# High-efficiency deflection of high energy protons due to channeling along the $\langle 110\rangle$ axis of a bent silicon crystal 

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## ABSTRACT

A deflection efficiency of about $61 \%$ was observed for $400 \mathrm{GeV} / \mathrm{c}$ protons due to channeling, most strongly along the $\langle 110\rangle$ axis of a bent silicon crystal. It is comparable with the deflection efficiency in planar channeling and considerably larger than in the case of the $\langle 111\rangle$ axis. The measured probability of inelastic nuclear interactions of protons in channeling along the $\langle 110\rangle$ axis is only about $10 \%$ of its amorphous level whereas in channeling along the (110) planes it is about $25 \%$. High efficiency deflection and small beam losses make this axial orientation of a silicon crystal a useful tool for the beam steering of high energy charged particles.
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## 1. Introduction

In the last twenty years, channeling has been exploited for steering [1], collimation [2-4] and extraction [2,5-7] of relativistic beams in circular accelerators, as well as splitting and focusing of extracted beams [8]. In the last decade, a significant boost to the research on particle-crystal interactions was provided by the fabrication of uniformly bent crystals with thickness along the beam direction suitable for experiments at high-energy. The novel gen-

[^0]eration of crystals has demonstrated the capability of efficiently steering positively charged $[9,10]$ particle beams and to observe the deflection of negatively charged particle beams [11,12]. As well as efficient deflection, channeling has been shown to modify the probability of incoherent interactions with atomic nuclei with respect to an amorphous material of the same length [13]. In particular, the use of bent crystals as a primary collimator has been demonstrated to reduce the beam losses in the SPS proton synchrotron at CERN [14-16], leading to the installation of two bent crystals in the LHC collider [17]. The crystals installed in the LHC were successfully tested and shown to reduce the beam losses in the LHC ring with $6.5 \mathrm{TeV} / \mathrm{c}$ protons [18].

As a charged particle traverses a crystal with a small angle with respect to one of the main crystallographic axes，the particle mo－ tion is governed by the potential of the atomic strings averaged along the axis［19］，i．e．the particle is subject to axial channel－ ing（AC）．The maximum angle between the particle incident angle and the crystal axis，for which channeling occurs is called criti－ cal angle for channeling $\psi_{a c}=\left(4 Z e^{2} / p \beta d\right)$［19］，where $d$ is the distance between neighboring atoms in the atomic string，$p \beta$ the particle momentum－velocity，$Z$ the atomic number of the crys－ tal atoms and $e$ the elementary charge．For a silicon crystal，$\psi_{a c}$ is almost three times larger than the critical angle for channel－ ing between atomic planes，i．e．planar channeling（PC）［20］．How－ ever，because the potential barrier separating the axial channels formed by neighboring atomic strings is rather low，the fraction of particles confined within a single axial channel is limited．As an example，for a silicon crystal，such a potential barrier is $\sim 6 \mathrm{eV}$ for the $\langle 110\rangle$ direction and only 1 eV for the $\langle 111\rangle$ ．If a particle under AC has a transverse energy slightly higher than the poten－ tial well barrier，particles interacting with a bent crystal may be deflected by the multiple scattering on the atomic strings toward the bending direction，increasing the efficiency of AC．Indeed，as soon as a particle penetrates the crystal，the position of scatter－ ing centers shifts，causing the subsequent random scattering with atomic strings to acquire a preferential direction．Such an effect was experimentally demonstrated for positively $[10,21]$ and nega－ tively［12］charged particles．

As predicted in［22］high deflection efficiency and small beam losses due to inelastic interactions may be achieved using the axial channeling，most strongly along the $\langle 110\rangle$ axis of a silicon crystal． Despite that fact，experimental measurements on $A C$ are limited to studies of the deflection efficiency of $400 \mathrm{GeV} / \mathrm{c}$ protons interacting with a 〈111〉 silicon crystal［10，12，21］，and measurement of the inelastic nuclear interaction（INI）frequency under AC was observed only for $15 \mathrm{GeV} / \mathrm{c}$ pions interacting with germanium crystals［23， 24］．

