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Title: Lower mantle hydrogen partitioning between periclase and perovskite: a quantum chemical modeling.

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Corresponding Author: Prof. Alessandro Pavese,

Corresponding Author's Institution: University of Milan, Italy

First Author: Marcello Merli, Prof

Order of Authors: Marcello Merli, Prof; Costanza Bonadiman, Prof; Valeria Diella; Alessandro Pavese

Abstract: The partitioning of hydrogen (often addressed to as H<sub>2</sub>O) between periclase (pe) and perovskite (pvk) at lower mantle conditions (24-80 GPa) has been investigated, using quantum mechanics, equilibrium reaction thermodynamics and following two H-incorporation models. One is based on the replacements (MSWV) given by Mg<sup>2+</sup> ↔ 2H<sup>+</sup> and Si<sup>4+</sup> ↔ 4H<sup>+</sup>; the other relies upon substitutions (MSWA) in terms of 2Mg<sup>2+</sup> ↔ Al<sup>3+</sup>+H<sup>+</sup> and Si<sup>4+</sup> ↔ Al<sup>3+</sup>+H<sup>+</sup>. H<sub>2</sub>O partitioning between the two mentioned phases is considered in the light of homogeneous (Bulk Silicate Earth, BSE; pvk: 75% - pe:16% modal contents) and heterogeneous (Layered Mantle, LM; pvk:78% - pe:14% modal contents) mantle geochemical models, which are set up to bear lower and upper bulk H<sub>2</sub>O contents (BWC) of 800 and 1500 ppm, respectively. The equilibrium constant,  $[BWC]_{K(P,T)}^{[D,H_2O]^{[pe/pvk]}}$ , of the reactions governing the H-exchange between pe and pvk exhibits an almost negligible dependence on P, whereas it is remarkably sensitive to T, BWC and hydrogen incorporation scheme. Both MSWV and MSWA lead to  $[BWC]_{K(P,T)}^{[D,H_2O]^{[pe/pvk]}} \leq 1$ , which suggests an ubiquitous shift of the exchange reaction towards a H<sub>2</sub>O-hosting perovskite. This takes place more markedly in the latter model, thus showing that the H<sub>2</sub>O-partitioning is affected by the mechanism of uptake. In general, the larger BWC, the smaller is  $[BWC]_{K(P,T)}^{[D,H_2O]^{[pe/pvk]}}$ . Over the BWC range of 800-1500 ppm, MSWV leads to a  $\langle [BWC]_{K}^{[D,H_2O]^{[pe/pvk]}} \rangle$  (average of  $[BWC]_{K(P,T)}^{[D,H_2O]^{[pe/pvk]}}$  calculated along the lower mantle related P-T-paths predicted by the lower mantle geochemical models) that may be ultimately considered as a constant value (0.875). In the case of the MSWA mechanism,  $\langle [BWC]_{K}^{[D,H_2O]^{[pe/pvk]}} \rangle$  is more sensitive to BWC (and LM over BSE), but its values lie in the rather narrow range 0.610- 0.780. The concentration ratios (formally named "partition coefficient": CH<sub>2</sub>O<sub>pe</sub>/CH<sub>2</sub>O<sub>pvk</sub>) inferred from  $\langle [BWC]_{K}^{[D,H_2O]^{[pe/pvk]}} \rangle$  range, for MSWV, between 0.60 and 0.49 (BWC spanning from 500 to 3000 ppm). In this view, the MSWV partition coefficient is estimated to be 0.56. MSWA, in turn, yields a  $C_{[H_2O]^{[pe]}}/C_{[H_2O]^{[pvk]}}$ -trend having a slightly steeper negative slope ( $C_{[H_2O]^{[pe]}}/C_{[H_2O]^{[pvk]}}$  ratio: 0.6-0.3; BWC 500-3000 ppm), but over the interval 800-1500 ppm it may also be considered nearly invariant and as large as 0.47 (average over an interval between 0.43 and 0.51). Combining the results from MSWV and MSWA we propose that, in the P-T-BWC range of geochemical interest, the H<sub>2</sub>O pe/pvk "partition coefficient" lies in the short interval 0.47-0.56. This implies that water always prefers pvk than pe, but also suggests that even in a lower mantle with low or very low bulk water content, periclase hardly becomes a pure anhydrous phase.

Suggested Reviewers: Donato Belmonte Doc  
researcher, Dipartimento di Scienze della terra, dell'ambiente e della vita, university of Genova, Italy

Donato.Belmonte@unige.it  
modeling expert

William McDonough Prof  
University of Maryland  
mcdonoug@geol.umd.edu  
geochemistry expert

William Griffin Prof  
Macquarie University, Sidney  
bill.griffin@mq.edu.au  
geochemistry expert

David Price Prof  
UCL; London's global university  
d.price@ucl.ac.uk  
modeling expert

Bernard Marty Prof  
Centre de Recherches Pétrographiques et Géochimiques (CRPG), Vandœuvre les Nancy  
bmarty@crpg.cnrs-nancy.fr  
geochemistry expert

Dear Editor,

please, find enclosed the manuscript “**Lower mantle hydrogen partitioning between periclase and perovskite: a quantum chemical modeling**” by Macello Merli, Costanza Bonadiman, Valeria Diella and Alessandro Pavese for potential publication in *Geochimica et Cosmochimica Acta*.

The aim of the present work is to explore the partitioning of hydrogen (often addressed to as H<sub>2</sub>O) between periclase and perovskite at lower mantle conditions (24-80 GPa), using quantum mechanics, equilibrium reaction thermodynamics and following two H-incorporation models. Subsequently we exploited the theoretical results to predict in the light of lower mantle geochemical models the hydration/dehydration trends and eventually the H<sub>2</sub>O-distribution between *pe* and *pvk*.

We believe this work may be of interest to the readership of *Geochimica et Cosmochimica Acta*. This manuscript is an original work and has not been published, neither is it under consideration for publication elsewhere.

Thank you very much for your consideration and handling.

Milan 12/03/2015

Alessandro Pavese



## 34 Abstract

35 The partitioning of hydrogen (often addressed to as H<sub>2</sub>O) between periclase (*pe*) and perovskite  
36 (*pvk*) at lower mantle conditions (24-80 GPa) has been investigated, using quantum mechanics,  
37 equilibrium reaction thermodynamics and following two H-incorporation models. One is based on  
38 the replacements (MSWV) given by  $\text{Mg}^{2+} \leftrightarrow 2\text{H}^+$  and  $\text{Si}^{4+} \leftrightarrow 4\text{H}^+$ ; the other relies upon substitutions  
39 (MSWA) in terms of  $2\text{Mg}^{2+} \leftrightarrow \text{Al}^{3+} + \text{H}^+$  and  $\text{Si}^{4+} \leftrightarrow \text{Al}^{3+} + \text{H}^+$ . H<sub>2</sub>O partitioning between the two  
40 mentioned phases is considered in the light of homogeneous (Bulk Silicate Earth, BSE; *pvk*: 75% -  
41 *pe*:16% modal contents) and heterogeneous (Layered Mantle, LM; *pvk*:78% - *pe*:14% modal  
42 contents) mantle geochemical models, which are set up to bear lower and upper bulk H<sub>2</sub>O contents  
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50 leads to a  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  (average of  ${}_{BWC}K(P,T)_{D,H_2O}{}^{pe/pvk}$  calculated along the lower mantle  
51 related *P-T*-paths predicted by the lower mantle geochemical models) that may be ultimately  
52 considered as a constant value (0.875). In the case of the MSWA mechanism,  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  is  
53 more sensitive to *BWC* (and LM over BSE), but its values lie in the rather narrow range 0.610-  
54 0.780. The concentration ratios (formally named “partition coefficient”:  $C_{\text{H}_2\text{O}}{}^{pe}/C_{\text{H}_2\text{O}}{}^{pvk}$ ) inferred  
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58 500-3000 ppm), but over the interval 800-1500 ppm it may also be considered nearly invariant and  
59 as large as 0.47 (average over an interval between 0.43 and 0.51). Combining the results from  
60 MSWV and MSWA we propose that, in the *P-T-BWC* range of geochemical interest, the H<sub>2</sub>O  ${}^{pe/pvk}$   
61 “partition coefficient” lies in the short interval 0.47-0.56. This implies that water always prefers *pvk*  
62 than *pe*, but also suggests that even in a lower mantle with low or very low bulk water content,  
63 periclase hardly becomes a pure anhydrous phase.

## 1. INTRODUCTION

The mechanisms of hydrogen incorporation in nominally anhydrous minerals (NAM) govern the exchange of “water” (here we freely use such term, along with H<sub>2</sub>O, to refer to the H-content of a mineral, expressed by oxides) between interior and surface of the Earth, as well as the degree of retention and possible abundance of hydrogen deep into our planet (Smyth, 2006; Johnson, 2006; Hirschmann 2006; Hirschmann and Kohlstedt 2012).

The exact water “budget” of the Earth’s interior is currently unknown, but the availability constrains of the Earth geochemical models (McDonough and Sun, 1995; Wood and Corgne, 2007) suggest it to be comparable to the surface reservoirs’. Earth’s core may contain water, after hints of metal-silicate partitioning experiments (Li and Agee, 1996; Abe et al., 2000; Saxena et al., 2004), although the volatile species geochemical model (Marty, 2012) does not support that H<sub>2</sub>O could be stored there during the accretion and terrestrial differentiation processes.

Water mass estimates in the main mineral phases of our planet’s interiors (i.e: Othani, 2005 and Murakami et al., 2002; Inoue et al., 2010), in combination with geochemical bulk models (i.e: McDonough and Sun, 1995; Lyubetskaya and Korenaga, 2007; Javoy et al., 2010), lead to that the Earth’s mantle may host from about 0.5 to over 5 oceans at present-day (Huang et al. 2005; Smyth and Jacobsen 2006; Khan and Shankland , 2012; Marty, 2012).

The bulk silicate Earth chemical models yield that over 50% by weight of oxides are provided by MgO and FeO (e.g.: McDonough and Sun, 1995; Palme and O’Neill, 2003; Lyubetskaya and Korenaga, 2007; Javoy et al., 2010), with olivine (and its high-pressure  $\beta$ - and  $\gamma$ -polymorphs) as the dominant mineral of the upper mantle. Olivine, as most NAMs, incorporates hydrogen *via* intrinsic point defects of its structure (Ingrin and Skogby, 2000; Bolfan-Casanova, 2005; Hauri et al., 2006). This way, it accounts for an amount of water, in the upper 410 km of the mantle, nearly equivalent to the entire volume of the oceans (Hirschmann et al., 2005, 2009; Khan and Shankland, 2012).

The amount of water that NAMs can incorporate in the Transition Zone (410-660 km depth) is larger by as much as an order of magnitude (Bolfan-Casanova, 2005, Khan and Shankland, 2012) than that stored in the upper mantle ( Hirschmann et al., 2005; Bonadiman et al., 2009; Inoue et al., 2010). Nominally anhydrous wadsleyite and ringwoodite in the lower part of the transition zone can accommodate up to 3.3 wt% water (Smyth, 1994; Bolfan-Casanova et al., 2000, Kleppe, 2006, Griffin et al., 2013). Over the volume of the Earth’s transition zone, such phases represent a potential hydrogen reservoir that might store up to approximately four times the water present in the oceans and atmosphere (Hirschmann et al., 2006; Dai and Karato, 2009; Griffin et al., 2013).

