## Measurements of Born cross sections of $\boldsymbol{e}^{+} \boldsymbol{e}^{-} \rightarrow D_{s}^{*+} \boldsymbol{D}_{s J}^{-}+$c.c.

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(Received 7 June 2021; accepted 4 August 2021; published 27 August 2021)
The Born cross sections are measured for the first time for the processes $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}+$c.c. and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}+$c.c. at the center-of-mass energy $\sqrt{s}=4.600 \mathrm{GeV}, 4.612 \mathrm{GeV}$,

[^0]$4.626 \mathrm{GeV}, 4.640 \mathrm{GeV}, 4.660 \mathrm{GeV}, 4.68 \mathrm{GeV}$, and 4.700 GeV , and for $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}+\mathrm{c.c}$. at
$\sqrt{s}=4.660 \mathrm{GeV}, 4.680 \mathrm{GeV}$, and 4.700 GeV , using data samples collected with the BESIII detector at the
BEPCII collider. No structures are observed in cross-section distributions for any of the processes.

DOI: 10.1103/PhysRevD.104.032012

## I. INTRODUCTION

The $D_{s}^{+}$meson and its excited states are formed from $c \bar{s}$ quark-antiquark pairs. Throughout the paper, chargeconjugation is implied. Three excited $P$-wave states above the $D^{(*)} K$ threshold have been observed at the CLEO, $B A B A R$, Belle, and BESIII experiments [1-9]. They are referred to as $D_{s 0}^{*}(2317)^{+}, D_{s 1}(2460)^{+}$, and $D_{s 1}(2536)^{+}$, and are assigned the spin-parity quantum numbers $J^{P}$ as $0^{+}, 1^{+}$, and $1^{+}$, respectively [10], matching the predictions from the heavy-quark effective theory [11,12]. Their masses are measured to be $(2317.8 \pm 0.5) \mathrm{MeV} / c^{2}$, $(2459.5 \pm 0.6) \mathrm{MeV} / c^{2}$, and $(2535.11 \pm 0.06) \mathrm{MeV} / c^{2}$, respectively [10]. For the cases of the $D_{s 0}^{*}(2317)^{+}$and $D_{s 1}(2460)^{+}$states, these values are significantly lower than the theoretical predictions for the charmed-strange mesons in the $P$-wave doublet [13]. The low-mass puzzle of the $D_{s 0}^{*}(2317)^{+}$and $D_{s 1}(2460)^{+}$mesons has inspired various exotic explanations, including tetraquark states [14-19], $D^{(*)} K$ molecule states [20-24], or mixtures of $c \bar{s}$ and $D^{(*)} K$ states [25]. Further experimental measurements are needed in order to elucidate their structures.

Moreover, several charmoniumlike $Y$ states with $J^{P C}=1^{--}$lying above the open-charm threshold have been discovered, such as the $Y(4260)$ [26-28], $Y(4360)$ [29,30], and $Y(4660)$ [30]. Since $Y$ states could decay to open-charm meson pairs, exclusive cross section measurements of open-charm meson pair production in $e^{+} e^{-}$ collisions will provide further insight on the internal structures of these charmoniumlike resonances. Measurements of $e^{+} e^{-} \rightarrow D_{s}^{(*)+} D_{s}^{(*)-}$ cross sections were performed at Belle [31], BABAR [32], and CLEO [33]. BESIII extended these studies to higher excited states by measuring the cross sections of $e^{+} e^{-} \rightarrow D_{s}^{+} D_{s 1}(2460)^{-}$ and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}$[34] with an integrated luminosity of $859 \mathrm{pb}^{-1}$ at center-of-mass (c.m.) energies $\sqrt{s}$ from 4.467 to 4.600 GeV . In this paper, we report new measurements of the Born cross sections of the processes $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}, e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}$, and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$at BESIII at $\sqrt{s} \geq 4.6 \mathrm{GeV}$, and search for possible vector charmoniumlike states.