In this paper，we experimentally investigate the deflection effi－ ciency and the inelastic interaction frequency of $400 \mathrm{GeV} / \mathrm{c}$ protons interacting with $\langle 111\rangle$ and $\langle 110\rangle$ bent silicon crystals under axial channeling at the H8 external line of the SPS at CERN．

## 2．AC mechanism

Charged particles interacting with an aligned crystal under AC are mainly deflected by two phenomena，hyperchanneling［25］and the randomization of transverse momenta of the particles because of multiple scattering by atomic strings［26］．Hyperchanneling con－ sists in the confinement of the particle trajectory between the po－ tential well barriers separating neighboring atomic planes．Due to the low potential barrier，such a phenomenon is possible only for a few percent of the incident particles．On the contrary，when parti－ cles scatter on atomic strings，the deflection due to the randomiza－ tion of transverse particle momentum affects all the particles not under hyperchanneling and is possible if the crystal bending angle $(\alpha)$ is lower than a characteristic value $\alpha_{t s}$［27］
$\alpha<\alpha_{t s}=\frac{2 R \psi_{a c}^{2}}{l_{0}}$
where $R$ is crystal bending radius，$l_{0}=4 /\left(\pi^{2} n d R_{a} \psi_{a c}\right)$ the min－ imum encounter length between the incident particle and a nu－ cleus，$n$ being the concentration of atoms in the crystal and $R_{a}$ the atomic screening radius．

Although Eq．（1）proved to be a good condition for the observa－ tion of the particle deflection due to incoherent scattering［10，12， 21］，it does not furnish an estimate of the best crystal length at a

Table 1
Parameters of the $\langle 111\rangle$ and $\langle 110\rangle$ bent Si crystals，with $R$ the crystal bending radius，$L$ the crystal length along the beam direction，$\alpha_{p l}$ the channeling mean de－ flection angle．

|  | $\langle 111\rangle$ | $\langle 110\rangle$ |
| :--- | :--- | :--- |
| Plane | $(1 \overline{1} 0)$ | $(1 \overline{1} 0)$ |
| Axis | $\langle 111\rangle$ | $\langle 110\rangle$ |
| $L(\mathrm{~mm})$ | $1.941 \pm 0.002$ | $1.881 \pm 0.002$ |
| $R(\mathrm{~m})$ | $32 \pm 2$ | $35 \pm 2$ |
| $\alpha_{p l}(\mu \mathrm{rad})$ | $63 \pm 1$ | $54 \pm 1$ |

fixed bending angle．A useful parameter introduced to account for the maximum crystal length for efficient particle steering at the full bending angle $\alpha=L / R$ is the relaxation length $l_{r}$［21］，i．e．the length within which the fraction of particles in the $A C$ regime are reduced to $1 / e$ and escape from AC to skew planes．In order to ef－ ficiently deflect under AC a crystal has to fulfill the inequality［21］
$L<l_{r}$
Up to now，an analytic equation for the calculation of $l_{r}$ does not exist．The dependence of the $l_{r}$ on $R$ was worked out only for a $400 \mathrm{GeV} / \mathrm{c}$ proton beam interacting with a＜111〉 Si crystal［21］ and included the incoherent scattering on nuclei and electrons．

