Observation of $e^+e^- \rightarrow \phi \chi_{c1}$ and $\phi \chi_{c2}$ at $\sqrt{s} = 4.600$ GeV

Observation of e⁺e⁻ → φχ_{c1} and φχ_{c2} at √s = 4.600 GeV

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Using a data sample collected with the BESIII detector operating at the BEPCII storage ring at a centerof-mass energy of $\sqrt{s} = 4.600$ GeV, we search for the production of $e^+e^- \to \phi \chi_{c0.1.2}$. A search is also performed for the charmonium-like state X(4140) in the radiative transition $e^+e^- \rightarrow \gamma X(4140)$ with X(4140) subsequently decaying into $\phi J/\psi$. The processes $e^+e^- \to \phi \chi_{c1}$ and $\phi \chi_{c2}$ are observed for the first time, each with a statistical significance of more than 10σ , and the Born cross sections are measured to be $(4.2^{+1.7}_{-1.0} \pm 0.3)$ and $(6.7^{+3.4}_{-1.7} \pm 0.5)$ pb, respectively, where the first uncertainties are statistical and the second systematic. No significant signals are observed for $e^+e^- \to \phi \chi_{c0}$ and $e^+e^- \to \gamma X(4140)$ and upper limits on the Born cross sections at 90% C.L. are provided at $\sqrt{s} = 4.600$ GeV.

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I. INTRODUCTION

In recent years, many charmonium-like states have been observed experimentally, whose characters are different from the predictions of the charmonium states in the potential model. The X(3872) was first observed by the Belle Collaboration in $B^{\pm} \to K^{\pm} \pi^{+} \pi^{-} J/\psi$ [1] and was subsequently confirmed by several other experiments [2–5]. The vector states X(4260), X(4360), and X(4660), sometimes called the Y(4260), Y(4360), and Y(4660), were discovered by the BABAR, Belle, and CLEO

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collaborations via their decays into low-mass charmonium states $\pi^{+}\pi^{-}J/\psi$ or $\pi^{+}\pi^{-}\psi(3686)$ [6–10]. Some charged charmonium-like states and their neutral partners, such as $Z_c(3900), Z_c(3885), Z_c(4020), Z_c(4025), Z_c(4200)$ have been also observed by several experiments [11-21]. There are many theoretical interpretations of the nature of these XYZ states, such as molecular, hybrid, or multiquark states, threshold enhancements, or some other configurations [22]. However, the nature of these states is still unclear. Due to the richness of XYZ states above the open charm threshold. searching for new decay modes of these states and measuring their line shape precisely will provide helpful information to determine their properties.

The authors of Ref. [23] predicted a sizable coupling between the X(4260) and the $\omega \chi_{c0}$ channel by considering the threshold effect of the $\omega\chi_{c0}$. The BESIII Collaboration measured the cross sections of $e^+e^- \rightarrow \omega \chi_{c0,1,2}$ at c.m. energies between 4.23 and 4.60 GeV and determined the mass of an intermediate resonance to be about 4226 MeV/ c^2 , assuming that the $\omega \chi_{c0}$ signals come from a single resonance [24,25]. These resonant parameters are also inconsistent with those obtained by fitting a single resonance to the $\pi^+\pi^-J/\psi$ cross section [6,7]. Recently, the BESIII Collaboration precisely measured the cross section of $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ in the relevant mass range and observed two resonant structures whose masses are determined to be 4224 and 4319 MeV/ c^2 [26]. The mass of the first state is lower than that from BABAR and Belle measurements corresponding to the X(4260). The fact that the parameters of the X(4260) agree with the structure observed by the BESIII Collaboration in $e^+e^- \rightarrow \omega \chi_{c0}$ suggests that the X(4260) has multiple decay modes. Considering that ω and ϕ mesons have the same spin, parity, and isospin, $\omega \chi_{cJ}$ and $\phi \chi_{cJ}$ may have a similar

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production mechanism. Therefore, we study and measure the cross sections of $e^+e^- \rightarrow \phi \chi_{c0,1,2}$.

The X(4140), sometimes called the Y(4140), was first reported by the CDF experiment in the decay $B^+ \rightarrow$ $\phi J/\psi K^+$ [27]. However, the existence of the X(4140)was neither confirmed by the Belle [28] and BABAR [29] collaborations in the same process, nor by Belle Collaboration in two-photon production [28]. Recently, the CMS [30] and DØ [31] collaborations reported the observation of the X(4140) with resonant parameters being consistent with those of the CDF measurement. More recently, the LHCb Collaboration observed the X(4140)with a statistical significance of 8.4σ using a 3 fb⁻¹ data sample of pp collisions in the same process [32], using a full amplitude analysis. The BESIII Collaboration has searched for the X(4140) in the process $e^+e^- \rightarrow \gamma \phi J/\psi$ with data samples at c.m. energies $\sqrt{s} = 4.23$, 4.26, and 4.36 GeV [33], but no obvious signal has been observed. In this article, we present the results of a study of $e^+e^- \rightarrow \phi \chi_{c0,1,2}$ and a search for the X(4140) in the process $e^+e^- \rightarrow \gamma X(4140) \rightarrow \gamma \phi J/\psi$, based on an $e^+e^$ annihilation data sample collected with the BESIII detector [34] at $\sqrt{s} = 4.600$ GeV. The c.m. energy of the data sample is determined with a precision of 0.8 MeV [35] using dimuon events. The integrated luminosity of the sample is measured using large-angle Bhabha scattering to be 567 pb^{-1} with a precision of 1.0% [36].