## II. DETECTOR, DATA SAMPLES, AND MONTE CARLO SIMULATIONS

The BESIII detector located at the Beijing Electron Positron Collider (BEPCII) [35] is a major upgrade of the BESII experiment at the BEPC accelerator [36]. The
cylindrical core of the BESIII detector consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time of flight system (TOF), and a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muonidentifier modules interleaved with steel. The acceptance of charged particles and photons is $93 \%$ over the $4 \pi$ solid angle. The charged-particle momentum resolution at $1 \mathrm{GeV} / c$ is $0.5 \%$, and the $\mathrm{d} E / \mathrm{d} x$ resolution is $6 \%$ for the electrons from Bhabha scattering. The EMC measures photon energies with a resolution of $2.5 \%(5 \%)$ at 1 GeV in the barrel (end-cap) region. The time resolution of the TOF barrel part is 68 ps . The time resolution of the end cap part was 110 ps before 2015; at that time the end cap TOF system was upgraded with multi-gap resistive plate chambers, and the time resolution improved to 60 ps .

The results reported in this article for the processes $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}$and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}$are determined from seven energy points from 4.600 to 4.700 GeV , where the data at 4.600 GeV were accumulated in 2014, and the remainder in 2020. At energies of 4.660 GeV and above, the data are also used to study $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$. Table I lists the individual c.m. energies and their integrated luminosities.

The GEANT4-based [37] Monte Carlo (MC) simulation framework bOOST [38], which includes the description of the detector geometry and response, is used to produce large simulated event samples. These samples are exploited to optimize the event selection criteria, to determine the detection efficiency, and to evaluate the initial-state radiation (ISR) correction factor $(1+\delta)$. Exclusive phase space (PHSP) MC samples of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}$, $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}, \quad$ and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$ are generated using ККМС [39-41], where the effects of ISR and beam-energy spread are taken into account. Generic MC samples of open-charm processes are used to estimate background contributions. The known decay modes are modeled with BESEVTGEN [42,43], using branching fractions taken from Particle Data Group (PDG) [10], while the unknown decays of charmonium states are modeled using LundCharm [44]. Final-state radiation effects are simulated by the pHOTOS [45] package. In the signal MC samples, $D_{s}^{*+}$ are simulated to decay into $\gamma D_{s}^{+}$, with the subsequent decay of $D_{s}^{+}$into $K^{+} K^{-} \pi^{+}$, while the $D_{s 0}^{*}(2317)^{-}, D_{s 1}(2460)^{-}$, and $D_{s 1}(2536)^{-}$mesons decay inclusively. A $P$-wave model and a Dalitz plot decay model

TABLE I. Summary of the measured Born cross sections for $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}, e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}$, and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$. Listed in the table are the integrated luminosity $\mathcal{L}_{\text {int }}$, the signal efficiency $\epsilon$ from signal MC sample, the number of fitted $D_{s, J}^{-}$signal events $N_{\text {fit }}$, the upper limit at $90 \%$ C.L. on the number of fitted $D_{s J}^{-}$signal yields $N_{\mathrm{U} . \mathrm{L} .}$, the ISR radiative correction factor $(1+\delta)$, the statistical signal significance, and the measured Born cross section $\left(\sigma_{B}\right)$ and its upper limit ( $\sigma_{B}^{\text {U.L. }}$ ) at $90 \%$ C.L.