## 3．Experimental measurements

The experimental setup was based on a particle telescope［28］， consisting of ten planes of silicon microstrip sensors，arranged as five pairs，each measuring two orthogonal coordinates，with an active area of $3.8 \times 3.8 \mathrm{~cm}^{2}$ ．The telescope provided excellent angular and spatial resolution for measuring the trajectories of incident and outgoing particles．The apparatus had a long base－ line，of approximately 10 m in each arm，and achieved an angular resolution in the incoming arm of $2.5 \mu \mathrm{rad}$ and a total angular resolution on the difference of the two arms of $5.2 \mu \mathrm{rad}$ ，with per－ formance limited by multiple scattering in the sensor layers．The crystal was mounted on a high－precision goniometer with an an－ gular resolution of about $1 \mu \mathrm{rad}$ ．This instrument allowed three degrees of freedom，one linear and two rotational movements，to align the crystal along either the horizontal or vertical directions． Two pairs of scintillators were placed after the target outside the beampipe in order to measure the secondary particles produced by the nuclear interactions of protons with the silicon crystals．Pre－ alignment of the samples was achieved by means of a laser system parallel to the beam direction．

The targets were two silicon crystals produced according to the method described in Refs．［29－31］．The crystals were mounted on mechanical holders that impart a controlled deformation to the primary and the anticlastic curvatures［5，32］．The crystal param－ eters are reported in Table 1．Both the crystals have a $\sim 2 \mathrm{~mm}$ length and the same bent $\langle 1 \overline{1} 0\rangle$ axis orthogonal to the beam di－ rection．Therefore，both crystals make use of a（150）bent plane for PC．However，the bent axes parallel to the beam direction are dif－ ferent，being respectively $\langle 111\rangle$ and $\langle 110\rangle$ ．As a consequence the use of such crystals allows comparison of the AC features for two different crystal axes under the same experimental condition．The crystal torsion due to the mechanical holder was compensated in the data analysis for both the crystals［33］．

The INI frequency for a particle interacting with a crystal un－ der AC（ $n_{a c}$ ）can be expressed in units of the INI frequency for a particle interacting with an amorphous material $\left(n_{a m}\right)$ ．In the experiment，we tagged as nuclear interacting particles（ $N_{i n i}$ ）the incoming particles that interact with the crystals and produced a signal in both the scintillators．Subtracting the background events that produce a coincidence in the scintillators（ $N_{b g, i n i}$ ）from the


Fig. 1. Potential averaged along the $\langle 111\rangle$ axis of a silicon crystal. The directions of the (110) and (211) planes are shown.


Fig. 2. Potential averaged along the $\langle 110\rangle$ axis of a silicon crystal. The directions of the (111) planes are shown.
measurement ( $N_{i n i}$ ) and dividing by the events under misaligned condition minus the background events ( $N_{a m, i n i}-N_{b g, i n i}$ ), we obtain the INI frequency ( $n$ ) for the particles under AC:
$n=\frac{N_{i n i}-N_{b g}}{N_{a m}-N_{b g}}$
Firstly, both the crystals were oriented under PC in order to measure the efficiency $\left(\epsilon_{p l}\right)$ and the mean deflection angle $\left(\alpha_{p l}\right)$. The particles with an incident angle below $2 \mu \mathrm{rad}$ with respect to the ( $1 \overline{1} 0$ ) bent plane were analyzed. The maximum deflection efficiency and the average deflection angle under PC are $83 \pm 1 \%$ and $63 \pm 1 \mu \mathrm{rad}$ for the $\langle 111\rangle$ crystal, $82 \pm 1 \%$ and $54 \pm 1 \mu \mathrm{rad}$ for the $\langle 110\rangle$ crystal. Since the bending radii ( $R$ ) for the $\langle 111\rangle$ $(32 \pm 2 \mathrm{~m})$ and $\langle 110\rangle(35 \pm 2 \mathrm{~m})$ crystals are much greater than


Fig. 3. Experimental (a. and c.) and simulated (b. and d.) distributions of the horizontal and vertical deflection angles of $400 \mathrm{GeV} / \mathrm{c}$ protons interacting with the $\langle 111\rangle$ (a. and b.) and $\langle 110\rangle$ (c. and d.) crystals.