II. DETECTOR AND MONTE CARLO SAMPLES

The Beijing Spectrometer III (BESIII) detector, described in detail in Ref. [34], is a magnetic spectrometer operating at the Beijing Electron-Positron collider (BEPCII), which is a double-ring e^+e^- collider with a c.m. energy range from 2.0 to 4.6 GeV. The cylindrical core of the BESIII detector consists of a helium-based main drift chamber (MDC), a plastic scintillator time-of-flight (TOF) system, and a CsI(Tl) electromagnetic calorimeter (EMC) that are all enclosed in a superconducting solenoid magnet providing a 1.0 T magnetic field. The magnet is supported by an octagonal flux-return yoke with modules of resistive plate muon counters (MUC) interleaved with steel. The acceptance of the MDC for charged tracks is 93% of a 4π solid angle. It provides a charged particle momentum resolution of 0.5% at 1.0 GeV/c and ionization energy loss (dE/dx) measurements with resolution better than 6%. The time resolution of the TOF is 80(110) ps for the barrel (end caps) and the EMC measures photon energy with a resolution of 2.5%(5%) at 1.0 GeV in the barrel (end caps). The MUC provides a position resolution of 2 cm and detects muon tracks with momenta higher than 0.5 GeV/c.

The optimization of event selection, determination of the detection efficiency, and estimation of the backgrounds are performed using the GEANT4-based [37] Monte Carlo (MC)

simulation software BOOST [38]. It includes the geometric and material description for the BESIII detector and a simulation of the detector response. Signal MC samples of $e^+e^- \rightarrow \phi \chi_{c0,1,2}$ and $e^+e^- \rightarrow \gamma X(4140) \rightarrow \gamma \phi J/\psi$ are generated at $\sqrt{s} = 4.600$ GeV, where each sample contains 10^5 events. Both χ_{c1} and χ_{c2} states are reconstructed via $\chi_{c1,2} \to \gamma J/\psi$, $J/\psi \to \ell^+ \ell^-$ ($\ell = e$ or μ), and ϕ via its decay to K^+K^- . For $e^+e^- \to \phi \chi_{c0}$, since the branching fraction of $\chi_{c0} \to \gamma J/\psi$, with $J/\psi \to \ell^+ \ell^-$ is smaller than those of $\chi_{c0} \to \pi^+ \pi^-$, $K^+ K^-$, $\pi^+ \pi^- \pi^+ \pi^-$, and $K^+ K^- \pi^+ \pi^-$, the χ_{c0} state is reconstructed with the latter four channels. Initial-state radiation effects are simulated with KKMC [39], where the production cross sections are assumed to follow the line shape of the X(4660) [10], modified by a phasespace factor. Final-state radiation effects associated with charged particles are handled with PHOTOS [40].

An "inclusive" MC sample is also generated with an integrated luminosity equivalent to that of the data sample. QED events—such as $e^+e^- \rightarrow e^+e^-$, $\mu^+\mu^-$, and $\gamma\gamma$ —are generated with BABAYAGA [41]. The processes including an intermediate $D_{(s)}^{(*)}$ meson (such as $e^+e^- \rightarrow D\bar{D}$, $D^*\bar{D}^*$, $D\bar{D}^* + \text{c.c.}$, $D_s^+D_s^-$, $D_s^+D_s^{*-} + \text{c.c.}$, and $D_s^{*+}D_s^{*-}$), the known charmonium production processes, and the process $e^+e^- \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$ with all of their known decays are generated using EVTGEN [42]. The unmeasured but possible decays associated to charmonium states are generated with LUNDCHARM [43] and other hadronic events are generated with PYTHIA [44].

III. $e^+e^- \rightarrow \phi \chi_{c1}$ AND $\phi \chi_{c2}$ A. Event selection

The final states for $e^+e^- \rightarrow \phi \chi_{c1}$ and $\phi \chi_{c2}$ are $\gamma K^+ K^- \ell^+ \ell^-$. For each charged track in the MDC, the polar angle must satisfy $|\cos\theta| < 0.93$ and the point of closest approach to the e^+e^- interaction point must be within ± 10 cm in the beam direction and within 1 cm in the plane perpendicular to the beam direction. We require that there are at least three candidate charged tracks in the final state. Leptons from J/ψ decays can be separated from other tracks kinematically; hence, the two tracks with momenta greater than 1.0 GeV/c and opposite charge are assumed to be leptons. The energy deposited in the EMC is used to separate electrons from muons. For muon candidates, the deposited energy is required to be less than 0.6 GeV, while for electron candidates it is required to be greater than 1.0 GeV. The momenta of the kaons are about 0.2 GeV/c in the laboratory frame, and low-momentum kaons significantly affect the reconstruction efficiency. To increase the efficiency, only one kaon is required to be reconstructed and pass the particle identification (PID) requirements. For each charged track with low momentum, the PID probability $Prob_i(i = \pi, K)$ of each particle hypothesis is calculated, combining the dE/dx and TOF information. Here we require $Prob_K > Prob_{\pi}$.