| $\sqrt{s}(\mathrm{GeV})$ | $\mathcal{L}_{\text {int }}\left(\mathrm{pb}^{-1}\right)$ | $\epsilon(\%)$ | $N_{\text {fit }}$ | $N_{\text {U.L. }}$ | $(1+\delta)$ | Significance | $\sigma_{B}\left(\sigma_{B}^{\text {U.L. }}\right)(\mathrm{pb})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}+$c.c. |  |  |  |  |  |  |  |
| 4.600 | 586.89 | 14.1 | $25.7{ }_{-18.3}^{+19.1}$ | 52.0 | 0.821 | $1.4 \sigma$ | $6.8_{-4.8}^{+5.0}(14.8)$ |
| 4.612 | 102.50 | 13.7 | $9.5{ }_{-7.8}^{+8.6}$ | 22.0 | 0.826 | $1.2 \sigma$ | $14.7{ }_{-12.0}^{+13.3}$ (34.7) |
| 4.626 | 511.06 | 13.7 | $62.9 \pm 18.8$ | $\ldots$ | 0.830 | $3.6 \sigma$ | $19.3 \pm 5.8 \pm 2.0$ |
| 4.640 | 541.37 | 13.8 | $20.8{ }_{-17.3}^{+18.1}$ | 46.4 | 0.834 | $1.2 \sigma$ | $6.0_{-5.0}^{+5.2}(14.1)$ |
| 4.660 | 523.63 | 13.9 | $20.0_{-17.2}^{+18.2}$ | 45.6 | 0.838 | $1.2 \sigma$ | $5.8{ }_{-5.0}^{+5.3}$ (14.1) |
| 4.680 | 1643.38 | 14.0 | $151.9 \pm 33.2$ | $\ldots$ | 0.845 | $4.9 \sigma$ | $13.9 \pm 3.0 \pm 1.4$ |
| 4.700 | 526.20 | 13.8 | $47.5_{-18.6}^{+19.5}$ | 73.6 | 0.849 | $2.7 \sigma$ | $13.7_{-5.4}^{+5.6}$ (21.4) |
| $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}+$c.c. |  |  |  |  |  |  |  |
| 4.600 | 586.89 | 14.1 | $107.6 \pm 17.8$ | $\ldots$ | 0.743 | $7.1 \sigma$ | $31.2 \pm 5.2 \pm 3.7$ |
| 4.612 | 102.50 | 13.7 | $15.88_{-7.0}^{+7.7}$ | 26.8 | 0.766 | $2.5 \sigma$ | $26.1_{-11.5}^{+12.8}$ (44.4) |
| 4.626 | 511.06 | 13.5 | $88.2 \pm 18.3$ | $\ldots$ | 0.783 | $5.6 \sigma$ | $29.1 \pm 6.0 \pm 2.6$ |
| 4.640 | 541.37 | 13.6 | $75.2 \pm 18.3$ | $\ldots$ | 0.796 | $4.7 \sigma$ | $22.8 \pm 5.6 \pm 2.3$ |
| 4.660 | 523.63 | 13.5 | $100.6 \pm 19.3$ | $\ldots$ | 0.811 | $6.1 \sigma$ | $31.1 \pm 6.0 \pm 2.7$ |
| 4.680 | 1643.38 | 14.0 | $339.0 \pm 35.0$ | $\ldots$ | 0.822 | $11.0 \sigma$ | $31.9 \pm 3.3 \pm 2.5$ |
| 4.700 | 526.20 | 13.7 | $103.4 \pm 20.2$ | $\ldots$ | 0.831 | $5.8 \sigma$ | $30.8 \pm 6.0 \pm 2.6$ |
| $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}+$c.c. |  |  |  |  |  |  |  |
| 4.660 | 523.63 | 13.8 | $35.0 \pm 11.5$ | $\ldots$ | 0.639 | $3.4 \sigma$ | $13.4 \pm 4.4 \pm 1.7$ |
| 4.680 | 1643.38 | 13.9 | $243.7 \pm 27.9$ | $\ldots$ | 0.706 | $10.1 \sigma$ | $26.9 \pm 3.1 \pm 2.3$ |
| 4.700 | 526.20 | 14.0 | $109.7 \pm 18.7$ | $\ldots$ | 0.753 | $7.0 \sigma$ | $35.1 \pm 6.0 \pm 3.0$ |

[46-48] are used to simulate $D_{s}^{*+} \rightarrow \gamma D_{s}^{+}$and $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}$, respectively.

## III. SELECTION CRITERIA

The candidate events of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}$, $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}, \quad$ and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$ are selected with a partial reconstruction method to obtain higher efficiencies. The $D_{s 0}^{*}(2317)^{-}, D_{s 1}(2460)^{-}$, and $D_{s 1}(2536)^{-}$signals are searched for in the recoil-mass spectrum of $D_{s}^{*+}$ candidates. The $D_{s}^{*+}$ candidates are reconstructed via $D_{s}^{*+} \rightarrow \gamma D_{s}^{+}$, while the $D_{s}^{+}$candidates are reconstructed via $D_{s}^{+} \rightarrow \phi \pi^{+}, \phi \rightarrow K^{+} K^{-}$and $D_{s}^{+} \rightarrow$ $\bar{K}^{* 0} K^{+}, \bar{K}^{* 0} \rightarrow K^{-} \pi^{+}$. Thus, there are three charged tracks from $D_{s}^{+}$decays and one additional photon candidate from $D_{s}^{*+} \rightarrow \gamma D_{s}^{+}$.