In the lower mantle, the precise amount of stored water, its location and the mechanisms of exchange with the upper mantle are still a matter of debate (e.g. Hirschmann et al., 2005; Bolfan-Casanova et al., 2006; Panero et al., 2015). In such a region, Fe-periclase (~15% by volume) with a

100 composition of  $\text{Mg}_{1-x}\text{Fe}_x\text{O}$ ,  $0.1 < x < 0.2$  (Ito and Takahashi, 1989; Ringwood, 1991; Guyot et al.,  
101 1988; Fiquet et al. 1998) and silicate Mg-perovskite (~80% by volume) are the principal mineral  
102 phases. Experimental studies (Bolfan-Casanova et al., 2000; Murakami et al., 2002; Litasov and  
103 Othani, 2007, Joachim et al., 2013) suggest that at 23-25 GPa and 1400-2000 °C the partitioning  
104 coefficient for hydrogen between (Mg,Fe)O and (Mg,Fe)(Si,Al)O<sub>3</sub> is  $\geq 1$ , with H<sub>2</sub>O-contents in  
105 periclase ranging from 40-60 to 2000 ppm (Bolfan-Casanova et al., 2000; Murakami et al., 2002).  
106 However, Hernández et al. (2013) predict that in a Fe-free ambient water prefers to enter perovskite  
107 with respect to periclase, at 24 GPa and 1500 K. This all points to that, although extensive  
108 investigations (Mosenfelder et al., 2013; Jahn et al., 2013; Ghosh et al., 2013) have been devoted to  
109 hydrogen incorporation, yet much remains uncertain about the microscopic mechanisms underlying  
110 such reactions, in part because remarkable experimental difficulties make it complex to elucidate  
111 how the H<sub>2</sub>O-partitioning takes place (Wood and Corgne, 2007). In literature, one finds out several  
112 models to account for the uptake of hydrogen in high-pressure mineral phases (Keppler and Bolfan-  
113 Casanova, 2006): cation-vacancy occurrence and introduction of H for compensation (hydro-garnet-  
114 like substitution); double replacement, such as  $2\text{Mg}/1\text{Si} \leftrightarrow \text{Al}(\text{Fe}^{3+})+\text{H}$ ; reduction of iron to Fe-  
115 metallic (Litasov, 2010).

116 Although comparatively little is known about water solubility in periclase and perovskite at  
117 lower mantle pressure, the pure H<sub>2</sub>O-MgO-SiO<sub>2</sub> system is probably a weak acceptor and most of the  
118 H-incorporation is related to double-replacement mechanisms involving mainly aluminum and iron  
119 (Litasov, 2010; Litasov and Othani, 2007; Bolfan-Casanova et al., 2006; Panero and Stixrude,  
120 2004). As to Fe<sup>3+</sup> in periclase, Demouchy et al. (2007) and Mackwell et al. (2005) discuss the role  
121 of ferric iron in combination with vacancy occurrence (at hydrous-ambient-pressure conditions),  
122 whereas Bolfan-Casanova et al. (2006) observe Fe anti-correlates with hydroxyl formation, at high  
123 pressure. In particular, Fe-periclase and perovskite can host hetero-valent cations through coupled  
124 substitutions as well as creation of point defects (Van Orman et al., 2009) over a wide *P-T* range.  
125 Fe<sup>3+</sup> dwelling in (Mg,Fe)O (*i.e.* McCommon et al., 2004; Lin and Wheat, 2012; Otsuka et al., 2010)  
126 shows a pressure/oxygen fugacity dependence, so that in the lower mantle a change of the crystal-  
127 chemical behavior of ferric iron is expected (Otsuka et al., 2010). On the basis of experimental and  
128 theoretical data, it is plausible to assume that (Mg,Fe)O in the shallow part of the lower mantle ( $P \approx$   
129 25-28 GPa) hosts Fe<sup>3+</sup> in the octahedral sites, in combination with cation vacancies or occurrence of  
130 a monovalent cation (Na<sup>+</sup>) to fulfill the charge balance (Mc Cammon et al., 2004). The solubility  
131 competition between monovalent cation (Na<sup>+</sup>) and the protons (H<sup>+</sup>) might play a role in affecting  
132 the tendency of H to site in periclase or pervoskite, and all this would ultimately affect the global  
133 evaluation of water content and transport properties, in the lower mantle.

134 In a simplistic “big picture”, the partition coefficients of moderately- and highly-siderophile  
135 elements between core-forming liquids and silicate melts determined at ambient pressure suggest

136 that such species should have entered almost entirely the Earth's core (McDonough and Arevalo,  
137 2008). Seismological heterogeneities at the core-mantle boundary (*i.e.* 2300-2800 Km depth) reveal  
138 (Hilst et al., 1997; Lay et al. 1998; Nomura et al., 2014; Garnero et al. 2004) a distinct layer  
139 characterized by anomalous seismic velocities (Wysession et al., 1998), which have been  
140 interpreted by Kellogg et al. (1999) as due to a compositionally different and denser shell (D").  
141 D" contains super-adiabatic thermal gradients in excess of 1000 K (Montelli et al., 2004; Wolfe et  
142 al., 2009) and is the region wherein mantle upwelling processes are supposed to have their rise.  
143 Changes in iron chemistry and Mg/Fe ratio due to phase transitions (Kellogg et al., 1999; Mao et  
144 al., 2006) could be responsible for such deep mantle layering. However, a potential segregation of  
145 even a small amount of water in this region, or in the Earth's core, could modify both melting  
146 relationships (e.g.: Inoue, 1994; Lay et al., 2004; Saxena et al.; 2004) and rheological properties  
147 (e.g.: Karato and Jung, 2003; Mei and Kohlstedt, 2000) drastically. The distribution of water has  
148 therefore an important influence on the dynamics and evolution, too, of terrestrial planets.

149 In this view, quantum mechanical modeling and computing techniques turn out to provide a  
150 valuable way to complement experimental issues, substantiating hypotheses or contributing to  
151 develop new ones. The aim of the present work is twofold: (1) using quantum mechanics [HF/DFT-  
152 LCAO calculations; CRYSTAL09-program (Dovesi et al., 2009)] we model the equilibrium  
153 constant,  $K(P,T)_D$ , for reactions involving an exchange of water between periclase (*pe*) and  
154 perovskite (*pvk*) at lower mantle regime, adopting two H-incorporation schemes; (2) we exploit the  
155 theoretical results to predict, in the light of lower mantle geochemical models, the  
156 hydration/dehydration trends and eventually the H<sub>2</sub>O-distribution between *pe* and *pvk*.

## 158 2. GEOCHEMICAL CONSTRAINTS

159  
160 H<sub>2</sub>O partitioning between lower mantle phases depends on the potentially available water  
161 "budget" and, as a consequence, the Bulk Earth's geochemical model that accounts for the mantle  
162 chemical composition. We consider here two distinct lower mantle geochemical models:

163 1) homogeneous mantle model (BSE=Bulk Silicate Earth), which is inferred from the Primitive  
164 Upper Mantle (PUM) composition according to terrestrial data (pyrolite) and chondritic constraints  
165 (e.g.: Zindler and Hart, 1986; McDonough and Sun, 1995; Lyubetskaya and Korenaga, 2007; Javoy  
166 et al., 2010), and it is extended to the whole silicate Earth;

167 2) heterogeneous mantle model (LM=layered mantle), which is based on geophysical data and  
168 cosmochemical constraints; it advocates a lower mantle chemically distinct from the upper mantle  
169 (e.g.: Stixrude and Bukowinski, 1992; Anderson, 1989; Cammarano and Romanowicz, 2007; Matas  
170 et al., 2007; Javoy et al., 2010). In particular, the lower mantle of LM bears a larger Si content  
171 ( $Mg/Si_{PUM} = 1.21-1.31$ ;  $Mg/Si_{LM} = 1.18$ ) than PUMS's in order to match the cosmochemical major



172 elements' contents of the bulk mantle (Matas et al., 2007).

173 The mineral phase compositions of the lower mantle, which are constrained by the geochemical  
174 model chosen, stem from mass balance calculations, aimed to give the best fit between supposed  
175 mineral phases and overall rock composition (Table 1).  $\text{CaSiO}_3$ -perovskite occurs along with  
176  $(\text{Mg,Fe})\text{SiO}_3$ -perovskite and  $(\text{Mg,Fe})\text{O}$ -periclase. Although  $\text{Al}_2\text{O}_3$  oxide accounts for about 3.5–4.5  
177 wt% of the lower mantle, the aluminum host-phase is still uncertain. Al may reside in  $(\text{Mg,Fe})\text{O-pe}$ ,  
178  $(\text{Mg,Fe})\text{SiO}_3\text{-pvk}$  (Irifune 1994; Irifune et al. 1996), or form a separate Al-rich phase (Kesson et al.,  
179 1995; Oganov and Brodholt, 2000; Pamato et al., 2015). In Table 1, for the sake of simplicity, we  
180 assume  $\text{Al}_2\text{O}_3$  as a “nondescript” HP-phase. Preliminary tests of mass balance have suggested us to  
181 exclude  $\text{SiO}_2$ -stishovite. The lower mantle  $\text{H}_2\text{O}$  content is here estimated by subtracting from the  
182 whole mantle (BM=bulk mantle) the contributions of the upper mantle and transition zone,  
183 normalized to their respective fractional masses (Table 2). Note that BM shares with BSE the  $\text{H}_2\text{O}$   
184 content, excluding the surface water reservoirs (atmosphere, oceans and sedimentary rocks) and  
185 adopting a normalization to the total mass of the Earth, as proposed by Marty (2012).

186  $\text{H}_2\text{O}$  global estimates converge to  $250\pm 50$  ppm for the upper mantle (Dixon et al., 2002;  
187 Michael, 1988; Saal et al., 2002; Salters and Stracke, 2004) and  $1.00\pm 0.3$  wt% for transition zone  
188 (Othani, 2005; Pearson et al., 2014). Using the conservative estimate of  $\text{H}_2\text{O}$  according to BSE, i.e.  
189 1100- 3000 ppm (Palme and O'Neill, 2003; Othani, 2005; Marty, 2012), and combining it with the  
190 mantle mass fractions, we infer the lower mantle's Bulk Water Contents (hereafter *BWC*) to range  
191 between a figure smaller than 1000 and 2000 ppm (Table 2), in agreement with earlier issues  
192 (Hernandez et al., 2013; Othani, 2005; Murakami et al., 2002). In this view, we have chosen to use  
193 800 and 1500 ppm as reference average values for lower and upper estimates, respectively, of *BWC*,  
194 whose precise values depend on the geochemical model and will be considered below, in the  
195 Discussion, section 8.

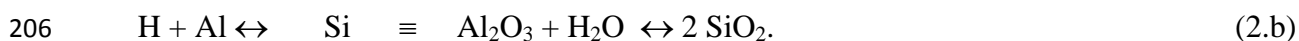
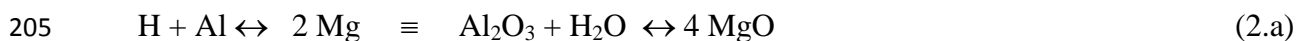
### 196 197 3. H-INCORPORATION MODELING

198  
199 Two mechanisms are here considered to account for H-incorporation in *pe* and *pvk*, at lower  
200 mantle conditions:

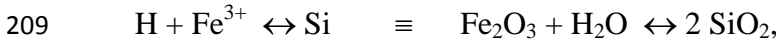
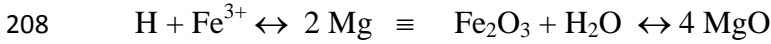
201 MSWV-scheme (Magnesium, Silicon, Water, Vacancies), relying upon



204 and MSWA-scheme (Magnesium, Silicon, Water, Aluminum), based on

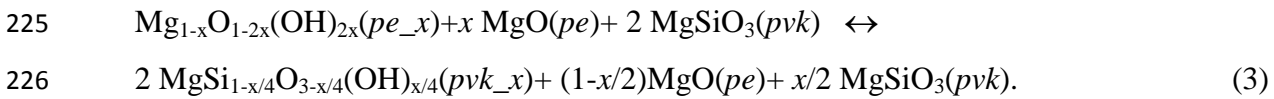


207 Other possible mechanisms of H-incorporation resorting to the introduction of  $\text{Fe}^{3+}$ , i.e.

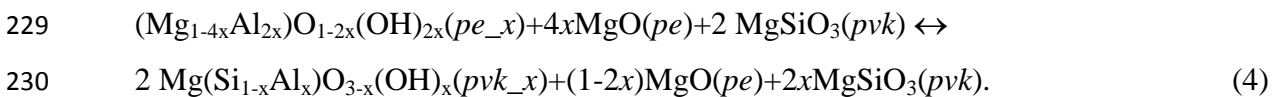


210 are here neglected as we pay attention to partitioning reactions governed by sub-solidus atomic  
 211 replacements, thus leaving out those that involve also REDOX-conditions of the environment. In  
 212 equ.(1a-b), we assume an incorporation *via* replacement of one Mg/Si with 2/4 H atoms. Such a  
 213 scheme leads to the formation of (i) hydroxyl groups (Smyth 2006), between entering H and  
 214 coordination oxygens, and (ii) X-cation vacancies ( $V_X$ ) at the expenses of either magnesium (in *pe*)  
 215 or silicon (in *pvk*). In *pvk*, the substitution of one six-fold coordinated Si with four H atoms that  
 216 establish as many hydroxyl groups with vertex oxygens of the same polyhedron accounts for a  
 217 better capacity to accept and organize OHs in such a site, than in higher coordination ones  
 218 (Williams and Hamley, 2001). In equ.(2a-b), H enters *pe* and *pvk* along with Al, to replace two Mg  
 219 atoms and one Si atom, respectively. The sites vacated by Mg/Si host Al, whereas H establishes  
 220 hydroxyls with coordination oxygens.