Table 2
The experimental and simulated deflection efficiency ( $\epsilon_{a c}$ ) axial channeling along the $\langle 111\rangle$ and $\langle 110\rangle$ silicon crystal axes.

|  | $\langle 111\rangle$ |  |  | $\langle\mathbf{1 1 0 \rangle}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: |
|  | Experiment | Simulation |  | Experiment | Simulation |  |  |  |
| $\epsilon_{a c}$ | $22 \pm 2$ | $24 \pm 2$ |  | $61 \pm 2$ | $67 \pm 2$ |  |  |  |

the 0.7 m critical bending radius $\left(R_{c}\right)$ at $400 \mathrm{GeV} / \mathrm{c}$ [20], the minimal bending radius for which channeling is possible, the deflection efficiency under PC is expected to be the same for the two crystals [12]. The deflection efficiency under PC was evaluated as described in Ref. [34].

After the channeling was demonstrated under PC, the crystal was oriented in order to observe AC, i.e., with the crystal axis parallel to the particle incoming direction. In order to investigate AC , both the crystals have to fulfill the inequalities in Eqs. (1) and (2). The parameter $l_{r}$ was estimated as $\sim 2.5 \mathrm{~mm}$ for $R=32$ and $\sim 3.7$ for $R=35$ [21]. Although the $\langle 111\rangle$ axis was used for the estimation, we expect a similar or better behavior for the $\langle 110\rangle$ axis, since the potential well depth is similar and the potential well is wider (see Figs. 1 and 2). The parameter $\alpha_{t s}$ is $\sim 600 \mu$ rad for the $\langle 111\rangle$ crystal and $\sim 800 \mu \mathrm{rad}$ for the $\langle 110\rangle$. Because $\alpha_{t s} \gg \alpha_{p l}$ and $L<l_{r}$ for both the crystals, we expect a high-efficiency beam deflection through AC for both of them.

The distribution of particle deflection angle after the interaction with the two crystals is shown in Fig. 3. Table 2 shows the deflection efficiency under AC. The particles with an incident angle below $3 \mu \mathrm{rad}$ with respect to the bent axis of the two crystals were analyzed, i.e. with $\sqrt{\theta_{x 0}^{2}+\theta_{y 0}^{2}}<\Theta$ where $\theta_{x 0}$ and $\theta_{y 0}$ are the horizontal and vertical particle incident angle with respect to the crystal axis orientation. The deflection efficiency $\epsilon_{a c}$ was evaluated as the fraction of particles in the circle centered on the mean horizontal deflection with radius $11 \mu \mathrm{rad}$ for the $\langle 110\rangle$ crystal and $15 \mu \mathrm{rad}$ for the $\langle 110\rangle$ crystal. The deflection efficiency was $22 \pm 2 \%$ for the $\langle 111\rangle$ and $61 \pm 2 \%$ for the $\langle 110\rangle$.


Fig. 4. Distributions of horizontal (a. and c.) and vertical (b. and d.) deflection angles for a narrow fraction of the $400 \mathrm{GeV} / \mathrm{c}$ proton beam after the passage through the $\langle 111\rangle$ (a. and b.) and $\langle 110\rangle$ (c. and d.) silicon crystals. Continuous blue lines are the experimental data, red dashed lines are the Geant 4 simulations. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 4 shows the distribution of the horizontal deflection angle for a $400 \mathrm{GeV} / \mathrm{c}$ proton beam interacting with the $\langle 111\rangle$ and $\langle 110\rangle$ silicon crystals. The particle with an incident angle below $3 \mu \mathrm{rad}$ are analyzed. The efficiency of one side deflection is $97 \%$ for the $\langle 111\rangle$ and $98 \%$ for the $\langle 110\rangle$ axis orientations. For both crystals the particle distributions are symmetric on the vertical plane and skewed to positive values on the horizontal plane, i.e. the bent plane. Although all the particles are initially subject to AC a consistent fraction is captured by the skew planes that intersect the main axis. For the crystal offering the $\langle 111\rangle$ axis the two symmetric tails that belong to the (110) family of planes at $60^{\circ}$ from the main (1 $1 \overline{1} 0$ ) plane (see Figs. 1 and 4), leading the particles captured by them to be deflected at an angle much lower than the full bending angle. For the crystal offering the $\langle 110\rangle$ axis the angle between the two symmetric (111) planes and the main (1 $\overline{1} 1$ ) plane is only $35.26^{\circ}$, causing the captured particles to be deflected at an angle similar to the main bending angle (see Figs. 2 and 4). As a consequence the deflection efficiency $\epsilon_{a c}$ is higher for the $\langle 110\rangle$ crystal than for the $\langle 111\rangle$.