Each track must originate from the interaction point (IP), which means that the distance of the closest approach to the IP of each track is required to be within 10 cm in the beam direction and within 1 cm in the plane perpendicular to the beam direction. Additionally, each track must reside within the active region of the MDC , meaning that its polar angle $\theta$ must satisfy $|\cos \theta|<0.93$. The $\mathrm{d} E / \mathrm{d} x$ and

TOF information are used to perform particle identification (PID). Pion candidates are required to satisfy $\operatorname{Prob}(\pi)>$ $\operatorname{Prob}(K)$ and $\operatorname{Prob}(\pi)>0.001$, where $\operatorname{Prob}(\pi)$ and $\operatorname{Prob}(K)$ are the PID probabilities for a track to be a pion and kaon, respectively. Kaon candidates are required to satisfy $\operatorname{Prob}(K)>\operatorname{Prob}(\pi)$ and $\operatorname{Prob}(K)>0.001$. With these PID requirements, the probability of misidentifying a $K^{+}$as $\pi^{+}$or a $\pi^{+}$as $K^{+}$is below $3 \%$.

The photon candidates are selected from EMC showers that are not associated with charged tracks. The deposited energy is required to be larger than 25 MeV in the barrel EMC $(|\cos \theta|<0.8)$, or larger than 50 MeV in the end-cap EMC $(0.86<|\cos \theta|<0.92)$. To eliminate the showers from charged particles, the angle between the photon and the extrapolated impact point of any good charged track at the EMC front face must be larger than $20^{\circ}$. The timing of the shower is required to be within $[50,700] \mathrm{ns}$ after the reconstructed event start time to suppress noise and energy deposits unrelated to the event.

To reconstruct $D_{s}^{*+}$ mesons, two kaons, one pion, and one photon candidates are required. All the $K^{+} K^{-} \pi^{+}$in all combinations of $\gamma K^{+} K^{-} \pi^{+}$, which pass a vertex fit are kept. Mass-constrained fits to the nominal masses of $D_{s}^{+}$
and $D_{s}^{*+}(2 \mathrm{C})$ are performed, and the $\chi^{2}$ of this fit is required to be less than ten to suppress the backgrounds. To select $D_{s}^{+} \rightarrow \phi \pi^{+}, \phi \rightarrow K^{+} K^{-}$and $D_{s}^{+} \rightarrow \bar{K}^{* 0} K^{+}, \bar{K}^{* 0} \rightarrow$ $K^{-} \pi^{+}$submodes, the invariant masses of $K^{+} K^{-}$and $K^{-} \pi^{+}$ are required to satisfy $\left|M\left(K^{+} K^{-}\right)-m_{\phi}\right|<9 \mathrm{MeV} / c^{2}$ and $\left|M\left(K^{-} \pi^{+}\right)-m_{\bar{K}^{* 0}}\right|<84 \mathrm{MeV} / c^{2}$, respectively, where $m_{\phi}$ ( $m_{\bar{K}^{* 0}}$ ) is the nominal mass of the $\phi\left(\bar{K}^{* 0}\right)$ meson taken from the PDG [10].