221 We base our leading reaction schemes on the equilibrium of a  $x$ -molar content of  $H_2O$  entering  
 222 either *pe* (1 mole) or *pvk* (2 moles), in agreement with the phase molar proportions determined by  
 223 the lower mantle models (Table 1).  $x$ - $H_2O$  is often addressed to as “H/ $H_2O$ -uptake” or “H/ $H_2O$ -  
 224 exchange”. According to the MSWV scheme, the equation below holds



227 MSWA, which in turn is likely closer to the supposed physical uptake mechanism and requires  
 228 an additional  $x$ -molar content of  $Al_2O_3$ , is associated to the equilibrium reaction shown beneath



231 *pe<sub>-x</sub>* and *pvk<sub>-x</sub>* refer to H-bearing periclase and perovskite, with compositions according to the  
 232 equations above. Note that we use a hydroxyl-based notation to stress the formation of OHs, as  
 233 stated above.

234

#### 235 4. EQUILIBRIUM CONSTANT

236

237 At equilibrium, the reactions described by Equ.(3)-(4) require that

238  $\Phi_{pe} \mu(pe) + \Phi_{pe_{-x}} \mu(pe_{-x})+ \Phi_{pvk} \mu(pvk) = \Omega_{pe} \mu(pe) + \Omega_{pvk_{-x}} \mu(pvk_{-x}) + \Omega_{pvk} \mu(pvk)$  (5.a)

239 or

240  $\sum_k \Phi_k \mu(k) = \sum_j \Omega_j \mu(j)$  (5.b)

241 where:  $\mu(A)$  is the chemical potential associated to the  $A$ -component and depends on  $P, T$  and the  
 242 system's composition. Moreover,

243  $\mu(A) = \mu_0(A) + RT \ln(a_A),$  (5.c)

244 where:  $R$  is the gas constant,  $\mu_0(A)$  depends on  $P$  and  $T$  only, and  $a_A$  is the activity. The equilibrium  
 245 constant  $K(P,T,x)_D$  for the reactions on study can be cast as

246 
$$K(P,T,x)_D = \left[ \frac{\prod_k a_k^{\Phi(k)}}{\prod_j a_j^{\Omega(j)}} \right] = \exp(-\Delta G_0(P,T,x)/RT),$$
 (6.a)

247 where:

248 
$$\Delta G_0(P,T,x) = \Phi_{pe\_x} \mu_0(pe\_x) - \Omega_{pvk\_x} \mu_0(pvk\_x) + (\Phi_{pe} - \Omega_{pe}) \mu_0(pe) + (\Phi_{pvk} - \Omega_{pvk}) \mu_0(pvk)$$
  
 249 (6.b)

250 We have estimated the dependence of  $\Delta G_0(P,T,x)$  on  $T$  via harmonic lattice dynamics modeling  
 251 and semi-empirical potentials (Gale, 1997). At high-pressure regime we observe that the effect of  
 252 the atomic vibrations dependent part of  $\Delta G_0(P,T,x)$  is immaterial with respect to that due to the  
 253 static contribution. Pressure, in turn, has been determined as  $P = \partial E(V,T) / \partial V$ , calculating by  
 254 quantum-mechanics and semi-empirical potentials the static and vibrational energy contributions,  
 255 respectively, for pure periclase and perovskite, only.

256

## 257 5. COMPUTING

258

259 *Ab-initio* Linear-Combination-of-Atomic-Orbital calculations (HF/DFT-CRYSTAL09 program;  
 260 Dovesi et al., 2009) have been carried out for  $pe\_x$  and  $pvk\_x$ , covering a pressure range from 24 to  
 261 80 GPa. The  $P$  range taken is so wide as to broadly encompass that of “pyrolite” liquidus (i.e.:  
 262 Corgne et al., 2005) at lower mantle pressures inferred from melting experiments of Trønnes and  
 263 Frost (2002) and Ito et al. (2004). At  $P > 24$  GPa, the sub-solidus post-spinel transition is completed  
 264 even in presence of 2 wt % H<sub>2</sub>O (Ghosh et al., 2013), and setting an upper  $P$ -limit at 80 GPa (~  
 265 2000 Km depth) allows one to exclude the D'' region, where the here chosen mineral portioning  
 266 model cannot be used.

267 Periclase and perovskite structures have been relaxed to equilibrium at a given nominal pressure  
 268 and 0 K, the former then corrected to account for thermal pressure. We have adopted a Hamiltonian  
 269 based on the WC1LYP scheme (Scanavino et al., 2012; Scanavino and Prencipe, 2013), which  
 270 contains a hybrid Hartree–Fock/density functional exchange–correlation term that mixes the  
 271 WCGGA exchange component (Wu and Cohen, 2006) with the exact nonlocal HF exchange  
 272 contribution and models correlation energy *via* the Lee–Yang–Parr GGA functional (Lee et al.,  
 273 1988). In the case of  $pe$ , we have used a hybridization rate (HR) of 20%, whereas for  $pvk$  HR has  
 274 been set at 28%. Such values have proven to model correctly equation of state, geometry and phase  
 275 transition pressures [see Parisi et al. (2012)]. In order to assess the effect of energy-shift due to a  
 276 different HR-ratios, we have sampled ten  $H(P)$ -values for perovskite, using a HR=20%, over the  $P$ -

277 interval here explored. The enthalpy differences, with respect to those by HR=28%, affect our main  
278 issues (equilibrium constants and inferred concentration ratios) by 3 - 12%, a figure negligible in  
279 view of the degree of approximation for so complex a process, and which does not cause any  
280 significant shift of the equilibrium of the reactions (3) and (4). The following values have been used  
281 for the tolerances governing the accuracy of the integrals of the self-consistent-field-cycles:  $10^{-8}$  for  
282 coulomb overlap,  $10^{-8}$  for coulomb penetration,  $10^{-8}$  for exchange overlap,  $10^{-8}$  for exchange  
283 pseudo-overlap in direct space and  $10^{-12}$  for exchange pseudo-overlap in reciprocal space. A  
284 threshold of  $10^{-8}$  a.u. has been chosen for SCF-cycles' convergence, while, for the frequencies  
285 calculation, the  $10^{-10}$  threshold has been used. Anderson mixing model (Anderson, 1965) as a  
286 convergence accelerator has been used. The reciprocal space has been sampled according to a  
287 regular sub-lattice with a shrinking factor IS equal to 6 corresponding to 112 **k**-points through the  
288 irreducible Brillouin zone for perovskite and 80 **k**-points for periclase. The convergence of the  
289 geometry optimization process depends on the root-mean-square (RMS) and absolute value of the  
290 largest component of both the gradients and nuclear displacements. The thresholds for the  
291 maximum and the RMS forces (the maximum and the RMS atomic displacements) have been set at  
292 0.00025 and 0.00020 a.u. and those for the maximum and the RMS atomic displacements at  
293 0.00130 and 0.00100 a.u. Relaxation terminates when all four conditions are fulfilled. Dissolution  
294 of water in *pe* and *pvk* has been modeled by super-cells (up to 64 and 125 octahedral sites, for MgO  
295 and MgSiO<sub>3</sub>, respectively) in which the replacements (1a-b) and (2a-b) mimic incorporation of H.  
296 We tuned the super-cell's size in order to allow reproduction of different degrees of dilution of  
297 water in the crystal structures, introducing one defect only at a time. For either incorporation  
298 scheme, the positions of H and Al have been determined according a least-enthalpy principle,  
299 exploring all possible H *versus* O configurations and taking into account the principle of local  
300 charge balance. According to MSWV, the H atoms lie along one of the main diagonals of the  
301 Si/Mg-emptied octahedron and establish hydroxyl groups with the oxygens at the ends; three  
302 configurations in either mineral are possible. The MSWA-scheme leads to H atoms forming  
303 hydroxyls with oxygens of the octahedron adjoining the one in which Al replaces Mg, in *pe*; the  
304 involved oxygen atoms are second nearest neighbors of Al and the resulting OH-groups are slightly  
305 canted from the main octahedral diagonal towards the aluminum-occupied site. The replacement of  
306 Si with Al and introduction of H in *pvk* yields formation of a hydroxyl between hydrogen and an  
307 oxygen of the octahedron hosting the cation substitution; six possible arrangements are possible.  
308 The start Gaussian LCAO basis set of Mg was taken from Causà et al. (1986), then improved by the  
309 addition of diffuse *sp* and *d* shells so as to obtain an 85-11G\* contraction. For O, we used the basis  
310 set of Ottonello et al. (2008) extended by a *d* shell to get an 84-11G\* contraction. In the case of Fe,  
311 the basis set of Valerio et al. (1995) was adopted, corresponding to an 86-41G\* contraction scheme.  
312 We also tried out a variational re-optimization of the exponents of the most diffuse Gaussian

313 functions of all the three elements, in *pe* and *pvk*, but without achieving any significant  
314 enhancement with respect to their original values. Further calculations have been carried out by  
315 semi-empirical potentials and lattice dynamics, using the GULP code, in order to estimate the effect  
316 of the vibration contribution on  $\Delta G_0(P,T,x)$ , as stated in the previous section. The Mg-O, Si-O, O-O  
317 interactions have been modelled by Buckingham-type potentials from the program's repository  
318 (Gale, 1997).

319

320

## 6. $K(P,T,x)_D$ CALCULATION

321

322 In the present instance, one has that

$$323 \mu_0(A_{-x},P,T)=H_0(A_{-x},P) - T \times S(A_{-x})_{\text{config}}, \quad (7)$$

324 where  $H_0(A_{-x},P)$  and  $S(A_{-x})_{\text{config}}$  are enthalpy and configuration entropy of the  $A_{-x}$  phase, taking  
325 into account that we restrict our energy calculations to static contributions, only. A first order  
326 expansion in  $x$  suffices to provide a correct description of the enthalpy as substantiated by the  
327 trends of  $H_0(A_{-x},P)$  for *pe*<sub>-x</sub> and *pvk*<sub>-x</sub> determined by exploring 80  $P$ - $x$  points systematically  
328 sampled over the interval 20-80 GPa, and 0-0.1, for either phase. Linear interpolations in  $x$  of points  
329 sharing the same  $P$  yield R-values larger than 0.999, so that  $H_0(A_{-x},P) \approx H_0(A,P) + \omega(A,P) \times x$ ,  
330 where  $\omega$  depends on the incorporation scheme.

331 Altogether, equ.(6.b) for MSWV results in

$$332 \Delta G_0(P,T,x)=\{[\omega_{\text{MSWV}}(pe,P)-2 \times \omega_{\text{MSWV}}(pvk,P)] + 0.5 \times [3 \times H_0(pe,P) - H_0(pvk,P)]\} \times x \\ 333 - T \times \Delta S(x)_{\text{MSWV,config}} \quad (8.a)$$

334 and

$$335 \Delta S(x)_{\text{MSWV,config}} = R \times [x/2 \times \ln(4/3) + 1/2 \times x \times \ln(x) + (1-x) \times \ln(1-x) - 2 \times (1-x/4) \times \ln(1-x/4)],$$

336  $R$  being the gas constant in kJ/K.