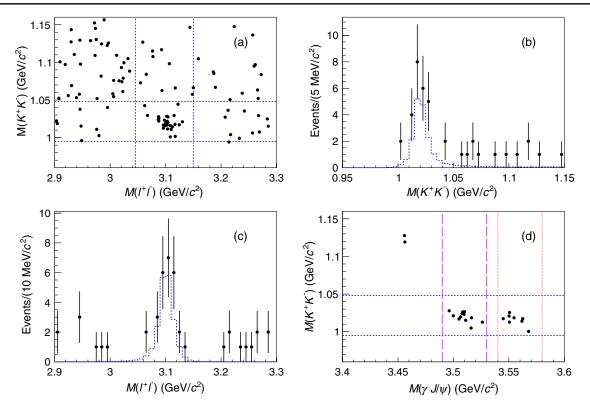


FIG. 1. (a) Distribution of $M(K^+K^-)$ versus $M(\ell^+\ell^-)$, (b) the projection along $M(K^+K^-)$ in the J/ψ mass window, (c) the projection along $M(\ell^+\ell^-)$ in the ϕ mass window, and (d) the distribution of $M(K^+K^-)$ versus $M(\gamma J/\psi)$ in the J/ψ mass window for data at $\sqrt{s}=4.600$ GeV. The blue dashed lines represent the mass windows of the ϕ and J/ψ in panels (a) and (d). The blue dashed histograms in panels (b) and (c) represent the MC simulated shapes of $M(K^+K^-)$ and $M(\ell^+\ell^-)$, respectively, which have been normalized to the measured Born cross sections. The magenta long-dashed and red dotted lines in panel (d) represent the signal regions of the χ_{c1} and χ_{c2} , respectively.

Photon candidates are reconstructed from showers in the EMC crystals. Each photon is required to have an energy deposition above 25 MeV in the barrel of the EMC ($|\cos\theta| < 0.80$) or 50 MeV in the end caps ($0.86 < |\cos\theta| < 0.92$). To exclude showers due to bremsstrahlung radiation from charged tracks, the angle between the shower position and the nearest charged tracks—extrapolated to the EMC—must be greater than 20 degrees. The timing information from the EMC is restricted to be $0 \le t \le 700$ ns to suppress electronic noise and energy deposits unrelated to the event. At least one photon candidate is required.

In order to improve the mass resolution and suppress backgrounds, a one-constraint (1C) kinematic fit is performed under the $e^+e^- \to \gamma K^\pm K^\mp_{\rm miss} \ell^+\ell^-$ hypothesis by constraining the mass of the missing track to be the kaon mass. If there are two kaons or more than one candidate photon, the combination of $\gamma K^\pm K^\mp_{\rm miss} \ell^+\ell^-$ with the least χ^2 is accepted. The χ^2 of the kinematic fit is required to be less than 20.

With all of the above selection criteria being applied, the invariant mass distribution of $M(K^+K^-)$ versus $M(\ell^+\ell^-)$ and the corresponding one-dimensional (1D) projections for data are shown in Figs. 1(a)–1(c). By default, M denotes

the invariant mass. Obvious signals can be seen in the ϕ and J/ψ mass windows, which are defined as $0.995 \le M(K^+K^-) \le 1.048 \text{ GeV}/c^2$ and $3.046 \le M(\ell^+\ell^-) \le 3.150 \text{ GeV}/c^2$, respectively. The mass windows of the ϕ and J/ψ are 4 times the full width at half maximum of the invariant mass distributions of signal events from the MC simulation. The distribution of $M(K^+K^-)$ versus $M(\gamma J/\psi)$ after the J/ψ mass window requirement is shown in Fig. 1(d). The signal regions of χ_{c1} and χ_{c2} states are set to be [3.49, 3.53] and [3.54, 3.58] GeV/ c^2 , respectively. Significant accumulations of events can be seen in the intersections of the signal regions.

The same selection criteria are applied to the inclusive MC sample to investigate possible background contributions. No events meet the requirements. Furthermore, exclusive MC samples for several processes, such as $e^+e^- \rightarrow K^+K^-J/\psi$, $\phi\pi^+\pi^-$, $K^+K^-\pi^+\pi^-$, $K^+K^-K^+K^-$, and $K^+K^-\pi^+\pi^-\pi^0$, which are potential background channels but not included in the inclusive MC samples, are generated separately. Each sample contains more than one million events (corresponding to a cross section of 2 nb at the current luminosity). The cross sections of these processes have been measured to be on the order of a few or a few tens of pb [45–48] in the energy range of interest.

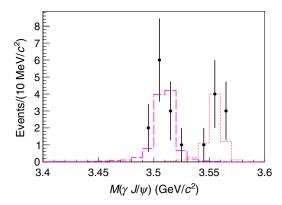


FIG. 2. Distribution of $M(\gamma J/\psi)$, after all requirements, for data at $\sqrt{s}=4.600$ GeV. The markers with error bars are for data. The magenta long-dashed and red dotted histograms are the shapes of the χ_{c1} and χ_{c2} signals from MC simulation, respectively, normalized to the measured Born cross sections.

We find that the dominant background events originate from $e^+e^- \rightarrow K^+K^-J/\psi$ in combination with a photon from initial-state radiation. Using the cross section of $e^+e^- \rightarrow K^+K^-J/\psi$ at $\sqrt{s}=4.600$ GeV measured by BESIII [45], the numbers of background events for the χ_{c1} and χ_{c2} channels normalized to the luminosity of the data sample are estimated to be 0.014 and 0.002, respectively. Simulation studies for all possible backgrounds show that less than 0.2% of the total candidate events are from background contributions.

