,⁷⁴ Z. L. Wang,² Z. Q. Wang,^{12,g}
 Z. Y. Wang,^{1,65} D. H. Wei,¹⁴ H. R. Wei,⁴⁴ F. Weidner,⁷⁰ S. P. Wen,¹ Y. R. Wen,⁴⁰ U. Wiedner,³ G. Wilkinson,⁷¹ M. Wolke,⁷⁷
 C. Wu,⁴⁰ J. F. Wu,^{1,8} L. H. Wu,¹ L. J. Wu,²⁰ L. J. Wu,^{1,65} Lianjie Wu,²⁰ S. G. Wu,^{1,65} S. M. Wu,⁶⁵ X. Wu,^{12,g} X. H. Wu,³⁵
 Y. J. Wu,³² Z. Wu,^{1,59} L. Xia,^{73,59} X. M. Xian,⁴⁰ B. H. Xiang,^{1,65} D. Xiao,^{39,k,l} G. Y. Xiao,⁴³ H. Xiao,⁷⁴ Y. L. Xiao,^{12,g}
 Z. J. Xiao,⁴² C. Xie,⁴³ K. J. Xie,^{1,65} X. H. Xie,^{47,h} Y. Xie,⁵¹ Y. G. Xie,^{1,59} Y. H. Xie,⁶ Z. P. Xie,^{73,59} T. Y. Xing,^{1,65} C. F. Xu,^{1,65}
 C. J. Xu,⁶⁰ G. F. Xu,¹ H. Y. Xu,² H. Y. Xu,^{68,2} M. Xu,^{73,59} Q. J. Xu,¹⁷ Q. N. Xu,³¹ T. D. Xu,⁷⁴ W. Xu,¹ W. L. Xu,⁶⁸ X. P. Xu,⁵⁶
 Y. Xu,⁴¹ Y. Xu,^{12,g} Y. C. Xu,⁷⁹ Z. S. Xu,⁶⁵ F. Yan,^{12,g} H. Y. Yan,⁴⁰ L. Yan,^{12,g} W. B. Yan,^{73,59} W. C. Yan,⁸² W. H. Yan,⁶
 W. P. Yan,²⁰ X. Q. Yan,^{1,65} H. J. Yang,^{52,f} H. L. Yang,³⁵ H. X. Yang,¹ J. H. Yang,⁴³ R. J. Yang,²⁰ T. Yang,¹ Y. Yang,^{12,g}