## IV. MEASUREMENTS OF THE $\boldsymbol{e}^{+} \boldsymbol{e}^{-} \rightarrow D_{s}^{*+} \boldsymbol{D}_{s J}^{-}$

The recoil-mass distributions of $D_{s}^{*+}$ candidates from data samples at $\sqrt{s}=4.600 \mathrm{GeV}, 4.612 \mathrm{GeV}$, $4.626 \mathrm{GeV}, 4.640 \mathrm{GeV}, 4.660 \mathrm{GeV}, 4.680 \mathrm{GeV}$, and 4.700 GeV are shown in Fig. 1. To improve the recoil-mass resolution, the recoil mass of $D_{s}^{*+}$ is defined to be $M_{D_{s}^{*+}}^{\text {rec }}=M_{\gamma K^{+} K^{-} \pi^{+}}^{\text {recoil }}+M\left(\gamma K^{+} K^{-} \pi^{+}\right)-m_{D_{s}^{*+}}$, where $M_{\gamma K^{+} K^{-} \pi^{+}}^{\text {recil }}=\sqrt{\left(P_{\text {c.m. }}-P_{\gamma}-P_{K^{+}}-P_{K^{-}}-P_{\pi^{+}}\right)^{2}}$. Here
$P_{\text {c.m. }}, P_{\gamma}, P_{K^{+}}, P_{K^{-}}$, and $P_{\pi^{+}}$are the four-momenta of the initial $e^{+} e^{-}$system, the selected $\gamma, K^{+}, K^{-}$, and $\pi^{+}$, respectively, $M\left(\gamma K^{+} K^{-} \pi^{+}\right)$is the invariant mass of the $\gamma K^{+} K^{-} \pi^{+}$system, and $m_{D_{s}^{*+}}$ is the nominal mass of the $D_{s}^{*+}$ meson [10]. Clear signals are seen for the $D_{s 1}(2460)^{-}$at all of the energy points apart from 4.612 GeV , and are found for the $D_{s 1}(2536)^{-}$at $\sqrt{s}=4.660 \mathrm{GeV}$, 4.680 GeV , and 4.700 GeV , and for the $D_{s 0}^{*}(2317)^{-}$at $\sqrt{s}=4.626 \mathrm{GeV}$ and 4.680 GeV . Detailed studies of the generic MC samples with a generic event type analysis tool, TopoAna [49], indicate that there are no peaking backgrounds in the signal region. We considered possible contributions of processes such as $e^{+} e^{-} \rightarrow D_{s}^{+} \gamma D_{s J}^{-}$and $e^{+} e^{-} \rightarrow D^{0}\left(\rightarrow K^{-} \pi^{+}\right)$ $K^{+} \gamma D_{s 0}^{*}(2317)^{-}$by plotting the recoil-mass distributions for events in the $D_{s}^{*+}$ mass sidebands; no peaking structures were observed. An unbinned maximum-likelihood fit is performed to the $D_{s}^{*+}$ recoil-mass distributions to


FIG. 1. The recoil-mass distributions of $D_{s}^{*+}$ candidates from data samples at $\sqrt{s}=4.600 \mathrm{GeV}, 4.612 \mathrm{GeV}, 4.626 \mathrm{GeV}, 4.640 \mathrm{GeV}$, $4.660 \mathrm{GeV}, 4.680 \mathrm{GeV}$, and 4.700 GeV , respectively. The dots with error bars are data and the solid lines are the best fits. Clear $D_{s 1}(2460)^{-}$signals are observed at all of the energy points except for 4.612 GeV ; clear $D_{s 1}(2536)^{-}$signals are observed at $\sqrt{s}=4.660 \mathrm{GeV}, 4.680 \mathrm{GeV}$, and 4.700 GeV , and clear $D_{s 0}^{*}(2317)^{-}$signals are observed at $\sqrt{s}=4.626 \mathrm{GeV}$ and 4.680 GeV . The fitted results, together with the signal significances, are summarized in Table I. The fit quality of $\chi^{2} / n . d . f$. is presented in each plot, where $n . d . f$. stands for the number of degrees of freedom.
determine the signal yields of $D_{s J}^{-}$mesons. The signal probability density function is modeled according to a MC-derived signal shape, while the background is modeled with an ARGUS function [50]. The fitted results are summarized in Fig. 1 and Table I. The $D_{s 0}^{*}(2317)^{-}$signal significance of the combined data samples from all energy points is $6.9 \sigma$. The signal significances are determined by comparing the log-likelihood values with and without including a $D_{s J}^{-}$signal in the fit, taking the change in the number of degrees of freedom into account.

Since the statistical significances of $D_{s J}^{-}$signals at some energy points are less than $3 \sigma$, with a uniform prior probability density function, the Bayesian upper limits on the numbers of $D_{s J}^{-}$signal events ( $N_{\text {U.L. }}$ ) are determined at the $90 \%$ confidence level (C.L.) by solving the following equation

$$
\int_{0}^{N_{\mathrm{U} . \mathrm{L} .}} \mathcal{L}(x) d x=0.9 \int_{0}^{+\infty} \mathcal{L}(x) d x
$$

where $x$ is the assumed yield of the $D_{s J}^{-}$signal and $\mathcal{L}(x)$ is the maximized likelihood of the data assuming $x$ signal events. The results of $N_{\text {U.L. }}$ obtained by using above method are listed in Table I.