B. Cross sections

The distribution of $M(\gamma J/\psi)$ after all event selection requirements is shown in Fig. 2. The χ_{c1} and χ_{c2} signal regions are defined as [3.49, 3.53] and [3.54, 3.58] GeV/ c^2 , respectively. Twelve and eight events, respectively, are observed by counting the number of events located in the χ_{c1} and χ_{c2} signal regions.

Assuming that the number of signal and background events both follow a Poisson distribution, the confidence interval $[\mu_a, \mu_b]$ with confidence level $\gamma = 0.6827$ should satisfy the formulas

$$\int_{\mu=0}^{\mu_a} \sum_{n=0}^{N} P(n,\mu) \cdot P((N-n),b) d\mu = \frac{1-\gamma}{2} = 0.1587,$$
(1)

$$\int_{\mu=0}^{\mu_b} \sum_{n=0}^{N} P(n,\mu) \cdot P((N-n),b) d\mu = \frac{1+\gamma}{2} = 0.8413,$$
(2)

where $P(n, \mu) = \frac{1}{n!} \mu^n e^{-\mu}$ is the probability density function of a Poisson distribution, N is the number of events observed in the signal region, n is the number of signal events, μ is the expected number of signal events, and b is the expected number of background events, which is

estimated using the dedicated background MC samples. The signal yields of the χ_{c1} and χ_{c2} channels are obtained to be $12.0^{+4.6}_{-2.6}$ and $8.0^{+4.0}_{-2.0}$, respectively. The *p*-value can be obtained by calculating the probability of the expected number of background events to fluctuate to the number of observed events or more in the signal regions assuming a Poisson distribution. The *p*-value is 1.17×10^{-31} for χ_{c1} and 6.34×10^{-27} for χ_{c2} , corresponding to statistical significances of 11.6σ and 10.6σ , respectively.

The Born cross sections are calculated according to

$$\sigma^{\rm B} = \frac{N^{\rm sig}}{\mathcal{L}_{\rm int}(\epsilon_e \mathcal{B}_e + \epsilon_\mu \mathcal{B}_\mu) \mathcal{B}_{\chi_c}(1 + \delta)(1 + \delta^{\rm vac})}, \quad (3)$$

where $N^{\rm sig}$ is the number of the signal events, $\mathcal{L}_{\rm int}$ is the integrated luminosity, ϵ_e and ϵ_μ are the selection efficiencies for the e^+e^- and $\mu^+\mu^-$ modes, respectively (and are listed in Table I), \mathcal{B}_e is the branching fraction $\mathcal{B}(J/\psi \to e^+e^-)$, \mathcal{B}_μ is the branching fraction $\mathcal{B}(J/\psi \to \mu^+\mu^-)$, \mathcal{B}_{χ_c} is the branching fraction $\mathcal{B}(\chi_{c1,2} \to \gamma J/\psi)\mathcal{B}(\phi \to K^+K^-)$, $(1+\delta)$ is the radiative correction factor, and $(1+\delta^{\rm vac})$ is the vacuum polarization factor. We assume that the cross section for $e^+e^- \to \phi \chi_{c1,2}$ follows the X(4660) line shape [10] modified by a two-body phase-space factor,

$$BW(\sqrt{s}) = \frac{\Gamma_{ee}\mathcal{B}(\phi\chi_{c1,2})\Gamma}{(s-M^2)^2 + (M\Gamma)^2} \cdot \frac{\Phi(\sqrt{s})}{\Phi(M)},\tag{4}$$

where BW is a Breit-Wigner function, the mass (M) and width (Γ) are taken from the Particle Data Group [49], Γ_{ee} is the partial width to e^+e^- , $\mathcal{B}(\phi\chi_{c1,2})$ is the branching fraction of $X(4660) \to \phi\chi_{c1,2}$, and $\Phi(\sqrt{s}) = \frac{q}{\sqrt{s}}$ is the phase-space factor for an S-wave two-body system, where q is the ϕ momentum in the e^+e^- c.m. frame (with $\hbar=c=1$). The radiative correction factor is obtained with a QED calculation [50], using the Breit-Wigner parameters of X(4660) [10] as input. The vacuum polarization factor $(1+\delta^{\rm vac})=1.055$ is taken from Ref. [51] and its uncertainty is negligible compared with other uncertainties.

The Born cross sections of $e^+e^- \to \phi \chi_{c1}$ and $\phi \chi_{c2}$ at $\sqrt{s} = 4.600$ GeV are measured to be $4.2^{+1.7}_{-1.0}$ and $6.7^{+3.4}_{-1.7}$ pb, respectively. The numbers used in the calculation and the results are listed in Table I.

TABLE I. The efficiencies (ϵ_e and ϵ_μ), the radiative correction factor $(1 + \delta)$, the number of signal events $(N^{\rm sig})$, the Born cross section $(\sigma^{\rm B})$, and the statistical significance for $e^+e^- \to \phi\chi_{c1}$ and $\phi\chi_{c2}$.