The INI frequency was measured for the axial and for amorphous (AM) orientations of the crystals. Fig. 5 shows the INI frequency normalized to the AM condition as a function of an angular range $\pm \Theta$ around the best $A C$ position for both the crystals, i.e. $\sqrt{\theta_{x o}^{2}+\theta_{y o}^{2}}<\Theta$. Particles under AM experience the same INI frequency independently of $\Theta$, because in such a case the crystal acts as an amorphous material. On the contrary, the INI frequency for AC strongly depends on $\Theta$. Indeed, as soon as the integration angle grows, the fraction of particles under AC diminishes in the beam, leading to the growing of the average INI frequency.

The interaction frequency under PC is always higher than for AC. Indeed, as predicted in [22], the particles under AC impinge on the strong electromagnetic field of the atomic rows without approaching close to the nuclei until they are aligned with respect to the crystal axis within one $\psi_{a c}$. Since $\psi_{a c} \gg \psi_{p c}$ for both


Fig. 5. Measured inelastic nuclear interaction (INI) frequency of $400 \mathrm{GeV} / \mathrm{c}$ protons interacting with the $\langle 111\rangle$ and $\langle 110\rangle$ crystals as a function of the angular region around the (110) planar channeling (black dash-dotted line, 1), the $\langle 111\rangle$ axial channeling (blue dashed line, 2) and $\langle 110\rangle$ (red continuous line, 3 ) orientations. The values are normalized to the INI frequencies for the amorphous crystal orientation. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
$\langle 111\rangle$ and $\langle 110\rangle$ axes ( $U_{0, a c} \sim 100 \mathrm{eV}$ for $\langle 111\rangle$ and $\langle 110\rangle$ axes and $U_{0, p c} \sim 20$ for ( $1 \overline{1} 0$ ) plane), the INI frequency under AC remains lower than the INI frequency under PC for higher incident angles, resulting in a net reduction of the INI frequency for the whole incident beam.

Whilst the potential well depth for $\langle 111\rangle$ and $\langle 110\rangle$ axes are similar, the shapes of the potential well are different. Indeed, the potential well for the $\langle 110\rangle$ axis is much wider than the potential well for the $\langle 111\rangle$ axis (see Figs. 2 and 1). As consequence, the fraction of particles captured in the skew planes is $\sim 45 \%$ for $\langle 111\rangle$ and $\sim 15 \%$ for the $\langle 110\rangle$. The INI frequency under AC is $\sim 0.30$ for the $\langle 111\rangle$ axis and $\sim 0.10$ for the $\langle 110\rangle$ axis for particles with $\sqrt{\theta_{x o}^{2}+\theta_{y o}^{2}}<5 \mu \mathrm{rad}$ (see Fig. 5).