The Born cross sections of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s J}^{-}$are calculated using the formula
$\sigma_{B}\left(e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s J}^{-}\right)=\frac{N_{\text {fit }}}{\mathcal{L}_{\text {int }}(1+\delta)\left(1+\delta^{\mathrm{vp}}\right) \epsilon_{D_{s}^{*+}}}$,
where $N_{\text {fit }}$ is the fitted $D_{s J}^{-}$signal yield, $1+\delta$ is the radiative correction factor obtained from a QED calculation with $1 \%$ accuracy [51] using the ККМС generator, $1+\delta^{\mathrm{vp}}$ is the vacuum polarization factor, which is taken from Ref. [52] ( $\delta^{v p}$ is around 0.055 for all studied energy points), and $\mathcal{L}_{\text {int }}$ is the integrated luminosity at each energy point. The $D_{s}^{*+}$ reconstruction efficiency $\epsilon_{D_{s}^{*+}}$ is the product of the detection efficiency $\epsilon$ and the branching fractions for $D_{s}^{*+} \rightarrow \gamma D_{s}^{+}$and $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+} \quad(93.5 \%$ and $5.39 \%$, respectively [10]). The calculation of the upper limits on Born cross sections at $90 \%$ C.L. is performed analogously, replacing $N_{\text {fit }}$ with $N_{\text {U.L. }}$.

The measured Born cross sections of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s J}^{-}$ and the upper limits at $90 \%$ C.L. (with systematic uncertainties included) are summarized in Table I. The systematic uncertainties and the method to take them into account in the upper limits are discussed in Sec. V. The Born cross sections, with statistical uncertainties only, are shown in Fig. 2.

## V. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties of the measured cross sections of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}, \quad e^{+} e^{-} \rightarrow$ $D_{s}^{*+} D_{s 1}(2460)^{-}$, and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$are divided into two categories; multiplicative systematic uncertainties


FIG. 2. The Born cross sections of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 0}^{*}(2317)^{-}$ (the dots with error bars), $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2460)^{-}$(the rectangles with error bars), and $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$(the triangles with error bars) from 4.6 GeV to 4.7 GeV , where the error bars are statistical only. The energy points with signal significances less than $3 \sigma$ are marked empty, and the upper limits at $90 \%$ C.L. on their cross sections are given in Table I.
and additive systematic uncertainties. The multiplicative systematic uncertainties are associated with tracking and PID efficiencies, photon-detection efficiency, MC sample size, ISR and vacuum-polarization corrections, measurement of luminosity, the branching fractions of intermediate states, and the kinematic fit. The additive systematic uncertainties are associated with the $D_{s J}^{-}$mass, the background shape, and the fit range.

The uncertainties related to PID and tracking are determined to be $3.0 \%$ respectively [53]. The uncertainty of the photon reconstruction efficiency is $1.0 \%$, which is derived from the study of $J / \psi \rightarrow \rho^{0}\left(\rightarrow \pi^{+} \pi^{-}\right) \pi^{0}(\rightarrow \gamma \gamma)$ [54] events. The uncertainties due to finite sizes of the MC samples are determined to be at most $0.9 \%$ at each energy point, which arises from the statistical uncertainty of the selection efficiency measured from these samples. From an MC study, we find that the systematic uncertainty due to the choice of $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}$decay model is negligible. The shapes of the cross section of the processes $e^{+} e^{-} \rightarrow$ $D_{s}^{*+} D_{s J}^{-}$affect the radiative correction factor and the detection efficiency. Due to the limited number of events in the data sample, a detailed determination of the energy dependence ("line shape"), which would allow for an iterative determination of radiative correction factors, is not possible. Therefore, the input line shapes are changed to a first-order polynomial multiplied by $\sqrt{E_{m}-E_{0}}$, a function that reasonably describes the shape of available data, where $E_{m}$ stands for the c.m. energy and $E_{0}$ stands for the threshold energy for each process, and the differences in the selection efficiency $\varepsilon(1+\delta)$ are taken as the systematic uncertainties. The uncertainty from vacuum polarization is less than $0.1 \%$ [52], which is negligible compared to other sources of uncertainties. The integrated luminosities of the data samples are measured using large-angle Bhabha scattering events with an uncertainty less than $1.0 \%$. The
uncertainties in the branching fractions $\mathcal{B}\left(D_{s}^{+} \rightarrow\right.$ $\left.K^{+} K^{-} \pi^{+}\right)$and $\mathcal{B}\left(D_{s}^{*+} \rightarrow \gamma D_{s}^{+}\right)$are $2.8 \%$ and $0.7 \%$ [10], respectively. The uncertainty of the 2 C kinematic fit is estimated using control samples of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s}^{*-}$ events at $\sqrt{s}=4.42 \mathrm{GeV}$ and 4.6 GeV . The difference between the data and MC efficiencies due to the 2 C kinematic fit is $1.7 \%$, which is taken as the systematic uncertainty. Using a control sample of $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s}^{*-}$, the mass resolutions of $D_{s}^{*-}$ candidates between signal MC simulation and data are consistent. Thus, the systematic uncertainty due to mass resolution is negligible.