Channel	$\epsilon_e(\epsilon_\mu)(\%)$	$1 + \delta$	N ^{sig}	$\sigma^{\rm B}$ (pb)	Significance
$\phi \chi_{c1}$	28.5(38.6)	0.73	$12.0^{+4.6}_{-2.6}$	$4.2^{+1.7}_{-1.0}$	11.6σ
$\phi \chi_{c2}$	21.7(29.6)		$8.0^{+4.0}_{-2.0}$		10.6σ

IV. $e^+e^- \rightarrow \phi \chi_{c0}$ A. Event selection

1.
$$\chi_{c0} \to \pi^+\pi^-/K^+K^-$$

For the decay modes $\chi_{c0} \to \pi^+\pi^-/K^+K^-$, we require that there are three charged-particle tracks for which the selection criteria are the same as described above for the $\phi \chi_{c1}$ and $\phi \chi_{c2}$ analyses. Similarly, we require only one kaon from ϕ decays to be reconstructed and pass the PID requirement. The tracks from χ_{c0} decays can be kinematically separated from kaons from ϕ decays; hence, the two oppositely charged tracks with momenta greater than 1.0 GeV/c are assumed to be $\pi^+\pi^-$ or K^+K^- pairs from χ_{c0} decays. To separate $\chi_{c0} \to K^+K^-$ from $\chi_{c0} \to \pi^+\pi^-$, a 1C kinematic fit is performed with the $e^+e^- \rightarrow K^{\pm}K^{\mp}_{\rm miss}\pi^+\pi^-$ or $K^{\pm}K^{\mp}_{\rm miss}K^+K^-$ hypothesis by constraining the mass of the missing track to the kaon mass. If $\chi^2(\chi_{c0} \to \pi^+\pi^-) < \chi^2(\chi_{c0} \to K^+K^-)$, the event is identified as originating from $\chi_{c0} \rightarrow \pi^+\pi^-$; otherwise, it is identified as originating from $\chi_{c0} \to K^+K^-$. The χ^2 of the kinematic fit is required to be less than 20. If more than one kaon from the ϕ decay is identified, the combination with the least χ^2 is retained.

To select signal events, we define the ϕ mass window as 4 times the full width at half maximum of the distribution of

 $M(K^+K^-)$ of signal events from the MC simulation, resulting in the requirement that $1.001 \le M(K^+K^-) \le 1.038 \text{ GeV}/c^2$. Figure 3 shows the distributions of $M(K^+K^-)$ for low-momentum tracks versus $M(\pi^+\pi^-/K^+K^-)$ for high-momentum tracks from the data sample, as well as the 1D projections. No obvious χ_{c0} signals are observed. By studying the inclusive MC sample, we find that more than 90% of background events are from $e^+e^- \to \phi K^+K^-$.

2.
$$\chi_{c0} \to \pi^+ \pi^- \pi^+ \pi^-$$

For the $\chi_{c0} \to \pi^+\pi^-\pi^+\pi^-$ decay mode, the same event selection criteria for charged tracks are applied. Four pions and only one kaon are required to pass the PID requirement. The total charge of the four pions is required to be zero. In order to improve the mass resolution and suppress backgrounds, a 1C kinematic fit is performed with the $e^+e^- \to K^\pm K^\mp_{\rm miss} \pi^+\pi^-\pi^+\pi^-$ hypothesis by constraining the mass of the missing track to the kaon mass. The χ^2 of the kinematic fit is required to be less than 20. If there is more than one kaon, the combination of $K^\pm K^\mp_{\rm miss} \pi^+\pi^-\pi^+\pi^-$ with the least χ^2 is retained. The ϕ mass window is defined as above to be $0.998 \le M(K^+K^-) \le 1.043 \text{ GeV}/c^2$. Figure 4 shows the distribution of $M(K^+K^-)$ versus $M(\pi^+\pi^-\pi^+\pi^-)$ for the

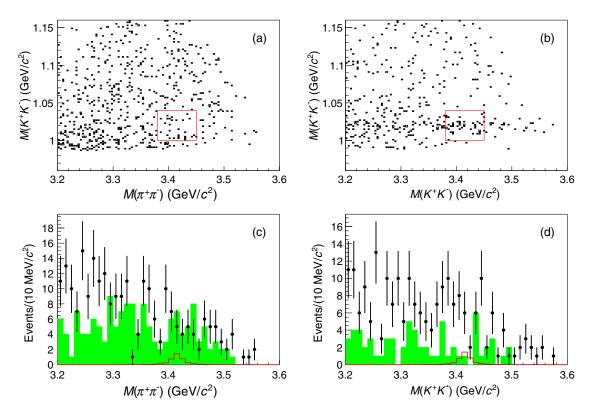


FIG. 3. (a), (b): Distributions of $M(K^+K^-)$ for low-momentum tracks versus $M(\pi^+\pi^-/K^+K^-)$ for high-momentum tracks. (c), (d): The projections along $M(\pi^+\pi^-/K^+K^-)$ in the ϕ mass window for the data sample. The red boxes represent the ϕ and χ_{c0} signal regions. The dots with error bars are the data. Histograms filled with green represent the ϕ sidebands, which have been normalized to the signal region of the ϕ . The red histograms represent the χ_{c0} MC shape, normalized to the upper limit of the measured cross section.