The distribution of the particle deflection angle for the $\langle 110\rangle$ axis orientation resembles the distribution obtainable via multiple volume reflection in one crystal (MVROC) at high-energy [35] with a crystal of similar features [36]. Therefore, the $98 \%$ efficiency of one side deflection for the $\langle 110\rangle$ axis orientation is comparable to the $\sim 87 \%$ efficiency for the MVROC case [36]. However, because of the trajectories of the particles in the crystal under AC and MVROC are different, the two orientational coherent effects have different ranges of applicability. Since the MVROC is a sequence of volume reflections from various planes in a crystal, one would expect that the INI frequency might be the averaged sum of the contribution of each plane. Since the INI frequency under volume reflection is similar to the amorphous case [13], the MVROC effect does not lower the INI frequency with respect to the amorphous case, as the AC does. On the other side, the AC has a very sharpen angular acceptance, because particle has to be aligned with an angle lower than the critical angle with respect to the axis direction, while particles in a wide angular range determined by the geometric properties of the crystal are subject to MVROC.

## 4. Monte Carlo simulations

The investigation of the trajectories inside the crystals was carried out by means of the Geant4 Monte Carlo toolkit [37]. The experimental setup at the H8-SPS area is reproduced in the simulation in order to take into account the error due to the finite resolution of the telescope. Channeling is implemented by including DYNECHARM++ [38] and ECHARM [39] into the Geant4 channel-
ing package [40]. Simulations of the distribution of the deflection angle in Figs. 3 and 4.

The distribution of the deflection angles reproduces the experimental results. Indeed, the spot of the particles deflected by the AC and the tails filled by the particles captured by skew planes are visible. Table 2 reports the simulation results for the deflection efficiency under AC. The efficiency is slightly higher than the experimental results for both the crystals. As a consequence, the INI frequency of the simulation is slightly lower than the experimental results.

The good agreement between the Geant4 simulations and the experimental data allows investigation of the dynamics of the interaction with the Monte Carlo approach. Since the simulations with Geant4 take into consideration the whole experimental setup and the contribution of the multiple scattering on the beam line elements to the final results, a different Monte Carlo approach can be used to evaluate the deflection efficiency under AC under ideal conditions. Therefore, Monte Carlo simulations without the experimental setup were carried out. Simulations show that the deflection efficiencies may reach values of about ( $39 \pm 3$ )\% and ( $79 \pm 3$ )\% for the $\langle 111\rangle$ and $\langle 110\rangle$ axial orientations of the silicon crystals, respectively, for particles with $\sqrt{\theta_{x o}^{2}+\theta_{y o}^{2}}<3 \mu \mathrm{rad}$.

## 5. Conclusions

In summary, we compared the deflection efficiency and INI frequency under $A C$ of $\langle 111\rangle$ and $\langle 110\rangle$ axes. The experiment confirms the theoretical predictions proposed in [22] and paves the way to the use of AC as an efficient manipulator of charged particle beams.

The AC with $\langle 110\rangle$ and $\langle 111\rangle$ silicon crystals causes $9 \%$ of the particles to be one side deflected. The particles captured by the skew planes ( $\sim 15 \%$ ) for the $\langle 110\rangle$ axis acquire a deflection angle similar to $\alpha$, while the two most strongly acting (110) planes of the $\langle 111\rangle$ axis cause a considerable fraction ( $\sim 45 \%$ ) of the particles to be deflected at an angle lower than $\alpha$ but $>0$. Moreover, simulations without the experimental setup show an ( $79 \pm 3$ )\% deflection efficiency for the $\langle 110\rangle$ axis if we consider only the particle-crystal interaction.

The measurement allowed to clearly establish that the INI frequency for particles under AC is significantly lower than for particles under PC. Moreover, we observed that the INI frequency for particles under AC for a $\langle 110\rangle$ crystal is three times lower than for a $\langle 111\rangle$ crystal. The experimental measurements were systematically compared with Monte Carlo simulations worked out via the Geant4 toolkit. The simulations reproduced the distributions of deflection angle for both crystals, confirming the understanding of the physics behind AC. Thanks to its deflection efficiency and the low INI frequency, we experimentally demonstrated that AC along the most effective $\langle 110\rangle$ axis of a bent silicon crystal is a good candidate for beam manipulation at high energy, since AC guarantees a high deflection efficiency and a very low INI frequency despite of the narrow angular acceptance.

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