The uncertainties due to $D_{S J}^{-}$mass are estimated by varying its value by the measured uncertainty [10]. The differences in the fitted $D_{s J}^{-}$signal yields are taken as the systematic uncertainties. Using a control sample of $e^{+} e^{-} \rightarrow$ $D_{s}^{*+} D_{s}^{*-}$ decays, we find the resolution in missing mass to be essentially the same in data as in the MC, at the current level of statistics. The systematic uncertainties due to fitting itself, the background shape, and the fit range are estimated with a toy MC method. We simulate an ensemble of experiments, generating $D_{s}^{*+}$ recoil mass distributions based on the nominal fitted results. We generate 1000 distributions and subsequently fit them to obtain $D_{s J}^{-}$signal
yields. We plot these results in Gaussian distributions. The difference between the mean values of these distributions and the input signal yields represents the systematic bias or uncertainty due to the fitting procedure. The uncertainty is found to be negligible for all $D_{S J}^{-}$signals. A similar method is used to estimate the systematic uncertainties due to the fit range and the background shape. For the fit range, the lower bound is changed from $2.20 \mathrm{GeV} / c^{2}$ to $2.18 \mathrm{GeV} / c^{2}$ and to $2.22 \mathrm{GeV} / c^{2}$. For the background shape, instead of an ARGUS function [50], a polynomial $f(M)=(M-$ $\left.M_{a}\right)^{c}\left(M_{b}-M\right)^{d}$ is used, where $M_{a}$ and $M_{b}$ are the lower and upper thresholds of the $D_{s}^{*+}$ recoil mass distribution.

For those energy points with a $D_{s J}^{-}$statistical significance larger than $3 \sigma$, the central values of the cross section with statistical and systematic uncertainties are reported, and the systematic uncertainties are summarized in Table II. For the other energy points, the upper limits on the cross section at $90 \%$ C.L. are reported and the systematic uncertainties are taken into account in two steps. Firstly, among the additive systematic uncertainties described above, the most conservative upper limit at $90 \%$ C.L. is kept. Then, to take into account the multiplicative systematic uncertainty, the likelihood curve is convolved with a Gaussian function

TABLE II. Summary of the systematic uncertainties (\%) in $\sigma_{B}\left(e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s J}^{-}\right)$for those energy points with statistical significances larger than $3 \sigma$.

| Sources/ $\sqrt{s}(\mathrm{GeV})$ | $D_{s 0}^{*}(2317)^{-}$ |  | $D_{s 1}(2460)^{-}$ |  |  |  |  |  | $D_{s 1}(2536)^{-}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4.626 | 4.680 | 4.600 | 4.626 | 4.640 | 4.660 | 4.680 | 4.700 | 4.660 | 4.680 | 4.700 |
| Tracking, PID and photon detection | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 |
| MC statistics | 0.9 | 0.8 | 0.8 | 0.9 | 0.9 | 0.9 | 0.8 | 0.9 | 0.9 | 0.8 | 0.8 |
| Kinematic fit | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 |
| $D_{s J}^{-}$mass | 5.1 | 3.9 | 1.5 | 1.7 | 3.0 | 2.3 | 0.7 | 2.2 | 4.7 | 2.1 | 1.3 |
| Fit range | 3.2 | 2.9 | 6.2 | 0.4 | 2.1 | 2.6 | 0.9 | 1.5 | 8.1 | 1.5 | 1.5 |
| Background shape | 2.4 | 2.4 | 5.2 | 3.2 | 4.5 | 0.1 | 0.2 | 1.5 | 2.3 | 1.6 | 2.4 |
| ISR radiative correction | 2.5 | 2.7 | 3.2 | 2.3 | 1.8 | 1.0 | 0.1 | 0.9 | 3.6 | 1.9 | 0.8 |
| Luminosity | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| Branching fraction | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 |
| Total | 10.5 | 9.9 | 11.8 | 9.0 | 9.9 | 8.6 | 7.9 | 8.5 | 13.0 | 8.6 | 8.5 |