337 For MSWA one has

$$338 \Delta G_0(P,T,x)=\{[\omega_{\text{MSWA}}(pe,P)-2 \times \omega_{\text{MSWA}}(pvk,P)] + 2.0 \times [3 \times H_0(pe,P) - H_0(pvk,P)]\} \times x \\ 339 - T \times \Delta S(x)_{\text{MSWA,config}} \quad (8.b)$$

340 and

$$341 \Delta S(x)_{\text{MSWA,config}} = R \times [2 \times x \times \ln(3/2) + (1-2 \times x) \times \ln(1-2 \times x) - 2 \times (1-x) \times \ln(1-x)].$$

342 Moreover, one observes that

$$343 \xi_{0,x} = 3 \times H_{0,x}(pe,P) - H_{0,x}(pvk,P) = a_{0,x} + a_{1,x} \times P + a_{2,x} \times P^2 \quad (9.a)$$

344 and

$$345 \xi_{\omega,x} = \omega_x(pe,P) - 2 \times \omega_x(pvk,P) = \omega_{0,x} + \omega_{1,x} \times P + \omega_{2,x} \times P^2, \quad (9.b)$$

346 so that

$$347 \Delta G_{0,x}(P,T,x) = (C \times \xi_{0,x} + \xi_{\omega,x}) \times x - T \times \Delta S(x)_{x,\text{config}} = (\xi''_{0,x} + \xi_{\omega,x}) \times x - T \times \Delta S(x)_{x,\text{config}}, \quad (10)$$

348 where: the subscript X stands for either MSWV or MSWA; C is set at 0.5, for MSWV, and at 2, for  
349 MSWA.

350 In Table 3 we set out the  $a_k/\omega_j$ -parameters, referred to Equ.(9.a-b), which we have calculated for  
351 the MSWV and MSVA models. Note that if one assumes  $x$ -H<sub>2</sub>O to be exchanged between partially  
352 hydrogenated perovskite and periclase, in contrast with the present model which relies on initially  
353 anhydrous H-exchangers,  $K(P,T,x)_D$  would be just slightly affected with respect to the one from the  
354 calculations here reported.

355

356

## 7. RESULTS

357

358 Let us indicate, for the sake of brevity, by  $R(pe\_x)$  and  $R(pvk\_x)$  the left-hand and right-hand  
359 side member, respectively, of Equ.(3) and (4). A shift of the H-exchange reaction toward  $R(pe\_x)$ ,  
360 or  $R(pvk\_x)$ , is here qualitatively associated to a “preference” of hydrogen to enter periclase, or  
361 perovskite, with respect to the other phase. In Figures 1a and b, we show isothermal  $K(P,T,x)_D$   
362 surfaces determined by either model using Equ.(6.a) at  $T=1500$  and  $2500$  K (spanning the  $T$ -interval  
363 of geochemical interest), as a function of pressure and  $x$ . The latter ranges up to the largest H<sub>2</sub>O-  
364 uptake compatible with 1  $pe$  mole and 2  $pvk$  moles, *i.e.*  $x \approx 0.02$ , assuming a reference  $BWC$  of 1500  
365 ppm. One observes that MSWV and MSWA lead to two different behaviors of the H<sub>2</sub>O-partitioning  
366 mechanisms, though both models give  $K(P,T,x)_D$  figures smaller than unity, thus suggesting a shift  
367 of the exchange reaction towards  $R(pvk\_x)$ . Such discrepancies are ascribable to the  $(\xi''_0 + \xi_\omega)$ -  
368 functions of Equ.(10). In particular, one observes that: (i)  $\xi''_0 + \xi_\omega$  depends on  $P$  only, and  
369  $\Delta G_0(P,T,x)$  is weakly dependent on  $T$  *via* configuration entropy; (ii) MSWV and MSWA provide  
370  $(\xi''_0 + \xi_\omega)$ -figures ranging from 247 to 252, and from 774 and 942 kJ/mol, respectively, over the 10-  
371 80 GPa interval. We expect therefore MSWA to show a more marked sensitivity to temperature and  
372 pressure than MSWV. Figure 2 displays through the  $\xi_\omega/\xi''_0$ -ratio an intrinsic difference between the  
373 two incorporation models. Note that that  $\xi_\omega$  and  $\xi''_0$  are reflective of the H-uptake mechanisms and  
374 “pure”  $pe/pvk$  behavior, respectively. In such a view, MSWV seems more prone to the cation  
375 substitution scheme than MSVA. Moreover, they exhibit  $\xi_\omega/\xi''_0$ s having dissimilar trends as a  
376 function of  $P$ , which yet agree to display decreasing  $\xi_\omega/\xi''_0$ -figures upon increasing pressure beyond  
377 45 GPa.

378 MSWV and MSWA show a remarkable dependence on the H<sub>2</sub>O-uptake, which leads to a general  
379 abatement of the equilibrium constant upon increasing  $x$ . By way of example, MSWV gives at  
380 1500/2500 K and 80 GPa a  $\Delta K(P,T,x)_D$ , between 0 and 0.02, of 77/60%, against some 36/25% of  
381 MSWA. Temperature affects the  $K(P,T,x)_D$  surface in terms of a shift towards unity at higher  $T$ -  
382 values. Such a behavior is consistent with that the larger  $T$ , the more the reaction model tends to

383 predict comparable penchants of *pe* and *pvk* to host hydrogen. “Low” *T*-values bring to light  
384 intrinsic differences between the incorporation mechanisms of MSWV and MSWA, yielding  
385  $K(P,T,x)_{DS}$  that increasingly divert from one another. At  $x=0.02$  and  $P=80$  GPa, MSWV and  
386 MSWA lead to  $\Delta K(P,T,x)_{DS}$ , passing from 1500 to 2500 K, of 16 and 58%, respectively. At  $x=0.02$   
387 and  $T=1500/2500$  K, MSWV and MSWA forecast changes of the equilibrium constant, from 24 to  
388 80 GPa, of about 2-3 and 17-28%, respectively.

389 Altogether, all this points to an H-incorporation energetics dependent on the mechanism that  
390 accounts for the atomic replacements required to host hydrogen. Hence, other atomic substitution  
391 schemes might shed further light on how far such an uptake reaction is affected by the chemical  
392 species involved.

393

394

## 8. DISCUSSION

395

396 On the basis of some experimental studies, Fe-free periclase seems to accommodate almost no  
397 water into its structure (Bolfan-Casanova et al., 2000; 2002); conversely, other authors (Murakami  
398 et al., 2002; Litasov and Othani, 2007) assign to this phase a large capability of water incorporation,  
399 with H<sub>2</sub>O-uptake ranging between 0.1 and 0.2 wt% (1000–2000 ppm). Such discrepancies might be  
400 reflective of the samples’ compositions, of their being out of *P-T* thermodynamic equilibrium  
401 and/or of the analytical strategy for water measurement. The different techniques used, i.e. infra-  
402 red spectroscopy (Bolfan-Casanova et al., 2000; 2002) *versus* secondary ion mass spectroscopy (i.e.  
403 Inoue et al., 2010), may yield sets of values that are internally consistent but discrepant with each  
404 other (Hernandez et al., 2013).

405 The *BWC* is re-calculated for the *pe-pvk* system, in view of the chosen geochemical models. The  
406 Equ.(3) and (4) require slightly different lower/upper *BWC*-values of the lower mantle: BSE  
407 (MSWA, 865/1614 ppm): LM (MSWA, 854/1593 ppm); BSE (MSWV, 869/1629 ppm); LM  
408 (MSWV, 859/1608 ppm). Assuming that the temperature gradient of the lower mantle is mainly  
409 adiabatic,  $\nabla T$  depends on the geochemical model and mineralogical composition (Turcotte and  
410 Schbert, 1982; Matas et al., 2007; Murakami et al., 2012). BSE and LM, which imply different  
411 mechanisms of convection, yield temperature gradients throughout the *P* range here investigated as  
412 large as 0.3 and 0.5 K/km, respectively, in agreement with Ono (2008); therefore, the ensuing *P-T*  
413 relationships we use are:

$$414 T(\text{LM})=11.290\times P+1648 \quad (11.a)$$

415 and

$$416 T(\text{BSE})=6.596\times P+1686, \quad (11.b)$$

417 *P* in GPa and *T* in K.

418 We introduce the notion of “average equilibrium constant”, defined by the equation below

$${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} = \frac{1}{BWC} \int_0^{BWC} K(P,T,x)_D dx \quad (12)$$

where the integration is calculated over the possible H<sub>2</sub>O-uptake values, i.e.  $x$  from 0.0, namely a fully anhydrous  $pe+pvk$  system, to  $BWC$  ( $\approx 0.01/0.02$  molar fraction, according to Figs 1a-1b). For the sake of simplicity, we shall use the reference notations “1500” and “800” ppm to refer to maximum and minimum geochemically sound  $BWC$ , respectively, instead of its precise values actually adopted for calculations. One can then quantify the variations of the average equilibrium constant upon the  $x$ -range explored by means of

$$\sigma_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} = \sqrt{\frac{1}{BWC} \int_0^{BWC} [K(P,T,x)_D - {}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}]^2 dx}. \quad (13)$$

In some case, we express the average equilibrium constant in terms of  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$  ( $\pm \sigma_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$ ), where the figure between parentheses is meant to give a measure of the “dispersion” of  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$ , neither is it related to the conventional notion of experimental uncertainty.

The MSWV partitioning mechanism predicts (Fig. 3a)  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$  decreasing upon increasing  $BWC$ , indicating a worsening of the H<sub>2</sub>O-uptake capacity of  $pe$ , and a consequent shift of the exchange reaction towards  $pvk$ . Pressure is of weak import over the range explored, as proven by very close  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$  values at 24 GPa and 80 GPa, for both 800 and 1500  $BWC$ ; the most relevant effects are due to temperature.  $\sigma_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} / {}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} < 0.1$  suggests a moderate dispersion. The difference between BSE and LM, in terms of  $pe$  versus  $pvk$  modal contents ( $pe/pvk$  : 0.21 vs 0.18), is likely too small to bring to light differences in the  $pv$ - $pvk$  H<sub>2</sub>O-uptake capacity following the MSWV partitioning mechanism.

MSWA shows similar features (Fig. 3b), but the differences between isobaric-curves, and between  $BWC$ s, are more marked than MSWV’s. The different BSE and LM  $pe/pvk$  modal proportions are here revealed, though they modestly influence the  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$  values in the MSWA exchange mechanism.  $\sigma_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} / {}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk} < 0.25$  is significantly larger than MSWV’s, as a consequence of the more quickly changing average equilibrium constant provided by MSWA. Notwithstanding that, the general behavior of  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$  is univocally determined, neither, in especial, is any inversion of the H-exchange reaction between  $pe$  versus  $pvk$  forecast to take place over the explored  $P$ - $T$  interval.

In full, both MSWV and MSWA show weakly varying  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$ -figures over the  $P$ - $T$  range of geochemical interest. The LM-model leads to an H-exchange equilibrium constant ranging over 0.836/0.906( $\pm 0.09/\pm 0.05$ )-0.860/0.920( $\pm 0.07/\pm 0.04$ ), for MSWV and 1500/800 ppm, and over 0.623/0.772( $\pm 0.182/\pm 0.120$ )-0.649/0.787( $\pm 0.174/\pm 0.113$ ), for MSWA and 1500/800 ppm. BSE, in



452 turn, gives  ${}_{BWC}K(P,T)_{D,H_2O}{}^{pe/pvk}$ s lying in the intervals 0.830/0.902( $\pm 0.090/\pm 0.053$ )-  
 453 0.842/0.910( $\pm 0.084/\pm 0.049$ ), for MSWV and 1500/800 ppm, and 0.614/0.762( $\pm 0.188/\pm 0.125$ )-  
 454 0.607/0.757( $\pm 0.190/\pm 0.127$ ), for MSWA and 1500/800 ppm.

455 In view of so narrow ranges, we have chosen to introduce the following quantity:

$$456 \langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle = \frac{1}{\Delta P} \int_{P_0}^{P_{max}} {}_{BWC}K(P,T(P))_{D,H_2O}{}^{pe/pvk} dP$$

457 where  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  represents the average  ${}_{BWC}K(P,T)_{D,H_2O}{}^{pe/pvk}$  calculated along the lower  
 458 mantle's  $P$ - $T$ -paths predicted by LM and BSE. We think that  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$ , which is somewhat  
 459 a grand-average equilibrium constant, may be effective to provide an overall description for the H-  
 460 exchange reactions as a function of  $BWC$  only.

461 BSE and LM provide  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$ s close to one another, for a given incorporation scheme  
 462 and  $BWC$  value (Table 4).  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  shows an increasing sensitivity to  $BWC$  and, foremost,  
 463 H-exchange mechanism. On the basis of the  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$ s in Table 4 one determines the  
 464  $d\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle/d(BWC)$  slopes, which are weakly dependent on the geochemical model and  
 465 significantly sensitive to the microscopic reaction mechanism, thus obtaining -0.00003, for MSWA,  
 466 and -0.00001 ppm<sup>-1</sup>, for MSWV.