Y. F. Yang,⁴⁴ Y. H. Yang,⁴³ Y. Q. Yang,⁹ Y. X. Yang,^{1,65} Y. Z. Yang,²⁰ M. Ye,^{1,59} M. H. Ye,^{8,a} Z. J. Ye,^{57,j} Junhao Yin,⁴⁴ Z. Y. You,⁶⁰ B. X. Yu,^{1,59,65} C. X. Yu,⁴⁴ G. Yu,¹³ J. S. Yu,^{26,i} L. Q. Yu,^{12,g} M. C. Yu,⁴¹ T. Yu,⁷⁴ X. D. Yu,^{47,h} Y. C. Yu,⁸² C. Z. Yuan,^{1,65} H. Yuan,^{1,65} J. Yuan,³⁵ J. Yuan,⁴⁶ L. Yuan,² S. C. Yuan,^{1,65} X. Q. Yuan,¹ Y. Yuan,^{1,65} Z. Y. Yuan,⁶⁰ C. X. Yue,⁴⁰ Ying Yue,²⁰ A. A. Zafar,⁷⁵ S. H. Zeng,⁶⁴ X. Zeng,^{12,g} Y. Zeng,^{26,i} Y. J. Zeng,⁶⁰ Y. J. Zeng,^{1,65} X. Y. Zhai,³⁵ Y. H. Zhan,⁶⁰ A. Q. Zhang,^{1,65} B. L. Zhang,^{1,65} B. X. Zhang,¹ D. H. Zhang,⁴⁴ G. Y. Zhang,^{1,65} G. Y. Zhang,²⁰ H. Zhang,^{73,59} H. Zhang,⁸² H. C. Zhang,^{1,59,65} H. H. Zhang,⁶⁰ H. Q. Zhang,^{1,59,65} H. R. Zhang,^{73,59} H. Y. Zhang,^{1,59} J. Zhang,⁸² J. Zhang,⁶⁰ J. J. Zhang,⁵³ J. L. Zhang,²¹ J. Q. Zhang,⁴² J. S. Zhang,^{12,g} J. W. Zhang,^{1,59,65} J. X. Zhang,^{39,k,1} J. Y. Zhang,¹ J. Z. Zhang,^{1,65} Jianyu Zhang,⁶⁵ L. M. Zhang,⁶² Lei Zhang,⁴³ N. Zhang,⁸² P. Zhang,^{1,8} Q. Zhang,²⁰ Q. Y. Zhang,³⁵ R. Y. Zhang,^{39,k,1} S. H. Zhang,^{1,65} Shulei Zhang,^{26,i} X. M. Zhang,¹ X. Y. Zhang,⁴¹ X. Y. Zhang,⁵¹ Y. Zhang,¹ Y. Zhang,⁷⁴ Y. T. Zhang,⁸² Y. H. Zhang,^{1,59} Y. M. Zhang,⁴⁰ Y. P. Zhang,^{73,59} Z. D. Zhang,¹ Z. H. Zhang,¹ Z. L. Zhang,⁵⁶ Z. L. Zhang,³⁵ Z. X. Zhang,²⁰ Z. Y. Zhang,⁷⁸ Z. Y. Zhang,⁴⁴ Z. Z. Zhang,⁴⁶ Zh. Zh. Zhang,²⁰ G. Zhao,¹ J. Y. Zhao,^{1,65} J. Z. Zhao,^{1,59} L. Zhao,¹ L. Zhao,^{73,59} M. G. Zhao,⁴⁴ N. Zhao,⁸⁰ R. P. Zhao,⁶⁵ S. J. Zhao,⁸² Y. B. Zhao,^{1,59} Y. L. Zhao,⁵⁶ Y. X. Zhao,^{32,65} Z. G. Zhao,^{73,59} A. Zhemchugov,^{37,b} B. Zheng,⁷⁴ B. M. Zheng,³⁵ J. P. Zheng,^{1,59} W. J. Zheng,^{1,65} X. R. Zheng,²⁰ Y. H. Zheng,^{65,p} B. Zhong,⁴² C. Zhong,²⁰ H. Zhou,^{36,51,o} J. Q. Zhou,³⁵ J. Y. Zhou,³⁵ S. Zhou,⁶ X. Zhou,⁷⁸ X. K. Zhou,⁶ X. R. Zhou,^{73,59} X. Y. Zhou,⁴⁰ Y. X. Zhou,⁷⁹ Y. Z. Zhou,^{12,g} A. N. Zhu,⁶⁵ J. Zhu,⁴⁴ K. Zhu,¹ K. J. Zhu,^{1,59,65} K. S. Zhu,^{12,g} L. Zhu,³⁵ L. X. Zhu,⁶⁵ S. H. Zhu,⁷² T. J. Zhu,^{12,g} W. D. Zhu,^{12,g} W. D. Zhu,⁴² W. J. Zhu,¹ W. Z. Zhu,²⁰ Y. C. Zhu,^{73,59} Z. A. Zhu,^{1,65} X. Y. Zhuang,⁴⁴ J. H. Zou,¹ and J. Zu^{73,59}

(BESIII Collaboration)

¹*Institute of High Energy Physics, Beijing 100049, People's Republic of China*

²*Beihang University, Beijing 100191, People's Republic of China*

³*Bochum Ruhr-University, D-44780 Bochum, Germany*

⁴*Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia*

⁵*Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA*

⁶*Central China Normal University, Wuhan 430079, People's Republic of China*

⁷*Central South University, Changsha 410083, People's Republic of China*

⁸*China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China*

⁹*China University of Geosciences, Wuhan 430074, People's Republic of China*

¹⁰*Chung-Ang University, Seoul, 06974, Republic of Korea*

¹¹*COMSATS University Islamabad, Lahore Campus, Defence Road, Off Raiwind Road, 54000 Lahore, Pakistan*