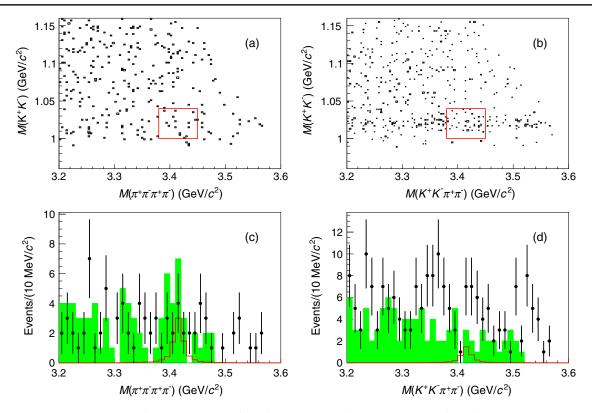


FIG. 4. Distributions of (a) $M(K^+K^-)$ versus $M(\pi^+\pi^-\pi^+\pi^-)$, (b) $M(K^+K^-)$ versus $M(K^+K^-\pi^+\pi^-)$, (c) the projection along $M(\pi^+\pi^-\pi^+\pi^-)$ in the ϕ mass window, and (d) the projection along $M(K^+K^-\pi^+\pi^-)$ in the ϕ mass window for data. The red boxes represent the ϕ and χ_{c0} signal regions. The dots with error bars are the data. The histograms filled with green represent the ϕ sidebands, normalized to the signal region of the ϕ . The red histograms represent the χ_{c0} MC shape, normalized to the upper limit of the measured cross section.

data sample and the 1D projections. Again, there are no obvious χ_{c0} signals.

3.
$$\chi_{c0} \rightarrow K^+K^-\pi^+\pi^-$$

For the $\chi_{c0} \to K^+ K^- \pi^+ \pi^-$ decay mode, we use the same criteria to select candidate charged tracks. Two oppositely charged pions and three kaons are required to pass the PID requirement. The absolute value of the net charge of all kaons should not be greater than one. A 1C kinematic fit is performed with the $e^+e^- \to K^\pm K^\mp_{\rm miss} K^+ K^- \pi^+ \pi^-$ hypothesis by constraining the mass of the missing track to the kaon mass and the χ^2 of the kinematic fit is required to be less than 20. If there are more than three kaons, the combination of $K^{\pm}K_{\rm miss}^{\mp}K^{+}K^{-}\pi^{+}\pi^{-}$ with the least χ^{2} is retained. Since the origin of the kaons from ϕ or χ_{c0} decays cannot be determined, all combinations of K^+K^- are considered. The ϕ mass window is defined as above to be $0.998 \le M(K^+K^-) \le$ 1.044 GeV/ c^2 . The distribution of $M(K^+K^-)$ versus $M(K^+K^-\pi^+\pi^-)$ and the 1D projections from the data sample are also shown in Fig. 4. No obvious χ_{c0} signals are observed.

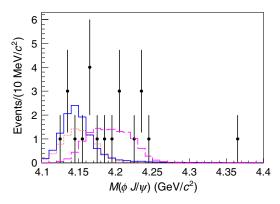
B. Cross section

A simultaneous unbinned maximum likelihood fit is performed on the distributions of $M(\pi^+\pi^-)$, $M(K^+K^-)$,

 $M(\pi^+\pi^-\pi^+\pi^-)$, and $M(K^+K^-\pi^+\pi^-)$. The signal shape is determined from the signal MC sample, and the background shape of each decay mode is described with a second-order Chebyshev polynomial function. The number of signal events for each decay mode depends on its branching fraction and efficiency. The efficiencies for $\chi_{c0} \to \pi^+ \pi^-, K^+ K^-, \pi^+ \pi^- \pi^+ \pi^-, \text{ and } K^+ K^- \pi^+ \pi^- \text{ are}$ 62.2, 58.6, 29.3, and 19.7%, respectively. The branching fractions are obtained from the Particle Data Group [49]. Since no significant $\phi \chi_{c0}$ signal is observed, the upper limit on the Born cross section is set at the 90% confidence level (C.L.). A scan of the likelihood with respect to the number of produced $\phi \chi_{c0}$ events is obtained, and the upper limit on n^{prod} at the 90% C.L. is determined according to $\int_0^{n^{\text{prod}}} L(x) dx / \int_0^{\infty} L(x) dx = 0.9$. Since the branching fractions and efficiencies of the four decay modes have been considered in the fit, the upper limit on the Born cross section is calculated with

$$\sigma^{\rm B} = \frac{n^{\rm prod}}{\mathcal{L}_{\rm int}(1+\delta)(1+\delta^{\rm vac})},\tag{5}$$

where $(1 + \delta) = 0.74$ [50] and $(1 + \delta^{\text{vac}}) = 1.055$ [51] were obtained with the same method as for $e^+e^- \rightarrow \phi \chi_{c1,2}$. The upper limit on σ^{B} is obtained by replacing n^{prod} with