467 Altogether, in the  $P$ - $T$  interval of interest ( $\approx 24$ -80 GPa, 1800-2600 K) and taking a bulk water  
 468 content over the range of 800-1500 ppm, the  $pe/pvk$  H-exchange equilibrium constant of the  
 469 MSWV mechanism may be ultimately considered as a constant value,  $\approx 0.875$ . Such a figure is  
 470 determined as the mean of the  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  values in Table 4 for LM and BSE. In the case of  
 471 the MSWA mechanism,  $\langle {}_{BWC}K_{D,H_2O}{}^{pe/pvk} \rangle$  is more sensitive to  $BWC$  (and LM over BSE), but its  
 472 values still lie in a rather narrow range, namely 0.610- 0.780.

473 Let us describe the system perovskite+periclase+H<sub>2</sub>O as anhydrous-periclase+anhydrous-  
 474 perovskite+H-bearing-periclase+H-bearing-perovskite, such that equilibrium be provided by a H-  
 475 exchange according to the reactions (3) and (4); taking into account that the H<sub>2</sub>O-content is  
 476 comparatively very small and assuming activity coefficients equal to unity then

$$477 {}_{BWC}K(P,T)_{D,H_2O}{}^{pe/pvk} \approx \left[ \left( \frac{\lambda_{pvk}}{\lambda_{pvk\_H}} \right)^2 \left( \frac{\lambda_{pe\_H}}{\lambda_{pe}} \right) \right]$$

478 where:  $\lambda_A$  is the fraction molar content related to the  $A$ -phase;  $pvk\_H$  and  $pe\_H$  refer to H-  
 479 bearing perovskite and periclase, respectively. For the sake of simplicity, we hypothesize that fully  
 480 anhydrous phases (if any exists in the whole Earth's mantle) occur in negligible amount, and  
 481 therefore  $\lambda_{pvk\_H}$  and  $\lambda_{pe\_H}$  are the sole significant terms stemming from the equilibrium reactions. In  
 482 this view,  $\lambda_{pvk\_H} + \lambda_{pe\_H} = 1$ , and the equation above simplifies into

$${}_{BWC}K(P, T)_{D, H_2O^{pe/pvk}} \approx \frac{\lambda_{pe-H}}{(1 - \lambda_{pe-H})^2}. \quad (14)$$

Using Equ.(14) and  $\langle {}_{BWC}K_{D, H_2O}^{pe/pvk} \rangle$ -values, one can calculate the ratio between the H<sub>2</sub>O-contents hosted by periclase and perovskite (i.e  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$ ).  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$ , formally named “partition coefficient”, is therefore a useful instrument to direct compare our results with experimental data.

Figure 4 displays the  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  trends as a function of *BWC*, determined for the LM and BSE models using the  $\langle {}_{BWC}K_{D, H_2O}^{pe/pvk} \rangle$ s of Table 4. Irrespective of the geochemical model, MSWV and MSWA give the same concentration ratio over the two phases ( $C_{H_2O}^{pe}/C_{H_2O}^{pvk} \approx 0.6$ ) at “from low to very low” bulk water contents (*BWC*<500 ppm). Upon increasing the potential bulk water contents, the  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratio decreases, exhibiting divergent trends as a function of the exchange mechanism (Fig.4). In particular, one observes that the MSWV-linear interpolation’s slope is close to 0 ( $C_{H_2O}^{pe}/C_{H_2O}^{pvk} = 0.60-0.49$ ; *BWC* spanning from 500 to 3000 ppm). In this light, we suggest that the  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratio for the lower mantle may be taken as large as 0.56, implying that *pe* accommodates from 237 to 538 ppm.

MSWA, in turn, leads to a  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$ -trend having a slightly steeper negative slope, which yields  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratios of  $\approx 0.3$  for a potential (unrealistic?) bulk water contents of 3000 ppm. In the region of 800-1500 ppm the MSWA- $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratio may also be considered nearly invariant and as large as 0.47, obtained as the average over the interval between 0.43 and 0.51; this leads to *pe* hosting H<sub>2</sub>O in terms of 480-230 ppm.

Combining the results of MSWV and MSWA, we propose that, over the *P-T-BWC* range of interest ( $\approx 24-80$  GPa, 1800-2600 K, 800-1500 ppm) the  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratio lies in the short interval of 0.47-0.56. Our results agree with those of Hernandez et al. (2013), insofar as H<sub>2</sub>O prefers *pvk* over *pe*, but are at variance on the partition coefficient, which is predicted of 0.01 by the quoted authors, *versus* ours that is by one order of magnitude larger (0.47-0.56). Then, the present issues suggest that even in a lower mantle with low or very low bulk water content, periclase hardly becomes a pure anhydrous phase.

## 9. CONCLUSIONS

On the basis of two different H-incorporation mechanisms and two geochemical lower mantle models, the  ${}_{BWC}K(P, T)_{D, H_2O}^{pe/pvk}$  values here calculated lie over the range from  $\approx 0.6$  to  $\approx 0.9$ , showing that the H-exchange reactions shifts towards *pvk*, independently of the microscopic H-uptake scheme, i.e. MSWV, or MSWA. However, the H-incorporation models, MSWV and MSWA, lead

516 to dissimilar trends, the latter giving smaller equilibrium constant values and showing a more  
517 marked sensitivity to  $P$ - $T$  than the former does. Both microscopic models give  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$ s  
518 that decrease upon augmenting the bulk water contents ( $BWC$ ), suggesting an increase of penchant  
519 of  $pvk$  to host water. In general, MSWV and MSWA exhibit a modest, quasi-negligible, dependence  
520 on  $P$ , whereas they are sensitive to temperature and foremost  $BWC$ . Note that  ${}_{BWC}K(P,T)_{D,H_2O}^{pe/pvk}$   
521 varies little over the  $P$ - $T$  range predicted by the LM and BSE geochemical frames for the lower  
522 mantle, and can therefore be replaced by its average,  $\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ , calculated over the pressure-  
523 temperature path forecast by the geochemical models. Regardless of the microscopic H-exchange  
524 reaction, the LM and BSE models lead to  $\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ s ranging from 0.613 to 0.908, and from  
525 0.589 to 0.899 respectively.

526 In full, the equilibrium constant of the H-incorporation reactions exhibits a complex dependence  
527 on both natural environment's variables ( $P$ ,  $T$ ,  $BWC$ ) and microscopic mechanisms involved. If  $pe$   
528 and  $pvk$  are supposed to occur in the lower mantle as H-bearing phases, then  $H_2O$  is distributed  
529 according to various possible partitioning mechanisms, of which we have here explored MSWV and  
530 MSWA, only. MSWV and MSWA lead to different  $K_D$ -values, whose discrepancies become  
531 apparent, in particular, if one takes  $K(P,T,x)_D$ . This suggests that the microscopic uptake scheme  
532 heftily affects the equilibrium constant. The experimentally determined  $H_2O$  contents in  $pe$  range  
533 from  $<10$  ppm (Bolfan-Casanova et al., 2000; 2002), to 0.1-0.2 wt% (1000–2000 ppm; Murakami et  
534 al., 2002). Such discrepancies might be reflective of the following aspects: (i) partial  
535 thermodynamic equilibrium in experiments, with respect to the ideals of calculations; (ii) in view of  
536 the point above, defects (cation replacements and deviations from ideal crystal structure), which  
537 widely occur in specimens from a  $HP$ - $HT$  synthesis, remarkably change the capacity of hosting  
538 hydrogen in a phase.

539 We therefore propose that, combining the results of MSWV and MSWA in the  $P$ - $T$ - $BWC$  range  
540 of interest ( $\approx 24$ -80 GPa, 1800-2600 K, 800-1500 ppm), the  $C_{H_2O}^{pe}/C_{H_2O}^{pvk}$  ratio (commonly named  
541 “partition coefficient”) lies in the interval 0.47-0.56. This implies that water always prefers  $pvk$  than  
542  $pe$ , but it also suggests that even in a lower mantle with low or very low bulk water content,  
543 periclase hardly becomes a pure anhydrous phase.

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- 550 Abe Y., Ohtani E., Okuchi T., Righter K. and Drake. M. (2000) Water in the early Earth. In *Origin*  
551 *of the Earth and Moon* (eds. R.M. Canup and K. Righter). University of Arizona Press, Tucson.  
552 pp 413-433.
- 553 Ahrens T. J. (1989) Water storage in the mantle. *Nature* **342**, 122-123.
- 554 Anderson D. G. (1965) Iterative procedures for nonlinear integral equations. *J. Assoc. Comput.*  
555 *Mach.* **12**, 547-560.
- 556 Anderson D. L. (1989) Composition of the Earth. *Science* **243**, 367–370.
- 557 Bolfan-Casanova N. ( 2005) Water in the Earth's mantle. *Min. Mag.* **69**, 229-257.
- 558 Bolfan-Casanova N., Keppler H. and Rubie D. C. (2000) Partitioning of water between mantle  
559 phases in the system MgO–SiO<sub>2</sub>–H<sub>2</sub>O up to 24 GPa: implications for the distribution of water in  
560 the Earth's mantle. *Earth Planet. Sci. Lett.* **182**, 209-221.
- 561 Bolfan-Casanova N., Mackwell S., Keppler H., McCammon C. and Rubie, D. C. (2002). Pressure  
562 dependence of H solubility in magnesiowüstite up to 25 GPa: implications for the storage of  
563 water in the Earth's lower mantle. *Geophys. Res. Lett.* **29** (10), 1029–1032.
- 564 Bolfan-Casanova N., McCammon C. A. and Mackwell S. J (2006) Water in transition zone and  
565 lower mantle minerals. In *Earth's Deep Water Cycle* (eds. S.D Jacobsen and S. Van Der Lee)  
566 Geophysical Monograph Series, Vol 168 AGU. doi:10.1029/168GM06.
- 567 Bonadiman C., Hao Y., Coltorti M., Dallai L., Huang U. and Xia Q. (2009) Water contents of  
568 pyroxenes in intraplate lithospheric mantle. *Eur. J. Mineral.* **21**, 637-647.
- 569 Cammarano F., Romanowicz B. (2007) Insights into the nature of the transition zone from  
570 physically constrained inversion of long period seismic data. *PNAS-High Pressure Geoscience*  
571 **104**, 9139-9144.
- 572 Causà M., Dovesi R., Pisani C. and Roetti C. (1986) Electronic structure and stability of different  
573 crystal phases of magnesium oxide. *Phys Rev B* **33**, 1308–1316.
- 574 Corgne, A., Liebske C., Wood B. J., Rubie D. C. and Frost D. J. (2005) Silicate perovskite-melt  
575 partitioning of trace elements and geochemical signature of a deep perovskitic reservoir. *Geochim.*

576 *Cosmochim. Acta* **69**, 485–496.

577 Dai L. and Karato S. (2009) Electrical conductivity of wadsleyite at high temperatures and high  
578 pressures. *Earth Planet. Sci. Lett.* **287**, 277–283.

579 Demouchy S., Mackwell S. J. and Kohlstedt D. L. (2007) Influence of hydrogen on Fe–Mg  
580 interdiffusion in (Mg,Fe)O and implications for Earth’s lower mantle. *Contrib. Mineral. Petrol.*  
581 **154**, 279–289.

582 Dixon, J. E., Leist L., Langmuir C. and Schilling, J. G. (2002). Recycled dehydrated lithosphere  
583 observed in plume-influenced mid-ocean-ridge basalt. *Nature* **420**, 385–389.

584 Dovesi, R., Saunders V. R., Roetti C., Orlando R., Zicovich-Wilson C. M., Pascale F., Civalleri B.,  
585 Doll K., Harrison N. M., Bush I. J., D’Arco P., and Llunell M. (2009) CRYSTAL09 User's  
586 Manual (University of Torino, Italy).

587 Fiquet G., Andrault D., Dewaele A., Charpin T., Kunz M. and Häusermann D. (1998) P–V–T  
588 equation of state of MgSiO<sub>3</sub>. *Phys Earth Planet Int.* **105**, 21–31.

589 Gale J.D. (1997) GULP: A computer program for the symmetry-adapted simulation of solids *J.*  
590 *Chem. Soc., Faraday Trans.* **93**, 629–637.