¹²*Fudan University, Shanghai 200433, People's Republic of China*

¹³*GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany*

¹⁴*Guangxi Normal University, Guilin 541004, People's Republic of China*

¹⁵*Guangxi University, Nanning 530004, People's Republic of China*

¹⁶*Guangxi University of Science and Technology, Liuzhou 545006, People's Republic of China*

¹⁷*Hangzhou Normal University, Hangzhou 310036, People's Republic of China*

¹⁸*Hebei University, Baoding 071002, People's Republic of China*

¹⁹*Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany*

²⁰*Henan Normal University, Xinxiang 453007, People's Republic of China*

²¹*Henan University, Kaifeng 475004, People's Republic of China*

²²*Henan University of Science and Technology, Luoyang 471003, People's Republic of China*

²³*Henan University of Technology, Zhengzhou 450001, People's Republic of China*

²⁴*Huangshan College, Huangshan 245000, People's Republic of China*

²⁵*Hunan Normal University, Changsha 410081, People's Republic of China*

²⁶*Hunan University, Changsha 410082, People's Republic of China*

²⁷*Indian Institute of Technology Madras, Chennai 600036, India*

²⁸*Indiana University, Bloomington, Indiana 47405, USA*

^{29a}*INFN Laboratori Nazionali di Frascati, I-00044, Frascati, Italy*

^{29b}*INFN Sezione di Perugia, I-06100, Perugia, Italy*

^{29c}*University of Perugia, I-06100, Perugia, Italy*

^{30a}*INFN Sezione di Ferrara, I-44122, Ferrara, Italy*

^{30b}*University of Ferrara, I-44122, Ferrara, Italy*

³¹*Inner Mongolia University, Hohhot 010021, People's Republic of China*

³²*Institute of Modern Physics, Lanzhou 730000, People's Republic of China*

- ³³*Institute of Physics and Technology, Mongolian Academy of Sciences, Peace Avenue 54B, Ulaanbaatar 13330, Mongolia*
- ³⁴*Instituto de Alta Investigación, Universidad de Tarapacá, Casilla 7D, Arica 1000000, Chile*
- ³⁵*Jilin University, Changchun 130012, People's Republic of China*
- ³⁶*Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany*
- ³⁷*Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia*
- ³⁸*Justus-Liebig-Universität Giessen, II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany*
- ³⁹*Lanzhou University, Lanzhou 730000, People's Republic of China*
- ⁴⁰*Liaoning Normal University, Dalian 116029, People's Republic of China*
- ⁴¹*Liaoning University, Shenyang 110036, People's Republic of China*
- ⁴²*Nanjing Normal University, Nanjing 210023, People's Republic of China*
- ⁴³*Nanjing University, Nanjing 210093, People's Republic of China*
- ⁴⁴*Nankai University, Tianjin 300071, People's Republic of China*
- ⁴⁵*National Centre for Nuclear Research, Warsaw 02-093, Poland*
- ⁴⁶*North China Electric Power University, Beijing 102206, People's Republic of China*
- ⁴⁷*Peking University, Beijing 100871, People's Republic of China*
- ⁴⁸*Qufu Normal University, Qufu 273165, People's Republic of China*
- ⁴⁹*Renmin University of China, Beijing 100872, People's Republic of China*
- ⁵⁰*Shandong Normal University, Jinan 250014, People's Republic of China*
- ⁵¹*Shandong University, Jinan 250100, People's Republic of China*
- ⁵²*Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China*
- ⁵³*Shanxi Normal University, Linfen 041004, People's Republic of China*
- ⁵⁴*Shanxi University, Taiyuan 030006, People's Republic of China*
- ⁵⁵*Sichuan University, Chengdu 610064, People's Republic of China*
- ⁵⁶*Soochow University, Suzhou 215006, People's Republic of China*
- ⁵⁷*South China Normal University, Guangzhou 510006, People's Republic of China*
- ⁵⁸*Southeast University, Nanjing 211100, People's Republic of China*