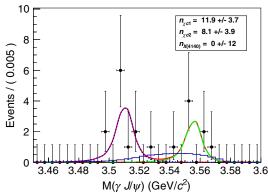


FIG. 5. Left: Distribution of $M(\phi J/\psi)$ in the ϕ and J/ψ mass windows for data. The dots with error bars are the data and the blue solid histogram represents the MC shape from $M(\gamma X(4140))$, normalized to the upper limit of the Born cross section. The magenta long-dashed and red dotted histograms represent the MC shapes from $M(\phi \chi_{c1})$ and $M(\phi \chi_{c2})$, respectively, normalized to the measured Born cross sections. Right: Fit to the distribution of $M(\gamma J/\psi)$. The dots with error bars are data. The red solid line is the fit curve. The blue dashed and green long-dashed lines represent χ_{c1} and χ_{c2} backgrounds, respectively. The red dash-dotted line represents X(4140) signal. The blue histogram represents the X(4140) signal shape from MC simulation with arbitrary normalization.

the upper limit on n^{prod} . To take the systematic uncertainty into account, the likelihood distribution is convolved with a Gaussian function with a mean value of 0 and a standard deviation of $n^{\text{prod}} \cdot \Delta$, where n^{prod} is the number of produced $e^+e^- \to \phi \chi_{c0}$ events and Δ is the relative systematic uncertainty described in the next section. The upper limit on the production of $e^+e^- \to \phi \chi_{c0}$ at 90% C.L. is estimated to be 5.4 pb.

V. $e^+e^- \to \gamma X(4140)$

For $e^+e^- \rightarrow \gamma X(4140)$, we search for X(4140) meson decays to $\phi J/\psi$, with J/ψ decaying to $\ell^+\ell^-$, and ϕ decaying to K^+K^- . Since the final state of $e^+e^- \rightarrow$ $\gamma X(4140)$ is the same as that for $e^+e^- \rightarrow \phi \chi_{c1,2}$, we apply the same event selection criteria and requirements. The resulting distributions $M(\phi J/\psi)$ and $M(\gamma J/\psi)$ in the ϕ and J/ψ mass windows are shown in Fig. 5. An unbinned maximum likelihood fit is performed on the distribution of $M(\gamma J/\psi)$. The signal shape is determined from the signal MC sample and the background shapes are described with those from MC simulations for $e^+e^- \rightarrow \phi \chi_{c1}$ and $\phi \chi_{c2}$. Since there is no obvious X(4140) signal, the upper limit on the Born cross section at 90% C.L. is determined. The upper limit on the number of signal events is obtained with the same method as for $e^+e^- \rightarrow \phi \chi_{c0}$. The upper limit on the Born cross section is calculated using Eq. (3), where $(1 + \delta) = 0.75$ [50] and $(1 + \delta^{\text{vac}}) = 1.055$ [51] were obtained with the method described above. The upper limit on the production of the Born cross section and branching fraction $\sigma[e^+e^- \to \gamma X(4140)] \cdot \mathcal{B}(X(4140) \to \phi J/\psi)$ at 90% C.L. is estimated to be 1.2 pb. The distribution of $M(\phi J/\psi)$ is also fitted, but a higher upper limit is obtained. Toy MC samples with the two methods are generated and studied, and we obtain a better sensitivity when applying the fit to $M(\gamma J/\psi)$.

VI. SYSTEMATIC UNCERTAINTY

The systematic uncertainties on the cross section measurements for $e^+e^- \to \phi \chi_{c0,1,2}$ and $e^+e^- \to \gamma X(4140)$ come mainly from the integrated luminosity, the tracking and photon reconstruction, the PID, the kinematic fit, the signal and background shapes, the fit range, the branching fraction, and the radiative correction. The systematic uncertainties are summarized in Table II and explained below.

The systematic uncertainty due to the detection efficiency includes uncertainties from track reconstruction, PID efficiency, photon reconstruction, the kinematic fit, angular distributions, and the radiative correction. The uncertainty from track reconstruction for each charged track is taken as 1.0% [52]. In the process $e^+e^- \rightarrow \phi \chi_{c0}$, the total systematic uncertainty from tracking

TABLE II. The relative systematic uncertainties of Born cross sections (%) for $e^+e^- \to \phi \chi_{c0,1,2}$ and $e^+e^- \to \gamma X(4140)$ at $\sqrt{s}=4.600$ GeV. An ellipsis (\cdots) means that the uncertainty is negligible.

Source	$\phi \chi_{c0}$	$\phi \chi_{c1}$	$\phi \chi_{c2}$	$\gamma X(4140)$
Luminosity	1.0	1.0	1.0	1.0
Tracking	4.2	3.0	3.0	3.0
Photon		1.0	1.0	1.0
PID	3.4	1.0	1.0	1.0
Kinematic fit	1.6	1.5	1.0	2.4
Branching fraction	5.7	3.8	3.9	1.2
Radiative correction	5.2	2.1	2.2	7.3
Angular distribution	3.7	4.5	4.3	13.8
Signal shape	3.4			11.0
Background shape	5.2			
Fitting range	1.0			1.7
Sum	12.1	7.3	7.2	19.7

reconstruction is obtained by taking into account the weights of the efficiencies and branching fractions of the four χ_{c0} decay modes. The total systematic uncertainty due to PID efficiency is obtained with the same method, where the PID uncertainty for each charged track is taken as 1.0% [52]. The systematic uncertainty from photon reconstruction is determined to be 1.0% for each photon by studying the control sample of $J/\psi \to \rho^0 \pi^0$ decays [53].

Since it is difficult to find an appropriate control sample to estimate the systematic uncertainty related to the kinematic fit and the vertex fit, we correct the charged-track helix parameters of the MC simulated events [54] to obtain a better match with the data sample. The difference between the efficiency with and without the correction is taken as the uncertainty associated with the kinematic fit. The MC sample with the track helix parameter correction applied is used in the nominal analysis.