TABLE III. Summary of the multiplicative systematic uncertainties (\%) in $\sigma_{B}\left(e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s J}^{-}\right)$for those energy points with statistical significances less than $3 \sigma$.

|  | $D_{s 0}^{*}(2317)^{-}$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4.600 | 4.612 | 4.640 | 4.660 | 4.700 | $D_{s 1}(2460)^{-}$ |
| Sources $/ \sqrt{s}(\mathrm{GeV})$ | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 | 7.0 |
| Tracking, PID and photon detection | 0.8 | 0.9 | 0.9 | 0.8 | 0.9 | 0.9 |
| MC statistics | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 | 1.7 |
| Kinematic fit | 2.5 | 7.3 | 2.8 | 2.4 | 2.5 | 1.0 |
| ISR radiative correction | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| Luminosity | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 | 2.8 |
| Branching fraction | 8.3 | 10.7 | 8.4 | 8.2 | 8.3 | 9.3 |
| Total |  |  |  |  |  |  |

with a width parameter equal to the corresponding total multiplicative systematic uncertainty. All of the multiplicative systematic uncertainties for the energy points with a $D_{s J}^{-}$signal significance less than $3 \sigma$ are summarized in Table III. Assuming that all the sources are independent, the total systematic uncertainty is obtained by adding them in quadrature. The final results of the Born cross section with systematic uncertainties considered are listed in Table I, and shown in Fig. 2 with statistical error bars only.

## VI. SUMMARY

In summary, signals are observed in the $e^{+} e^{-} \rightarrow$ $D_{s}^{*+} D_{s 0}^{*}(2317)^{-}$process from $e^{+} e^{-}$collision data samples at c.m. energies of 4.626 GeV and 4.68 GeV , in the $e^{+} e^{-} \rightarrow$ $D_{s}^{*+} D_{s 1}(2460)^{-}$process from data samples at c.m. energies of $4.6 \mathrm{GeV}, 4.626 \mathrm{GeV}, 4.64 \mathrm{GeV}, 4.66 \mathrm{GeV}, 4.68 \mathrm{GeV}$, and 4.7 GeV , and the $e^{+} e^{-} \rightarrow D_{s}^{*+} D_{s 1}(2536)^{-}$process from data samples at c.m. energies of $4.66 \mathrm{GeV}, 4.68 \mathrm{GeV}$, and 4.7 GeV , all with statistical significances larger than $3 \sigma$. The Born cross sections of these processes are measured for the first time. The results are listed in Table I, and shown in Fig. 2 with statistical error bars only. No significant structures are observed in the measured cross sections.

## ACKNOWLEDGMENTS

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key R\&D Program of China under Contracts No. 2020YFA0406300 and No. 2020YFA0406400; National Natural Science

Foundation of China (NSFC) under Contracts No. 11625523, No. 11635010, No. 11735014, No. 11822506, No. 11835012, No. 11935015, No. 11935016, No. 11935018, No. 11961141012, No. 12022510, No. 12025502, No. 12035009, No. 12035013, and No. 12061131003; the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contracts No. U1732263 and No. U1832207; CAS Key Research Program of Frontier Sciences under Contract No. QYZDJ-SSW-SLH040; 100 Talents Program of CAS; Institute of Nuclear and Particle Physics, Astronomy and Cosmology (INPAC) and Shanghai Key Laboratory for Particle Physics and Cosmology; ERC under Contract No. 758462; European Union Horizon 2020 research and innovation programme under the Marie Sklodowska-Curie Grant Agreement No. 894790; German Research Foundation DFG under Contracts No. 443159800, Collaborative Research Center CRC 1044, FOR 2359, FOR 2359, GRK 214; Istituto Nazionale di Fisica Nucleare, Italy; Ministry of Development of Turkey under Contract No. DPT2006K-120470; National Science and Technology fund; Olle Engkvist Foundation under Contract No. 200-0605; STFC (United Kingdom); The Knut and Alice Wallenberg Foundation (Sweden) under Contract No. 2016.0157; The Royal Society, United Kingdom under Contracts No. DH140054 and DH160214; The Swedish Research Council; U.S. Department of Energy under Contracts No. DE-FG0205ER41374 and No. DE-SC-0012069.
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