591 Garnero E. J., Maupin V., Lay T., and Fouch M. J. (2004) Variable azimuthal anisotropy in Earth’s  
592 lowermost mantle. *Science* **306**, 259–261.

593 Ghosh S., Ohtani E., Litasov K. D., Suzuki A., Dobson D., Funakoshi K. (2013) Effect of water in  
594 depleted mantle on post-spinel transition and implication for 660 km seismic discontinuity. *Earth*  
595 *Planet. Sci. Lett.* **371**, 103–111.

596 Griffin J. M., Berry J.A, Frost D. J., Wimperis S. and Ashbrook S. E. (2013) Water in the Earth's  
597 mantle: a solid-state NMR study of hydrous wadsleyite. *Chem. Sci.* **4**, 1523–1538.

598 Guyot F., Madon M., Peyronneau J. and Poirier J. P. (1988) X-ray microanalysis of high-  
599 pressure/high-temperature phases synthesized from natural olivine in a diamond anvil cell. *Earth*  
600 *Planet. Sci. Lett.* **90**, 52–64.

601 Hauri E. H., Gaetani G. A. and Green, T. H. (2006) Partitioning of water during melting of the  
602 Earth's upper mantle at H<sub>2</sub>O-undersaturated conditions. *Earth Planet. Sci. Lett.* **248**, 715–734

603 Hernández E. R., Alfè D. and Brodholt J. (2013) The incorporation of water into lower-mantle  
604 perovskites: A first-principles study. *Earth Planet. Sci. Lett.* **364**, 37–43.

605 Hilst, R.D. van der, Widiyantoro, S., and Engdahl, E. R. (1997) Evidence for deep mantle  
606 circulation from global tomography. *Nature* **386**, 578-584.

607 Hirschmann M. M. (2006). Water, melting, and the deep Earth H<sub>2</sub>O cycle. *Ann. Rev. Earth Planet.*  
608 *Sci.* **34**, 629-653. doi:10.1146/annurev.earth.34.031405.125211.

609 Hirschmann M. M. and Kohlstedt D. (2012) Water in Earth's mantle. *Physics Today* **65**(3), 40-45.

610 Hirschmann M.M., Aubaud C. and Withers A.C. (2005). Storage capacity of H<sub>2</sub>O in nominally  
611 anhydrous minerals in the upper mantle. *Earth Planet. Sci. Lett.* **236**, 167-181

612 Hirschmann M. M., Tenner T., Aubaud C. and Withers, A. C. (2009) Dehydration melting of  
613 nominally anhydrous mantle: The primacy of partitioning. *Phys Earth Planet Int.* **176**, 54-68.

614 Huang X., Xu Y. and Karato S. (2005), Water content in the transition zone from electrical  
615 conductivity of wadsleyite and ringwoodite. *Nature* **434**, 746–749.

616 Ingrin J. and Skogby H. (2000) Hydrogen in nominally anhydrous upper mantle minerals:  
617 Concentration levels and implications. *Eur. J. Mineral.* **12**, 543-570.

618 Inoue T. (1994) Effect of water on melting phase relations and melt composition in the system  
619 Mg<sub>2</sub>SiO<sub>4</sub>-MgSiO<sub>3</sub>-H<sub>2</sub>O up to 15 GPa. *Phys. Earth Planet. Inter.* **85**, 237-263.

620 Inoue T., Wada T., Sasaki R. and Yurimoto, H. 2010. Water partitioning in the Earth's mantle. *Phys*  
621 *Earth Planet Int.* **183**, 245–251.

622 Irifune T. (1994) Absence of an aluminous phase in the upper part of the Earth's lower mantle.  
623 *Nature* **370**, 131-133.

624 Irifune T, Koizumi T and Ando J (1996) An experimental study of the garnet-perovskite  
625 transformation in the system MgSiO<sub>3</sub>-Mg<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>. *Geoph. Res. Lett.* **96**, 147–157.

626 Ito E. and Takahashi E. (1989). Postspinel transformations in the system Mg<sub>2</sub>SiO<sub>4</sub>-Fe<sub>2</sub>SiO<sub>4</sub> and  
627 some geophysical implications. *J. Geophys. Res.* **94**, Issue B8, 10637.

628 Ito E., Kubo A., Katsura T. and Walter M. J (2004) Melting experiments of mantle materials under  
629 lower mantle conditions with implications for magma ocean differentiation. *Phys Earth Planet*

630 *Int.* **143-144**, 397-406.

631 Jahn S., Rahner R., Dachs E., Mrosko M. and Koch-Müller M. (2013) Thermodynamic properties  
632 of anhydrous and hydrous wadsleyite,  $\beta$ -Mg<sub>2</sub>SiO<sub>4</sub>. *High Pressure Res.* **33**, 584-594.

633 Javoy M., Kaminski E., Guyot F., Andraut D., Sanlou J. R., Moreira M., Labrosse S., Jambon A.,  
634 Agrinier P., Davaille A. and Jaupart C. (2010) The chemical composition of the Earth: Enstatite  
635 chondrite models. *Earth Planet. Sci. Lett.* **293**, 259-268.

636 Joachim B., Wohlers A., Norberg N., Garde's E., Petrishcheva E. and Abart R. (2013) Diffusion  
637 and solubility of hydrogen and water in periclase. *Phys Chem Minerals* **40**, 19-27.

638 Johnson E. A. (2006) Water in nominally anhydrous crustal minerals: speciation, concentration and  
639 geological significance. In *Reviews in Mineralogy and Geochemistry* (eds. J. Smyth and H.  
640 Keppler), Mineralogical Society of America, Vol. 62, 117-154.

641 Karato S. and Jung H. (2003) Effects of pressure on high-temperature dislocation creep in olivine  
642 polycrystals. *Philos. Mag. A* **83**, 401-414.

643 Kellogg L. H., Hager B. H., and Hilst R. D. van der (1999) Compositional stratification in the deep  
644 mantle. *Science* **283**, 1881-1884.

645 Keppler H. and Bolfan-Casanova N. (2006) Thermodynamics of water solubility and partitioning.  
646 In: Water in nominally anhydrous minerals. In *Reviews in Mineralogy and Geochemistry* (eds:  
647 J.Smyth and H. Keppler), Mineralogical Society of America, **62**, 193-230.

648 Kesson S. E., Fitz Gerald J. D., Shelley, J. M. G. and Withers, R. L. (1995) Phase relations,  
649 structure and crystal chemistry of some aluminous silicate perovskites. *Earth Planet. Sci. Lett.*  
650 **134**, 187-201.

651 Khan A. and Shankland T. J. (2012) A geophysical perspective on mantle water content and  
652 melting: Inverting electromagnetic sounding data using laboratory-based electrical conductivity  
653 profiles. *Earth Planet. Sci. Lett.* **317-318**, 27-43.

654 Klepe A. K. (2006) High-pressure Raman spectroscopic studies of hydrous wadsleyite II.  
655 *Am.Mineral.* **91**, 1102-1109.

656 Lay T, Garnero E. J., Williams Q. (2004) Partial melting in a thermo-chemical boundary layer at the

657 base of the mantle. *Phys. Earth Planet. Inter.* **146**, 441-467.

658 Lay T., Williams Q. and Garnero, E. J. (1998) The core–mantle boundary layer and deep Earth  
659 dynamics. *Nature* **392**, 461–468.

660 Lee C., Yang W. and Parr R. G. (1988) Development of the Colle-Salvetti correlation-energy  
661 formula into a functional of the electron density. *Phys. Rev. B* **37**, 785–789.

662 Li J. and Agee C. B. (1996) Geochemistry of mantle–core differentiation at high pressure. *Nature*  
663 **381**, 686 - 689.

664 Lin J.F. and Wheat A. (2012). Electronic spin transition of iron in the Earth’s lower mantle.  
665 *Hyperfine Interact.* **207**, 81-88.

666 Litasov K. D, Ohtani E., Langenhorst F., Yurimoto H., Kubo T. and Kondo, T. (2003). Water  
667 solubility in Mg-perovskites, and water storage capacity in the lower mantle. *Earth Planet. Sci.*  
668 *Lett.* **211**, 189-203.

669 Litasov K. D. (2010) The influence of Al<sub>2</sub>O<sub>3</sub> on the H<sub>2</sub>O content in periclase and ferropiclase at 25  
670 GPa. *Russ. Geol. Geophys.* **51**, 644–649.

671 Litasov K. D. and Ohtani E. (2007). Effect of water on the phase relations in Earth's mantle and  
672 deep water cycle. In *Advances in High-pressure Mineralogy* (ed E. Ohtani, E.), Geological Soc.  
673 Amer., pp.115-156.

674 Lyubetskaya T. and Korenaga J. (2007) Chemical composition of Earth's primitive mantle and its  
675 variance: 1. method and results. *J. Geophys. Res.* **112** (B3), B03211,  
676 doi:10.1029/2005JB004223.

677 Mackwell S. J., Bystricky M. and Sproni C. (2005) Fe–Mg interdiffusion in (Mg,Fe)O. *Phys Chem*  
678 *Mineral.* **32**, 418–425.

679 Mao W. L., Mao H-k, Sturhahn W., Zhao J., Prakapenka V.B., Yue Meng Y., Shu J., Fei Y. and  
680 Hemley R. J. (2006) Iron-Rich Post-Perovskite and the Origin of Ultralow-Velocity Zones.  
681 *Science* **312**, 564-565.

682 Marty B. (2012) The origins and concentrations of water, carbon, nitrogen and noble gases on  
683 Earth. *Earth Planet. Sci. Lett.* **313–314**, 56–66.



684 Matas J., Bass J., Ricard Y., Mattern E. and Bukowinski M. S. T. (2007) On the bulk composition  
685 of the lower mantle: predictions and limitations from generalized inversion of radial seismic  
686 profiles. *Geophys. J. Int.* **170**, 764–780.

687 McCommon C. E, Stachel T. and Harris J. W. (2004) Iron oxidation state in lower mantle mineral  
688 assemblages II. Inclusions in diamonds from Kankan, Guinea. *Earth Planet. Sci. Lett.* **222**, 423-  
689 434.

690 McDonough W. F and Arevalo R. (2008) Uncertainties in the composition of Earth, its core and  
691 silicate sphere. *J. of Phys -Conference Series* **136** 022006 (abstr).

692 McDonough W. F. and Sun S. (1995) The composition of the Earth. *Chem. Geol.* **120**, 223–253.

693 Mei S. and Kohlstedt D. L. (2000) Influence of water on plastic deformation of olivine aggregates:  
694 2. Dislocation creep regime. *J. Geophys. Res.* **105**, 21,471-21,481.

695 Michael P. J. (1988) The concentration, behavior and storage of H<sub>2</sub>O in the suboceanic upper  
696 mantle - Implications for mantle metasomatism. *Geochim. Cosmochim. Acta* **52**, 555-566.

697 Montelli R., Nolet G., Masters G., Engdahl E. R. and Hung S.-H. (2004) Finite-frequency  
698 tomography reveals a variety of plumes in the mantle. *Science*, **303**, 338- 343.

699 Mosenfelder J. L., Sharp T. G., Asimow P. D. and Rossman G. R. (2013) Hydrogen Incorporation in  
700 natural mantle olivines. In *Earth's Deep Water Cycle* (eds S. D. Jacobsen and S. Van Der Lee),  
701 American Geophysical Union, Washington, D. C.. doi: 10.1029/168GM05.

702 Murakami M., Ohishi Y., Hirao N. and Hirose K. (2012) A perovskitic lower mantle inferred from  
703 high-pressure, high-temperature sound velocity data. *Nature* **485**, 90-94.

704 Murakami M., Hirose K., Yurimoto H., Nakashima S. and Takafuji N. (2002) Water in Earth's  
705 lower mantle. *Science* **295**, 1885, doi:10.1126/science.1065998.

706 Nomura R., Hirose K., Uesugi K., Ohishi Y., Tsuchiyama A., Miyake A., and Ueno Y. (2014) Low  
707 core-mantle boundary temperature inferred from the solidus of pyrolite. *Science* **343**, 522–525.

708 Oganov, A. R. and Brodholt, J. P. (2000) High –pressure phases in the Al<sub>2</sub>SiO<sub>5</sub> system: the problem  
709 of aluminous phase in the Earth's lower mantle: *ab initio* calculations. *Phys. Chem. Miner.* **27**,  
710 430-439.