- ⁵⁹*State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China*
- ⁶⁰*Sun Yat-Sen University, Guangzhou 510275, People's Republic of China*
- ⁶¹*Suranaree University of Technology, University Avenue 111, Nakhon Ratchasima 30000, Thailand*
- ⁶²*Tsinghua University, Beijing 100084, People's Republic of China*
- ^{63a}*Turkish Accelerator Center Particle Factory Group, Istinye University, 34010, Istanbul, Turkey*
- ^{63b}*Near East University, Nicosia, North Cyprus, 99138, Mersin 10, Turkey*
- ⁶⁴*University of Bristol, H H Wills Physics Laboratory, Tyndall Avenue, Bristol BS8 1TL, United Kingdom*
- ⁶⁵*University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China*
- ⁶⁶*University of Groningen, NL-9747 AA Groningen, The Netherlands*
- ⁶⁷*University of Hawaii, Honolulu, Hawaii 96822, USA*
- ⁶⁸*University of Jinan, Jinan 250022, People's Republic of China*
- ⁶⁹*University of Manchester, Oxford Road, Manchester M13 9PL, United Kingdom*
- ⁷⁰*University of Muenster, Wilhelm-Klemm-Strasse 9, 48149 Muenster, Germany*
- ⁷¹*University of Oxford, Keble Road, Oxford OX13RH, United Kingdom*
- ⁷²*University of Science and Technology Liaoning, Anshan 114051, People's Republic of China*
- ⁷³*University of Science and Technology of China, Hefei 230026, People's Republic of China*
- ⁷⁴*University of South China, Hengyang 421001, People's Republic of China*
- ⁷⁵*University of the Punjab, Lahore-54590, Pakistan*
- ^{76a}*University of Turin and INFN, I-10125, Turin, Italy*
- ^{76b}*University of Eastern Piedmont, I-15121, Alessandria, Italy*
- ^{76c}*INFN, I-10125, Turin, Italy*
- ⁷⁷*Uppsala University, Box 516, SE-75120 Uppsala, Sweden*
- ⁷⁸*Wuhan University, Wuhan 430072, People's Republic of China*
- ⁷⁹*Yantai University, Yantai 264005, People's Republic of China*
- ⁸⁰*Yunnan University, Kunming 650500, People's Republic of China*
- ⁸¹*Zhejiang University, Hangzhou 310027, People's Republic of China*
- ⁸²*Zhengzhou University, Zhengzhou 450001, People's Republic of China*

^aDeceased.

^bAlso at the Moscow Institute of Physics and Technology, Moscow 141700, Russia.

^cAlso at the Novosibirsk State University, Novosibirsk, 630090, Russia.

^dAlso at the NRC "Kurchatov Institute," PNPI, 188300, Gatchina, Russia.

^eAlso at Goethe University Frankfurt, 60323 Frankfurt am Main, Germany.

^fAlso at Key Laboratory for Particle Physics, Astrophysics and Cosmology, Ministry of Education; Shanghai Key Laboratory for Particle Physics and Cosmology; Institute of Nuclear and Particle Physics, Shanghai 200240, People's Republic of China.

^gAlso at Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443, People's Republic of China.

^hAlso at State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, People's Republic of China.

ⁱAlso at School of Physics and Electronics, Hunan University, Changsha 410082, China.

^jAlso at Guangdong Provincial Key Laboratory of Nuclear Science, Institute of Quantum Matter, South China Normal University, Guangzhou 510006, China.

^kAlso at MOE Frontiers Science Center for Rare Isotopes, Lanzhou University, Lanzhou 730000, People's Republic of China.

^lAlso at Lanzhou Center for Theoretical Physics, Lanzhou University, Lanzhou 730000, People's Republic of China.

^mAlso at the Department of Mathematical Sciences, IBA, Karachi 75270, Pakistan.

ⁿAlso at Ecole Polytechnique Federale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland.

^oAlso at Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany.

^pAlso at Hangzhou Institute for Advanced Study, University of Chinese Academy of Sciences, Hangzhou 310024, China.