In order to estimate the uncertainty from the angular distributions of the ϕ meson and the radiative photon, we change the decay dynamics from phase space to $1+\cos^2\theta$ or $1-\cos^2\theta$ to generate new signal MC samples. For $e^+e^-\to \gamma X(4140)$, θ is the polar angle of the radiative photon in the e^+e^- rest frame with the z axis pointing in the direction of the electron beam, while for $e^+e^-\to\phi\chi_{c0,1,2}$, θ is the polar angle of the ϕ meson. The maximum difference in efficiency is taken as the systematic uncertainty.

The line shape used in the MC simulation will affect both the radiative correction factor and the efficiency. In the nominal MC simulation, we assume that the processes $e^+e^- \to \phi \chi_{c0,1,2}$ and $e^+e^- \to \gamma X(4140)$ follow the line shape of the X(4660) [10] modified by a phase-space factor. We change the line shape to $\frac{4\pi\alpha^2}{3s}\Phi(\sqrt{s})$ and the resultant difference of $(1+\delta)\cdot \epsilon$ is taken as the systematic uncertainty due to the radiative correction factor.

The luminosity is measured using large-angle Bhabha events with an uncertainty of less than 1.0% [36]. The branching fractions for $\phi \to K^+K^-$, $\chi_{c1,2} \to \gamma J/\psi$, $J/\psi \to \ell^+\ell^-$ and $\chi_{c0} \to \pi^+\pi^-$, K^+K^- , $\pi^+\pi^-\pi^+\pi^-$, $K^+K^-\pi^+\pi^-$ are taken from the Particle Data Group [49]. The uncertainties of the branching fractions are taken as the associated systematic uncertainties. For the ϕ and J/ψ mass windows, very loose criteria are used; hence, the difference in efficiency between MC simulation and data sample is negligible.

The signal yields $e^+e^- \to \phi \chi_{c0}$ and $e^+e^- \to \gamma X(4140)$ are determined from the fit, and the signal yields of $e^+e^- \to \phi \chi_{c1,2}$ is obtained by simply counting events. Only the systematic uncertainty associated with the fit is considered. The systematic uncertainty on the fit procedure comprises those due to the signal shape, background shape, and fit range. For $e^+e^- \to \phi \chi_{c0}$, we generate alternative signal MC samples by varying the mass and width of the χ_{c0} by one standard deviation and take the maximum difference with respect to the nominal values as the systematic uncertainty due to the signal shape. The systematic

uncertainty caused by the background shape is obtained by changing the background shape from a second-order polynomial function to a third-order polynomial function. The nominal fit range is taken to be [3.18, 3.58] GeV/c^2 . We vary the limit of the fit range by ± 0.05 GeV/c^2 and take the difference as the associated systematic uncertainty. For $e^+e^- \to \gamma X(4140)$, we generate a signal MC sample by varying the mass and width of the X(4140) with one standard deviation and take the maximum difference as the systematic uncertainty due to the signal shape. The nominal fit range is taken to be [3.45, 3.60] GeV/c^2 . We vary the limit of the fit range by ± 0.01 GeV/c^2 and take the resultant difference as the associated systematic uncertainty.

The total systematic uncertainties are obtained by adding the individual uncertainties in quadrature, assuming that all sources are independent. For $e^+e^- \rightarrow \phi \chi_{c0,1,2}$ and $e^+e^- \rightarrow \gamma X(4140)$, the total systematic uncertainties are 12.1, 7.3, 7.2, and 19.7%, respectively.

VII. RESULTS AND DISCUSSION

In summary, the processes $e^+e^- \to \phi \chi_{c1}$ and $\phi \chi_{c2}$ were observed for the first time at a c.m. energy of $\sqrt{s}=4.600$ GeV by using a data sample corresponding to an integrated luminosity of 567 pb⁻¹ collected with the BESIII detector. The corresponding Born cross sections were measured to be $(4.2^{+1.7}_{-1.0} \pm 0.3)$ and $(6.7^{+3.4}_{-1.7} \pm 0.5)$ pb, respectively. No obvious signals were observed for $e^+e^- \to \phi \chi_{c0}$ and $e^+e^- \to \gamma X(4140)$ and the upper limits on the Born cross sections at 90% C.L. were set to be 5.4 and 1.2 pb, respectively.

Since only one data set at or near $\sqrt{s}=4.600~{\rm GeV}$ is available to study these modes at BESIII, it is not possible to measure the line shape for their production. The cross sections of other decay modes at this energy point—such as $e^+e^- \to \pi^+\pi^- J/\psi$ and $e^+e^- \to \omega\chi_{c0,1,2}$ —are all at the level of a few pb. As $e^+e^- \to \phi\chi_{c1,2}$ signals have been observed, it will be interesting to measure the line shape between the threshold to 4.600 GeV or even higher.

The upper limit of the Born cross section for $e^+e^- \rightarrow \gamma X(4140)$ at 4.600 GeV is higher than those measured at 4.230, 4.260, and 4.360 GeV, due to the nontrivial backgrounds from $\chi_{c1,2}$. Measurements based on data samples with larger statistics at more energy points will be helpful to clarify the nature of these decay processes in this energy region.

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