711 Ohtani E. (2005). Effect of water on phase transitions in the Earth's mantle. *Elements* **1**, 25–30.

712 Ono S. (2008) Experimental constraints on the temperature profile in the lower mantle. *Phys. Earth*  
713 *and Planet. Inter.* **170**, 267–273.

714 Otsuka K., McCammon C. A. and Karato S-I (2010) Tetrahedral occupancy of ferric iron in  
715 (Mg,Fe)O: Implications for point defects in the Earth's lower mantle. *Phys. Earth and Planet.*  
716 *Inter.* **180**, 179-188.

717 Ottonello G., Civalleri B., Ganguly J., Vetuschi Zuccolini M. and Noel Y. (2008) Thermo-physical  
718 properties of the a–b–c polymorphs of Mg<sub>2</sub>SiO<sub>4</sub>: an all-electron ab initio study. *Phys. Chem.*  
719 *Miner.* **36**, 87–106.

720 Palme H. and O'Neill H. St. C. (2004) Cosmochemical estimates of Mantle Composition. In:  
721 *Treatise on Geochemistry* (eds , H.D Holland and K.K Turekian) Elsevier, Amsterdam, The  
722 Netherlands, Vol.2, pp 1-38.

723 Pamato M. G., Myhill R, Boffa Ballaran T., Frost D. J., Heidelbach F. and Miyajima N. (2015)  
724 Lower-mantle water reservoir implied by the extreme stability of a hydrous aluminosilicate.  
725 *Nature Geoscience* **8**, 75–79.

726 Panero W. R. and Stixrude L. (2004) Hydrogen incorporation in stishovite at high pressure and  
727 symmetric hydrogen bonding in d-AlOOH. *Earth Planet. Sci. Lett.* **221**, 421–431.

728 Panero W. R., Pigotti J. S., Reaman D. M, Kabbes J.E and Liu Z. (2015) Dry (Mg,Fe)SiO<sub>3</sub>  
729 perovskite in the Earth's lower mantle. *J. Geophys. Res. Solid Earth* **120**,  
730 doi:10.1002/2014JB011397.

731 Parisi F., Sciascia L., Princivalle F. and Merli M. (2012) The pressure induced ringwoodite to Mg-  
732 perovskite and periclase post-spinel phase transition: a Bader's topological analysis of the ab  
733 initio electron densities. *Phys. Chem. Miner.* **39**, 103–113.

734 Pearson D.G., Brenker F. E., Nestola F., McNeill J., Nasdala L., Hutchinson M.T., Matveev S.,  
735 Mather K., Slversmit G., Schmitz S., Vekemans B. and Vincze L. (2014) Hydrous mantle  
736 transition zone indicated by ringwoodite included within diamond. *Nature* **507**, 221-224.

737 Ringwood A. E. (1991) Phase transitions and their bearing on the constitution and dynamics of the

- 738 mantle. *Geochim Cosmochim Acta* **55**, 2083–2110.
- 739 Saal A. E., Hauri E., Langmuir C. H. and Perfit M. R. (2002) Vapour undersaturation in primitive  
740 mid-ocean-ridge basalt and the volatile content of Earth's upper mantle. *Nature* **419**, 451–455.
- 741 Salters V.J.M. and Stracke, A. (2004) Composition of the depleted mantle. *Geochem. Geophys.*  
742 *Geosyst.* **5**, 27, DOI: 10.1029/2003GC000597.
- 743 Saxena S. K., Liermann H-P. and Shen G. (2004). Formation of iron hydride and high-magnetite at  
744 high pressure and temperature *Phys. of the Earth and Planet. Int.* **146**, 313–317.
- 745 Scanavino I., Belousov R. and Prencipe M. (2012) Ab initio quantum-mechanical study of the  
746 effects of the inclusion of iron on thermoelastic and thermodynamic properties of periclase  
747 (MgO). *Phys. Chem. Miner.* **39**, 649–663.
- 748 Scanavino I. and Prencipe M. (2013) Ab-initio determination of high-pressure and high-temperature  
749 thermoelastic and thermodynamic properties of low-spin (Mg<sub>1-x</sub>Fe<sub>x</sub>)O ferropericlase with x in  
750 the range [0.06, 0.59]. *Am. Mineral.* **98**, 1270–1278.
- 751 Smyth J. R. (1994) A crystallographic model for hydrous wadsleyite: An ocean the Earth's interior?  
752 *Am. Mineral.* **79**, 1021-1025.
- 753 Smyth J. R. (2006) Hydrogen in high pressure silicate and oxide mineral structures. In *Water in*  
754 *nominally anhydrous minerals* (eds. J. Smyth and H. Keppler ). Geochemical Society-  
755 Mineralogical Society of America, Vol. 62 pp 85-115.
- 756 Smyth J. R. and Jacobsen S. D. (2006) Nominally anhydrous minerals and Earth's deep water cycle.  
757 In *Earth's Deep Water Cycle* (eds. S.D. Jacobsen and S. van der Lee). American Geophysical  
758 Union, Geophysical Monograph, Vol. 168 pp 1-11.
- 759 Stixrude L. and Bukowinski M. S. T. (1992) Stability of (Mg,Fe)SiO<sub>3</sub> perovskite and the structure  
760 of the lowermost mantle. *Geoph. Res Lett.* **19**, 1057-1060.
- 761 Trønnes R. G. and Frost D. J. (2002) Peridotite melting and mineral-melt partitioning of major and  
762 minor elements at 21-24 GPa. *Earth Planet. Sci. Lett.* **197**, 117-131.
- 763 Turcotte D. L. and Schubert G. (1982) Geodynamics. Wiley, New York, pp. 456.
- 764 Valerio G., Catti M., Dovesi R. and Orlando R. (1995) Ab initio study of antiferromagnetic rutile-

765 type FeF<sub>2</sub>. *Phys Rev B* **52**, 2422–2427.

766 Van Orman J. A., Li C. and Crispin K. L. (2009) Aluminum diffusion and Al-vacancy association  
767 in periclase. *Phys. Earth and Planet Int.* **172**, 34-42.

768 Walter, M. J., Kubo A., Brodholt J., Koga K. T., and Ohishi Y. (2004) Phase relations and equation-  
769 of-state of aluminous Mg-silicate perovskite and implications for the Earth's lower mantle. *Earth*  
770 *Planet. Sci. Lett.* **222**, 501–516.

771 Williams Q. and Hamley R. J. (2001) Hydrogen in the deep Earth. *Annu. Rev. Earth Planet. Sci.* **29**,  
772 365–418.

773 Wolfe, C. J., Solomon, S.C., Laske, G., Collins, J.A., Detrick, R. S., Orcutt, J. A., Bercovici D., and  
774 Hauri, E. H. (2009). Mantle shear-wave velocity structure beneath the Hawaiian hot spot. *Science*  
775 **326**. 1388- 1390.

776 Wood B. J. and Corgne A.(2007) Trace elements and hydrogen in the Earth's transition zone and  
777 lower mantle. In *Mineral Physics* (ed. G.D. Price), Treatise on Geophysics, (ed. G. Schubert).  
778 Elsevier, Amsterdam, Vol. 2 pp. 63-89.

779 Wood B. J. (1995) The effect of H<sub>2</sub>O on the 410-kilometer seismic discontinuity. *Science* **268**, 74-  
780 76.

781 Wu Z. and Cohen R. E. (2006) More accurate generalized gradient approximation for solids.  
782 *Physical Review B* **73**, 235116.

783 Wyssession M. E., Lay T, Revenaugh J., Williams Q., Garnero E., Jeanloz R., and Kellogg L. (1998)  
784 The D'' discontinuity and its implications. In *The Core-Mantle Boundary Region* (eds. M.  
785 Gurnis, M. E. Wyssession, E. Knittl and Buffet B.) Geodyn. SerAGU, Washington, D.C., Vol, 28,  
786 pp. 273–297.

787 Zindler A. and Hart S. (1986) Chemical Geodynamics. *Annual Rev. Earth Planet. Sc.* **14**, 493-571.  
788

789 **CAPTIONS OF THE FIGURES**

790

791 **Figure 1.**  $K(P, T, x)_D$  at 1500 and 2500 K, for MSWV (a) and MSWA (b).

792

793 **Figure 2.** MSWV,  $\xi_{\omega, \text{MSWV}} / \xi''_{0, \text{MSWV}}$ , and MSWA,  $\xi_{\omega, \text{MSWA}} / \xi''_{0, \text{MSWA}}$ , energy modeling. See  
794 Equ.9(a)-(b), for an explanation of  $\xi_s$ .

795

796 **Figure 3.**  $K(P, T)_{D, \text{H}_2\text{O}}^{pe/pvk}$  as a function of  $P$ ,  $T$  and  $BWC$  (Bulk Water Content), for MSWV (a)  
797 and MSWA (b). Empty and filled symbols correspond to 30 and 80 GPa, respectively. Triangles:  
798  $\text{H}_2\text{O}$  uptake value of  $\approx 1500$  ppm; circles:  $\text{H}_2\text{O}$  uptake value of  $\approx 800$  ppm.

799

800 **Figure 4.** Periclase-to-perovskite  $\text{H}_2\text{O}$ -contents ratio as a function of  $BWC$ . LM-MSWV: filled  
801 squares/filled line; LM-MSWA: filled diamonds/filled line; BSE-MSWV: empty squares/dashed  
802 line; BSE-MSWA: empty diamonds/dashed line.

Table 1. Lower mantle major element composition and mineral modal estimates obtained by mass balance calculations.

	BSE			LM
	*	**	#	***
wt%				
SiO <sub>2</sub>	45.00	45.01		47.53
Al <sub>2</sub> O <sub>3</sub>	4.45	3.59		4.04
FeO	8.05	7.94		8.23
MgO	37.80	38.97		37.87
CaO	3.55	2.73		2.32
<i>Mg-Pvk</i>	74	76	75	78
<i>Pe</i>	16	16	16	14
<i>Ca-Pvk</i>	7	6	6	6
Al <sub>2</sub> O <sub>3</sub> -HPphase	3	2	3	2
	r <sup>2</sup> =0.34	r <sup>2</sup> =0.13		r <sup>2</sup> =0.41

Major element mineral compositions from pyrolite-like experiments of Walter et al. (2004) and Corgne et al. (2005)

\*= McDonough and Sun (1995)

\*\*= Javoy et al. (2010)

\*\*\* = after Matas et al. (2007)

# BSE averaged mineral modal percentage used in calculation

Table 2. Water budget estimates in mantle repositories.

	Earth Mass (gr)	BSE mass (gr)	Upper mantle	Transition zone	Lower mantle	Bulk mantle
			(Fraction of Earth total mass)			
	5.98E+27	4.00E+27	0.103	0.075	0.492	
Thickness (km)			420	300	2170	2890
H <sub>2</sub> O (ppm)		1100-3000 <sup>1,2,3</sup>	200-300 <sup>4,5</sup>	1.0 -1.3 (wt%) <sup>6, 7</sup>	A-2000 <sup>6,8,9</sup>	1500-2400 <sup>3,6</sup>
Suggested value			250	1.2 (wt%)	<b>800/1500</b> (this study)	
					(A: value < 1000 ppm)	

1= McDonough and Sun (1995); 2=Palme and O'Neill (2004); 3= Marty (2012); 4= Dixon et al.(2002); 5= Saal et al. (2002); 6=Othani (2005); 7=Pearson et al (2014);8= Murakami et al.(2002); 9=Hernandez et al. (2013).

**Table 3.**  $a$  and  $\omega$  parameters for MSWV and MSWA models. See text for their meaning.

---

<b>MSWV model</b>		
$\omega_0$ (kJ/mol)	$\omega_1$ (kJ/mol/GPa)	$\omega_2$ (kJ/mol/GPa <sup>2</sup> )
145411.184	-4.77619218	0.0190667
$a_0$ (kJ/mol)	$a_1$ (kJ/mol/GPa)	$a_2$ (kJ/mol/GPa <sup>2</sup> )
-290293	5.7369	0.0057
<b>MSWA model</b>		
$\omega_0$ (kJ/mol)	$\omega_1$ (kJ/mol/GPa)	$\omega_2$ (kJ/mol/GPa <sup>2</sup> )
581384	-14.2968	0.0464
$a_0$ (kJ/mol)	$a_1$ (kJ/mol/GPa)	$a_2$ (kJ/mol/GPa <sup>2</sup> )
-290293	5.7369	0.0057

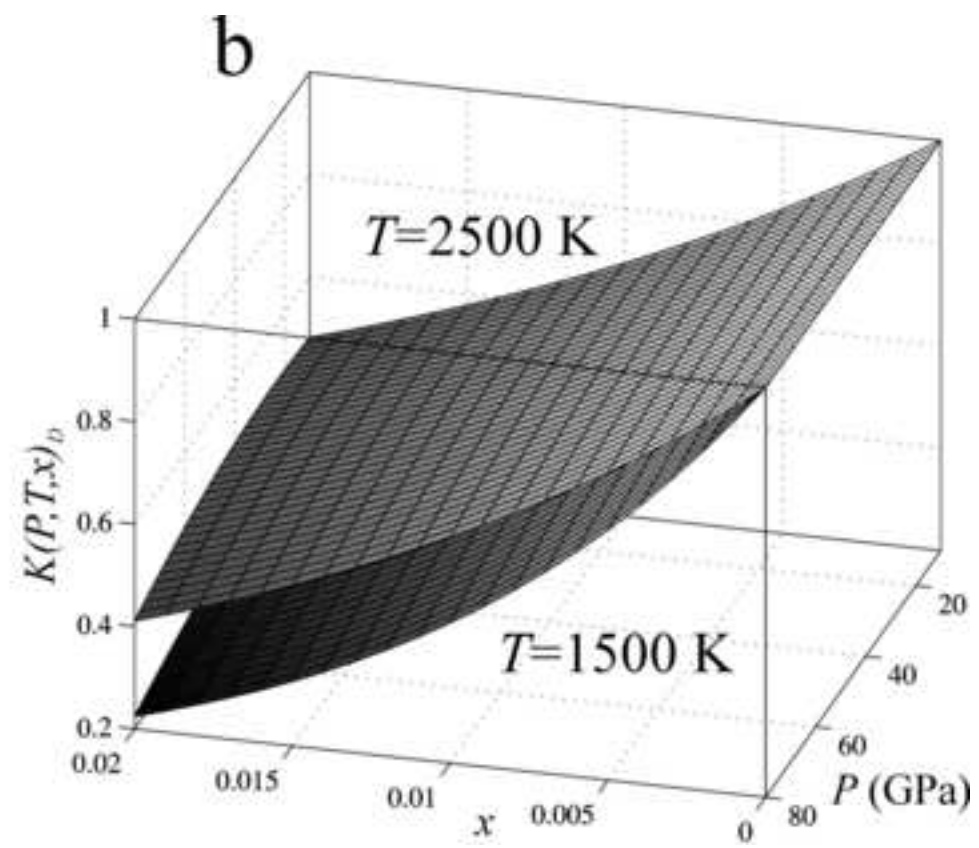
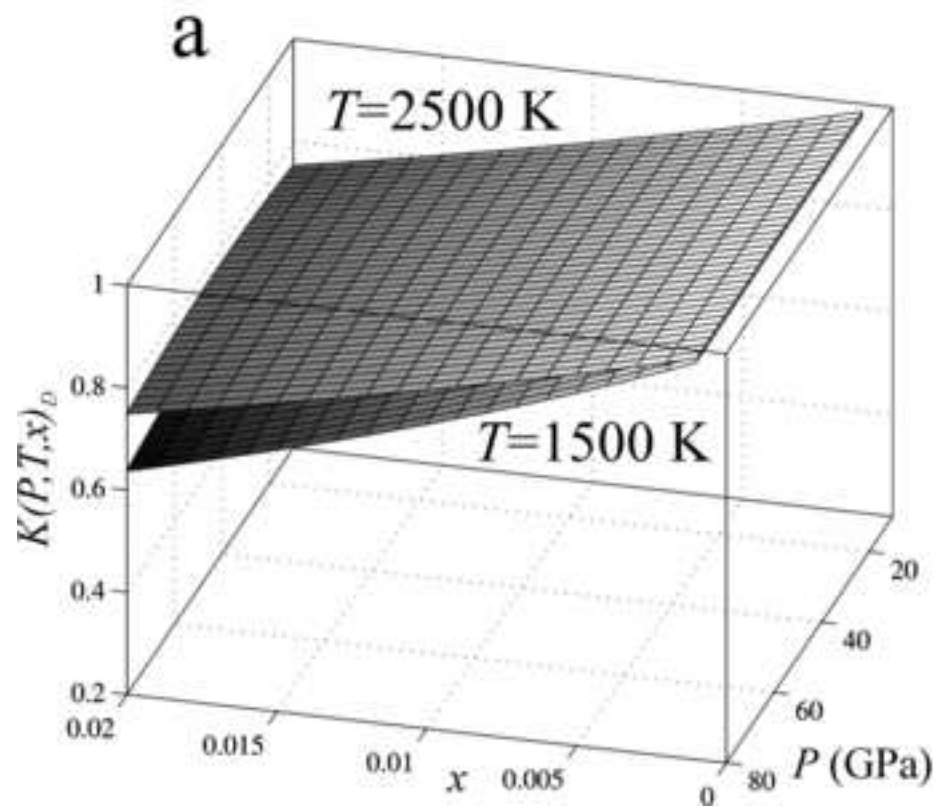
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**Table 4.**  $\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$  as a function of  $BWC$  (ppm) for the two H-incorporation models. Bold: reference values.

<b>MSWV</b>		
$BWC$ (ppm)	$\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ BSE model	$\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ LM model
100	0.987	0.988
300	0.962	0.965
<b>800</b>	<b>0.906</b>	<b>0.913</b>
<b>1500</b>	<b>0.836</b>	<b>0.848</b>
2000	0.791	0.806
2500	0.749	0.767
3000	0.711	0.731
<b>MSWA</b>		
$BWC$ (ppm)	$\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ BSE model	$\langle {}_{BWC}K_{D,H_2O}^{pe/pvk} \rangle$ LM model
100	0.965	0.968
300	0.899	0.908
<b>800</b>	<b>0.759</b>	<b>0.780</b>
<b>1500</b>	<b>0.610</b>	<b>0.638</b>
2000	0.529	0.559
2500	0.462	0.494
3000	0.408	0.439

Figure 1 a,b  
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**Figure 2**  
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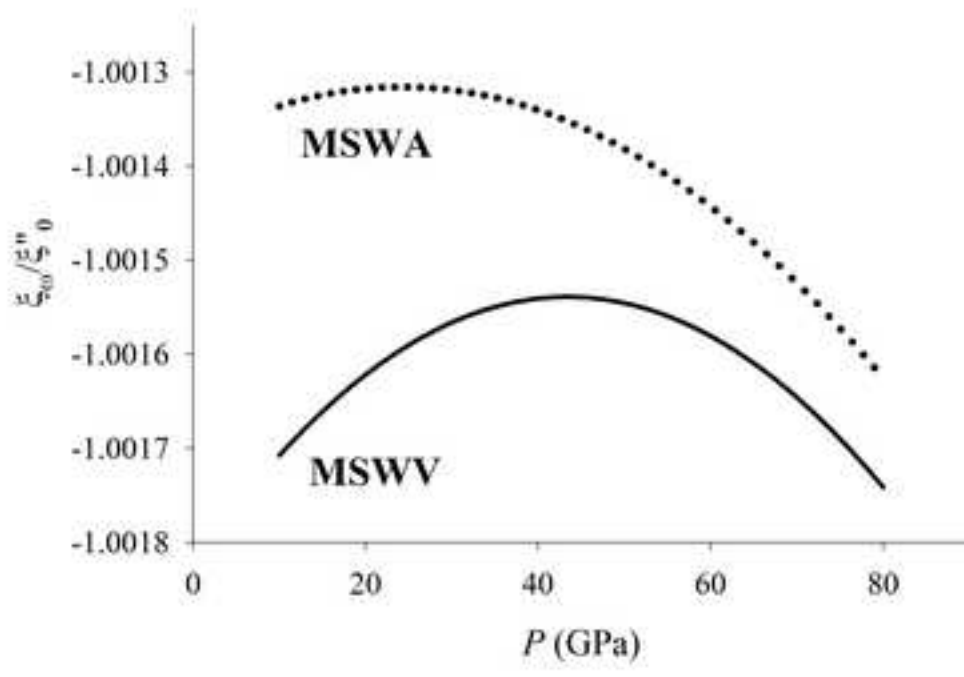


Figure 3 a,b  
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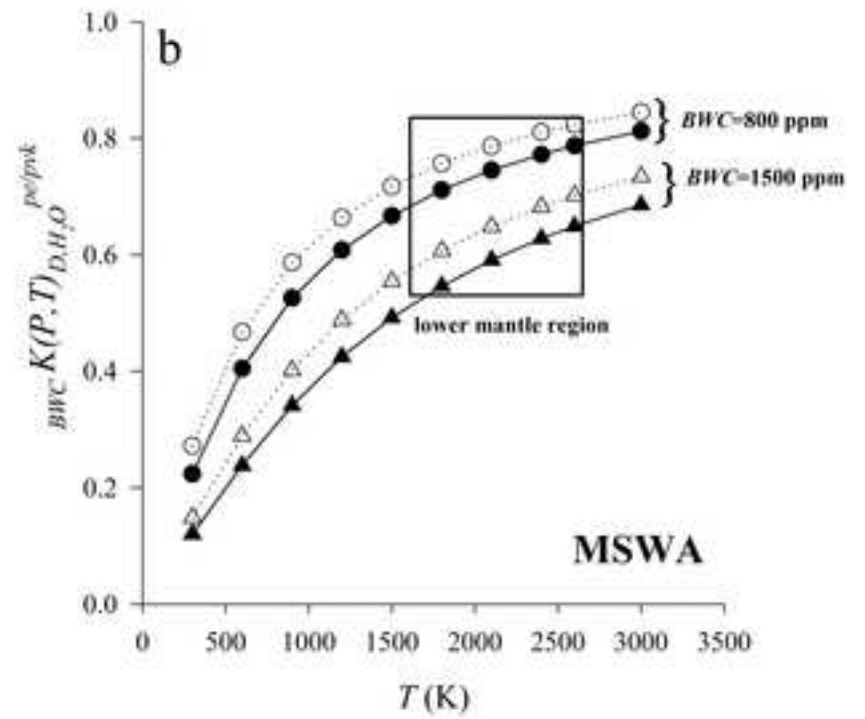
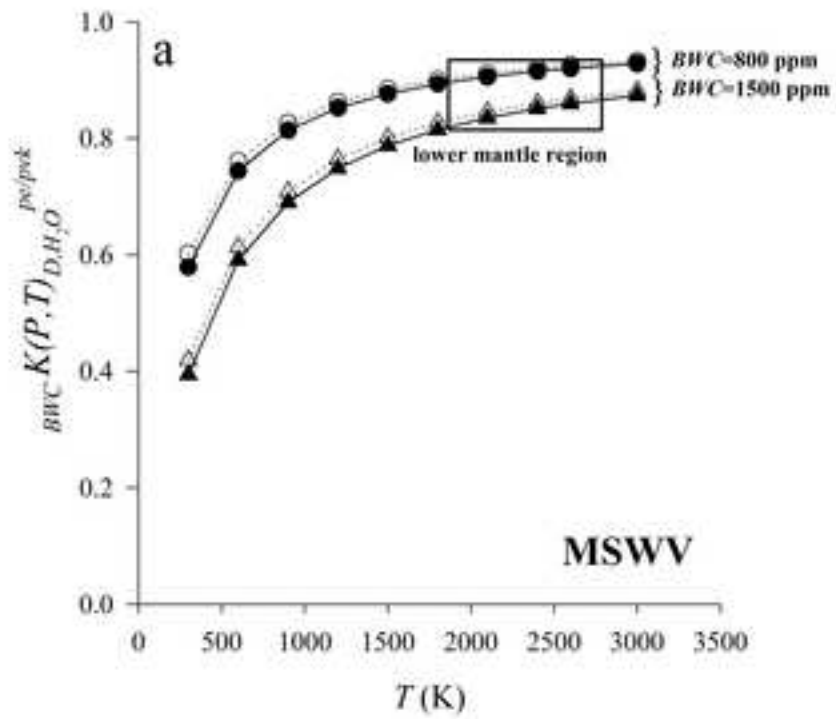


Figure 4  
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